

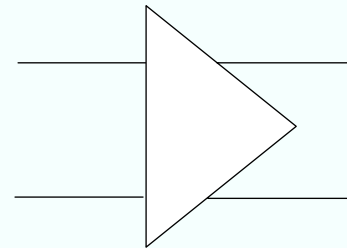
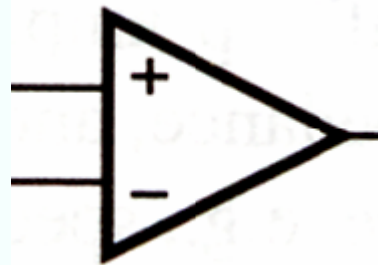
Ch 9 CMOS OP amp

- 1. Introduction**
- 2. 2-stage OP amp**
- 3. Folded cascode OP amp**
- 4. Design examples**

1. Introduction

OP amp :

- (1) Voltage amp : $V_o = A_{vd} * (V_{i+} - V_{i-})$
- (2) Differential input, single-ended output
- (3) Fully differential OP amp: diff output



Ideal OP amp :

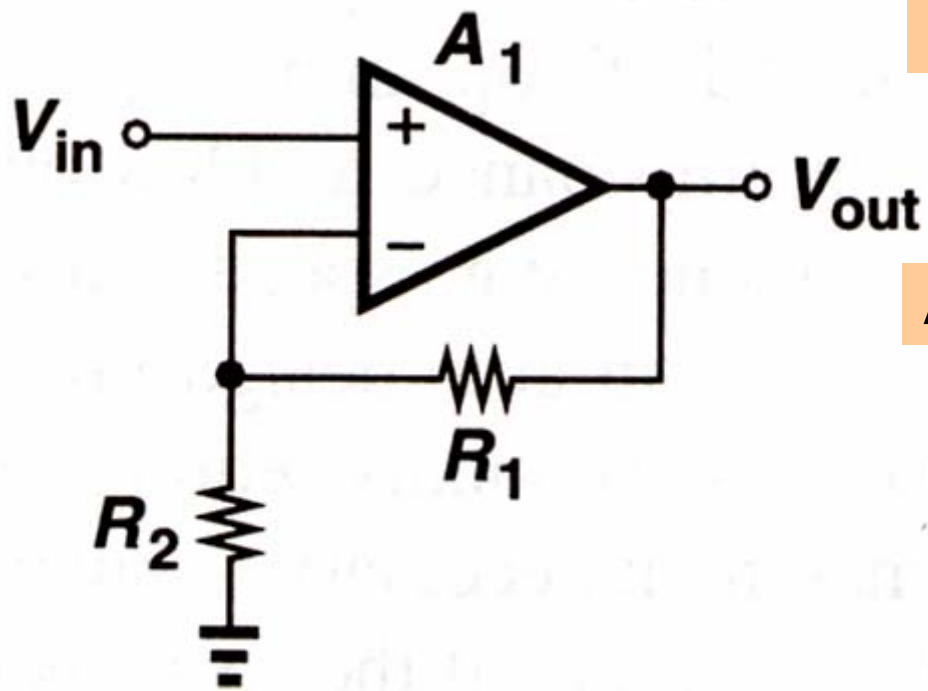
- (1) Differential mode voltage gain: infinity
- (2) Common mode voltage gain: 0
- (3) Input resistance: infinity
- (4) Output resistance: 0
- (5) Bandwidth: infinity

General purpose OP amp :

- (1) example 741 OP amp
- (2) small R_{out} to drive any load including R load
- (3) needs output stage

CMOS OP amp :

- (1) usually drive on-chip capacitive load only
- (2) large R_{out} \rightarrow current output \rightarrow OTA
(operational transconductance amplifier)
- (3) does not need output stage

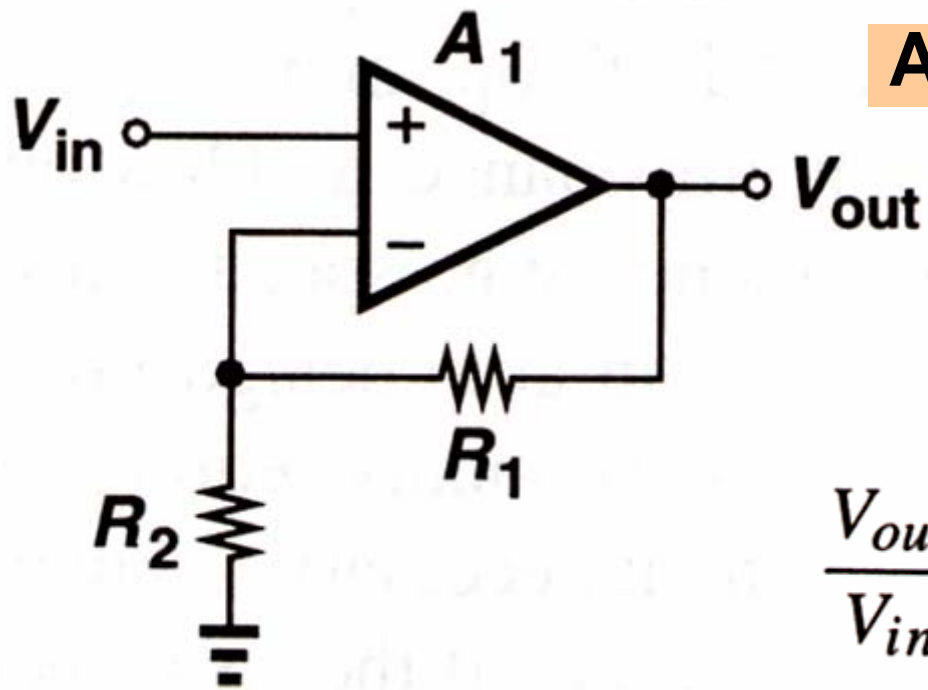


$A_1 = \text{infinity} \rightarrow \text{gain} = 1 + (R_1/R_2)$

$A_1 = ?$ for gain error $< 1\%$

$$V_{out} = A_1 \cdot \left(V_{in} - \frac{R_2}{R_1 + R_2} \cdot V_{out} \right)$$

$$\begin{aligned} \frac{V_{out}}{V_{in}} &= \frac{A_1}{1 + \frac{R_2}{R_1 + R_2} A_1} \\ &= \frac{R_1 + R_2}{R_2} \frac{A_1}{\frac{R_1 + R_2}{R_2} + A_1} \end{aligned}$$

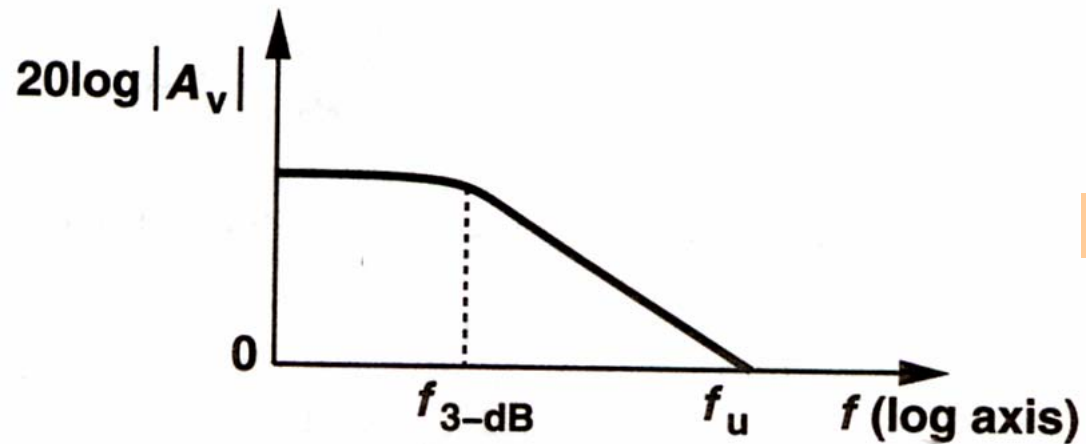


$A_1 = ?$ for gain error $< 1\%$

$$\frac{V_{out}}{V_{in}} \approx \left(1 + \frac{R_1}{R_2}\right) \left(1 - \frac{R_1 + R_2}{R_2} \frac{1}{A_1}\right)$$

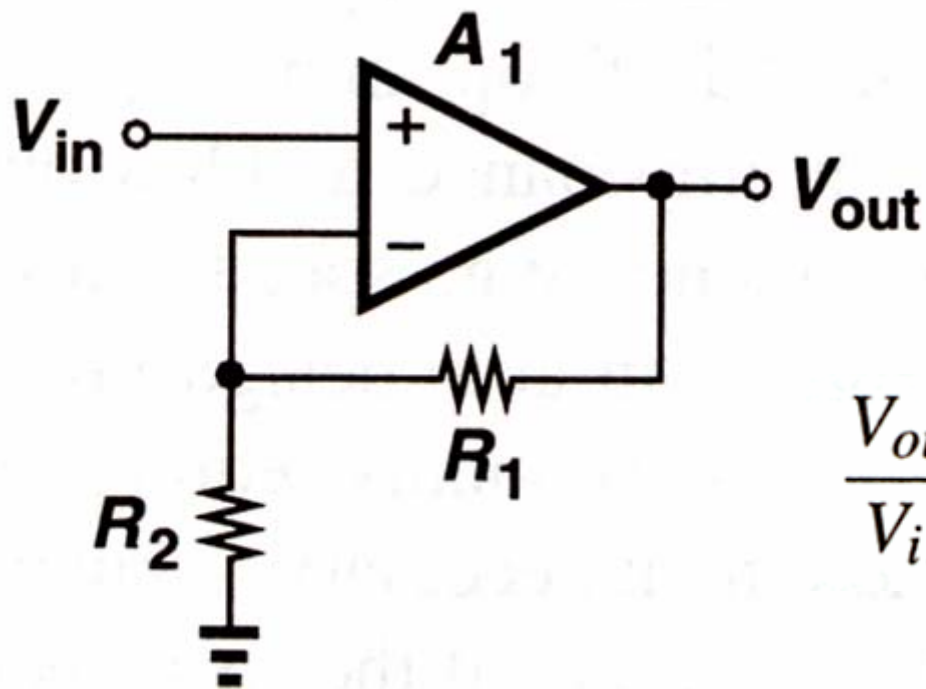
for gain error $< 1\%$

$$A_1 > 100 \cdot \frac{R_1 + R_2}{R_2}$$



$$A(s) = A_0 / (1 + s/\omega_0)$$

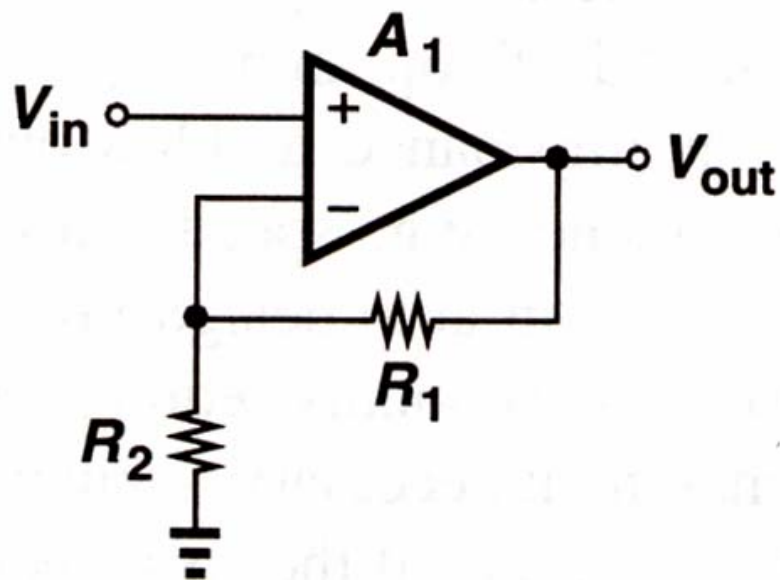
Single pole characteristic assumed



$$\frac{V_{out}}{V_{in}}(s) =$$

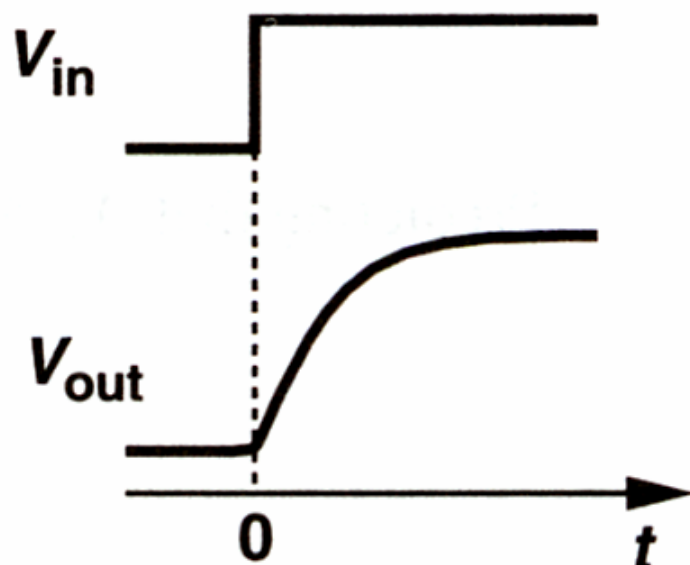
$$\left(V_{in} - V_{out} \frac{R_2}{R_1 + R_2} \right) A(s) = V_{out}$$

$$\frac{A_0}{1 + \frac{R_2}{R_1 + R_2} A_0} = \frac{V_{out}}{V_{in}}(s) = \frac{A_0}{1 + \frac{R_2}{R_1 + R_2} A_0} \frac{1}{1 + \frac{R_2}{R_1 + R_2} A_0 \omega_0}$$



$$\frac{V_{out}}{V_{in}}(s) = \frac{\frac{A_0}{1 + \frac{R_2}{R_1 + R_2} A_0}}{1 + \frac{\left(1 + \frac{R_2}{R_1 + R_2} A_0\right) \omega_0}{s}}$$

Step response

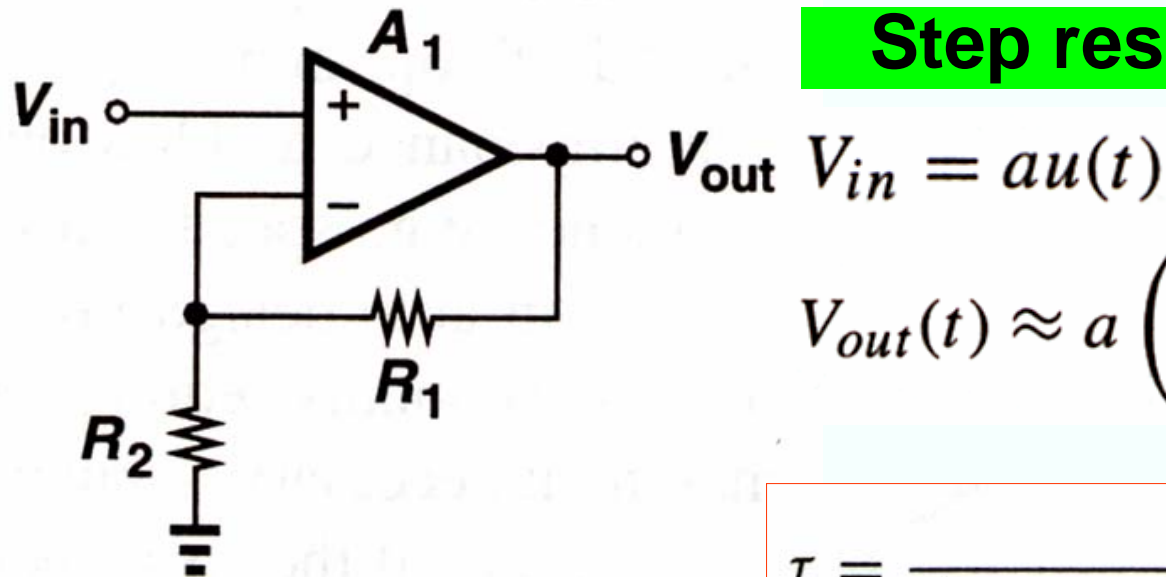


$$V_{in} = au(t)$$

$$V_{out}(t) \approx a \left(1 + \frac{R_1}{R_2}\right) \left(1 - \exp\left(-\frac{t}{\tau}\right)\right) u(t)$$

$$\tau = \frac{1}{\left(1 + \frac{R_2}{R_1 + R_2} A_0\right) \omega_0} \approx \left(1 + \frac{R_1}{R_2}\right) \frac{1}{A_0 \omega_0}$$

Step response

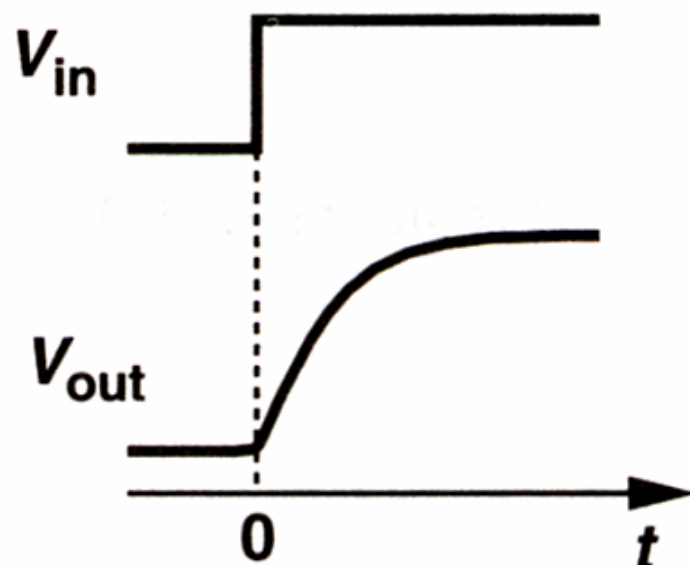


$$V_{in} = au(t)$$

$$V_{out}(t) \approx a \left(1 + \frac{R_1}{R_2} \right) \left(1 - \exp \frac{-t}{\tau} \right) u(t)$$

$$\tau = \frac{1}{\left(1 + \frac{R_2}{R_1 + R_2} A_0 \right) \omega_0} \approx \left(1 + \frac{R_1}{R_2} \right) \frac{1}{A_0 \omega_0}$$

reduced by $1+(\text{loop gain})$



For 1% settling, $V_{out} = 0.99V_F$

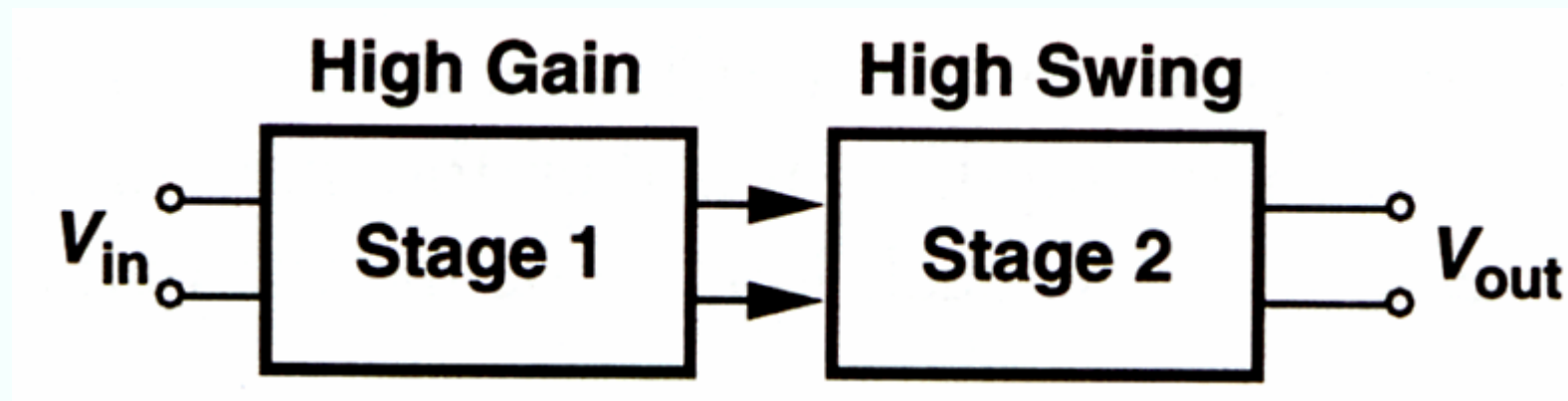
$$t_{1\%} = \tau \ln 100 \approx 4.6\tau$$

**Simple differential pair : voltage gain not enough
(< 20 for submicron devices)**

For high gain

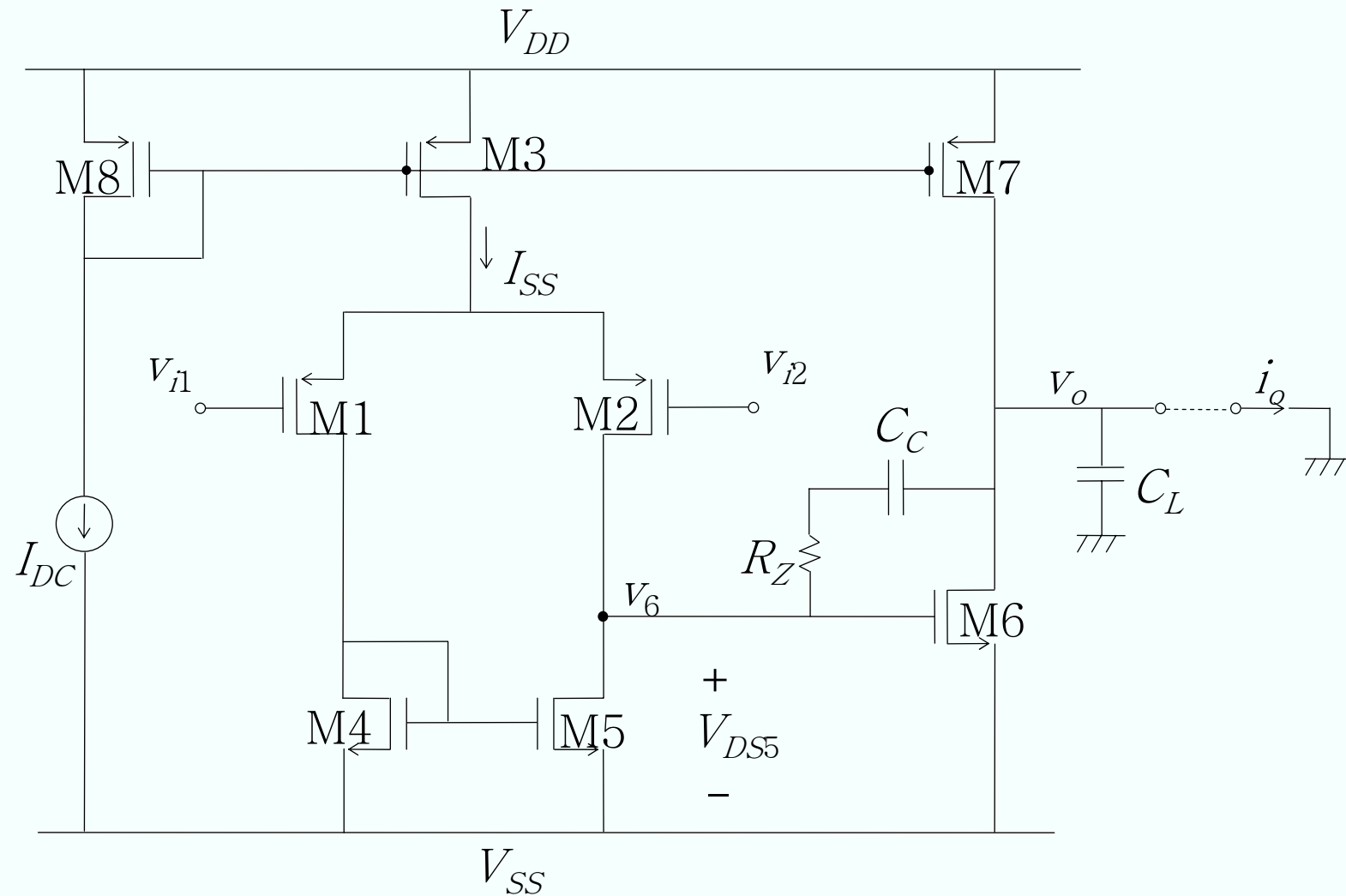
- 1-stage cascode OP amp (gain boost optional)
(telescopic OP amp, folded cascode OP amp)**
- reduced output swing**

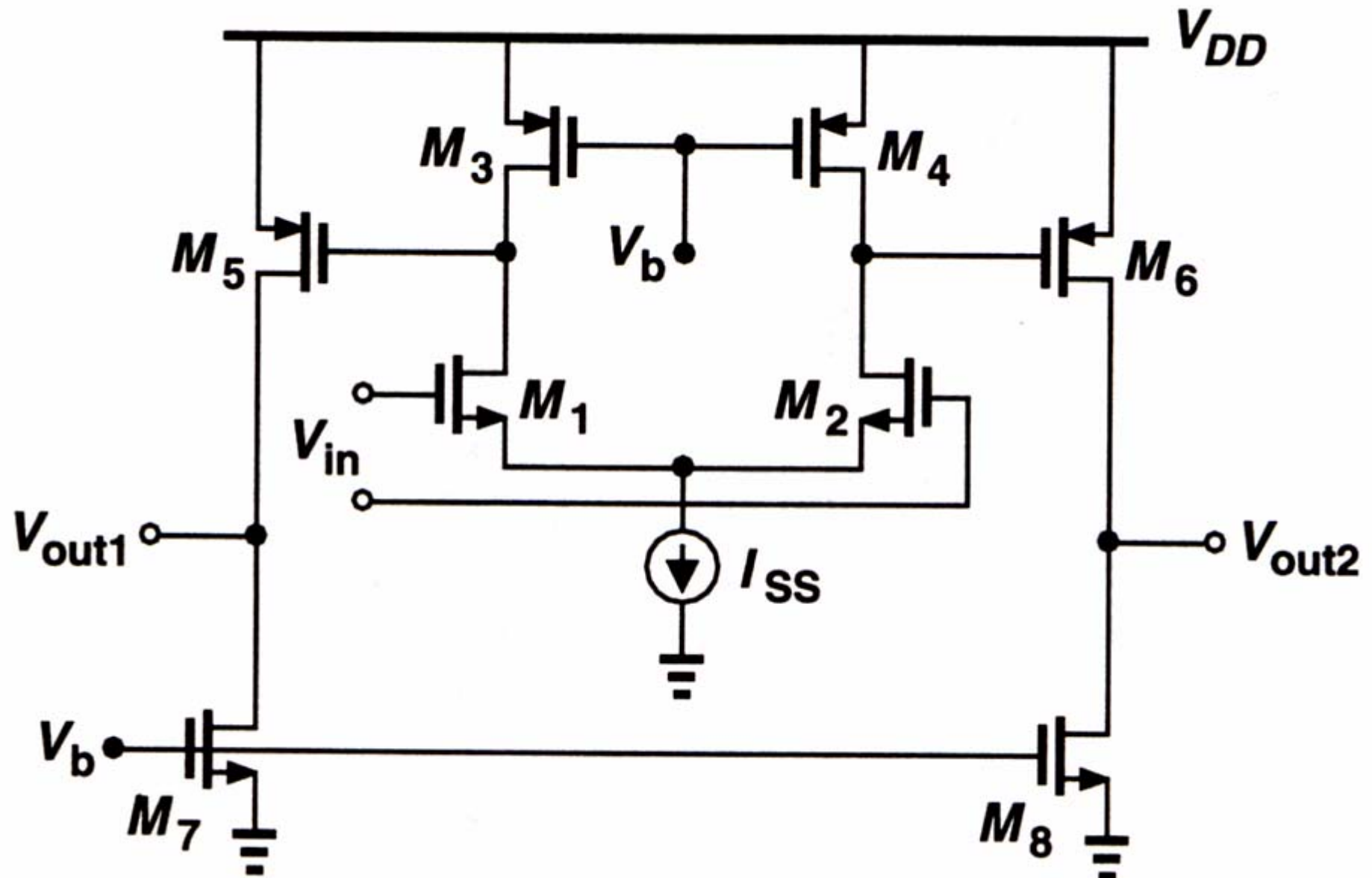
2-stage OP amp : pro → high gain + large output swing

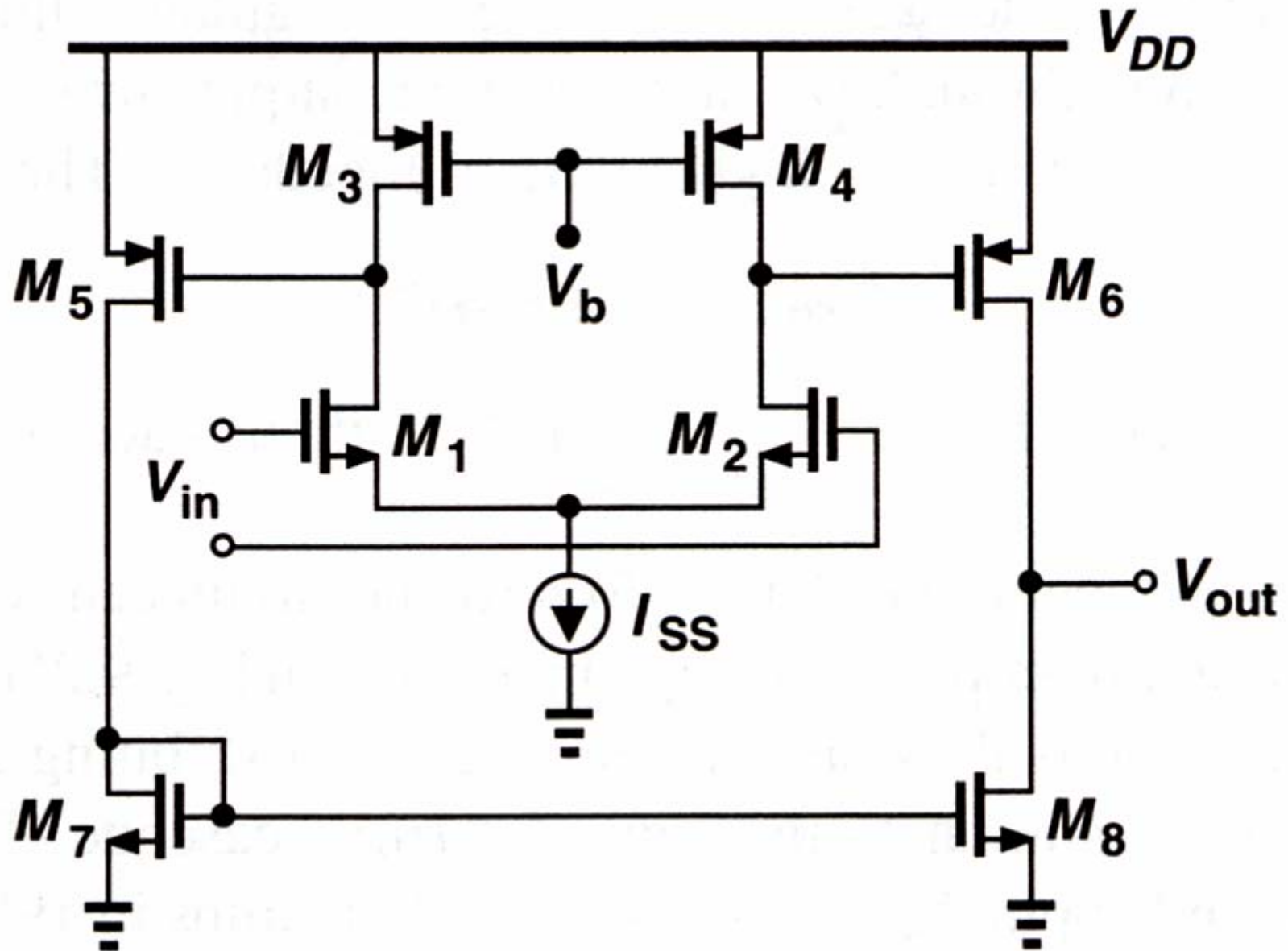


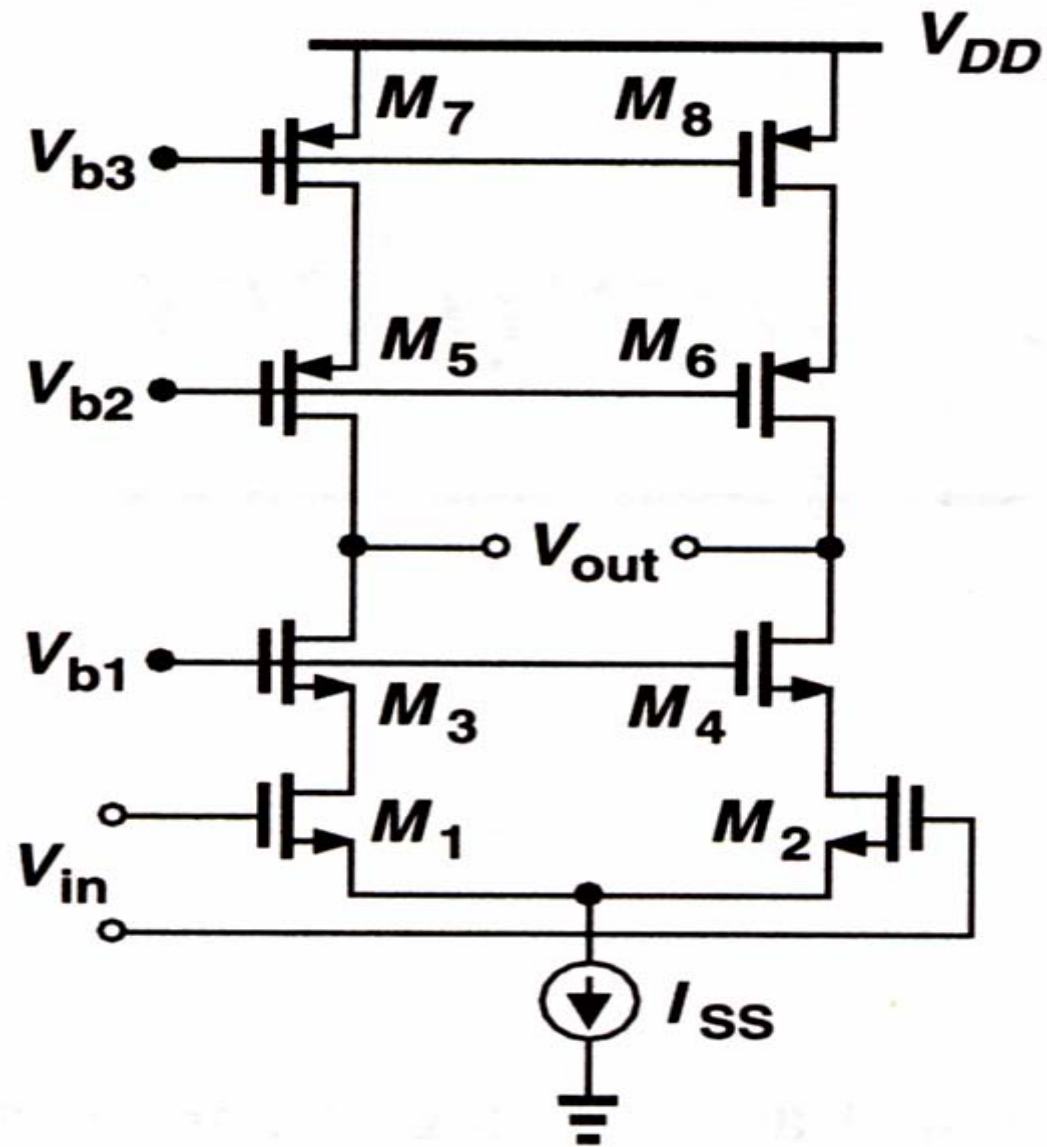
2-stage OP amp :

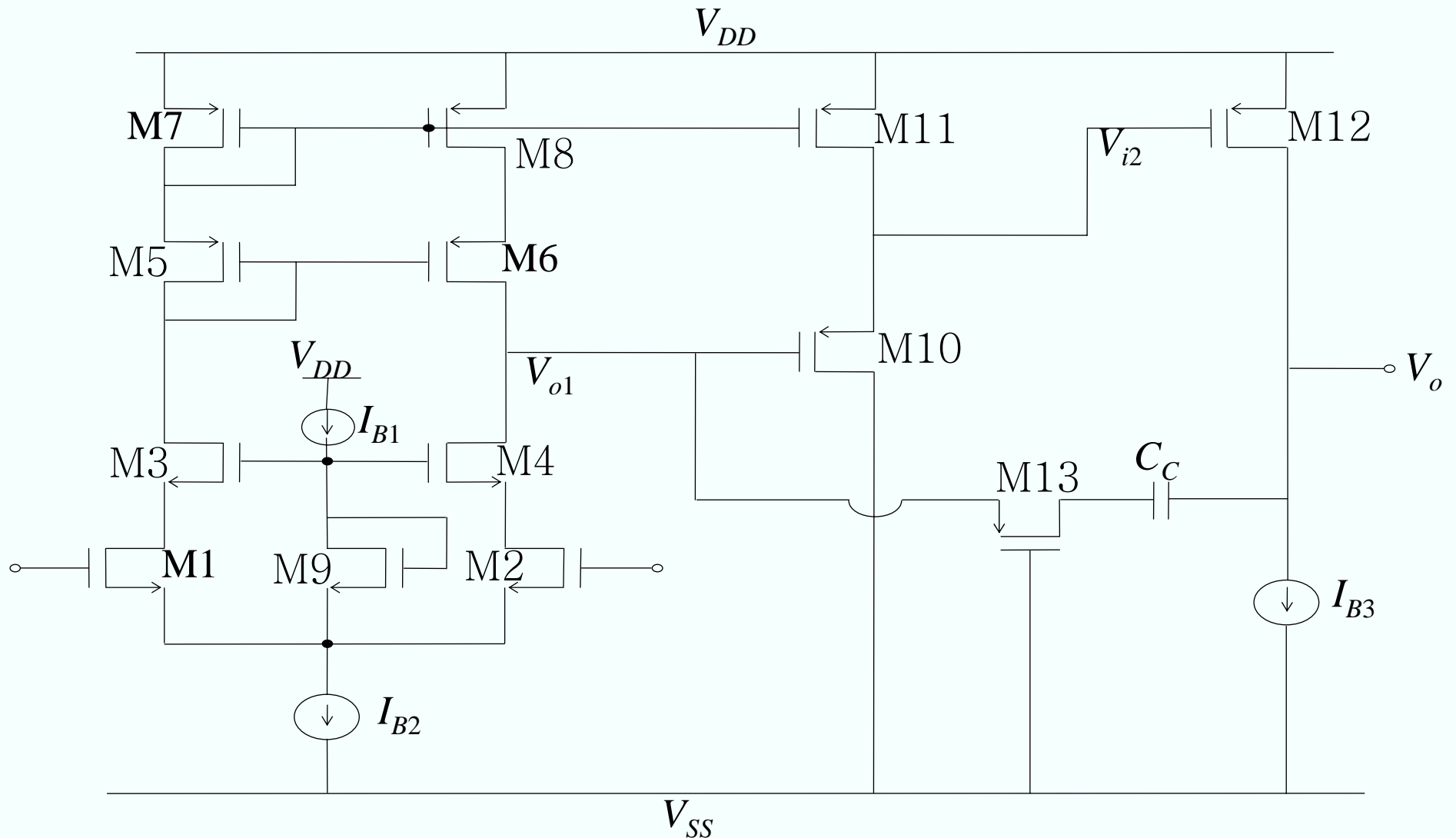
con → requires frequency compensation (Miller pole-splitting frequency compensation)

**Fig 9.1.1** 2-stage CMOS OP amp circuit

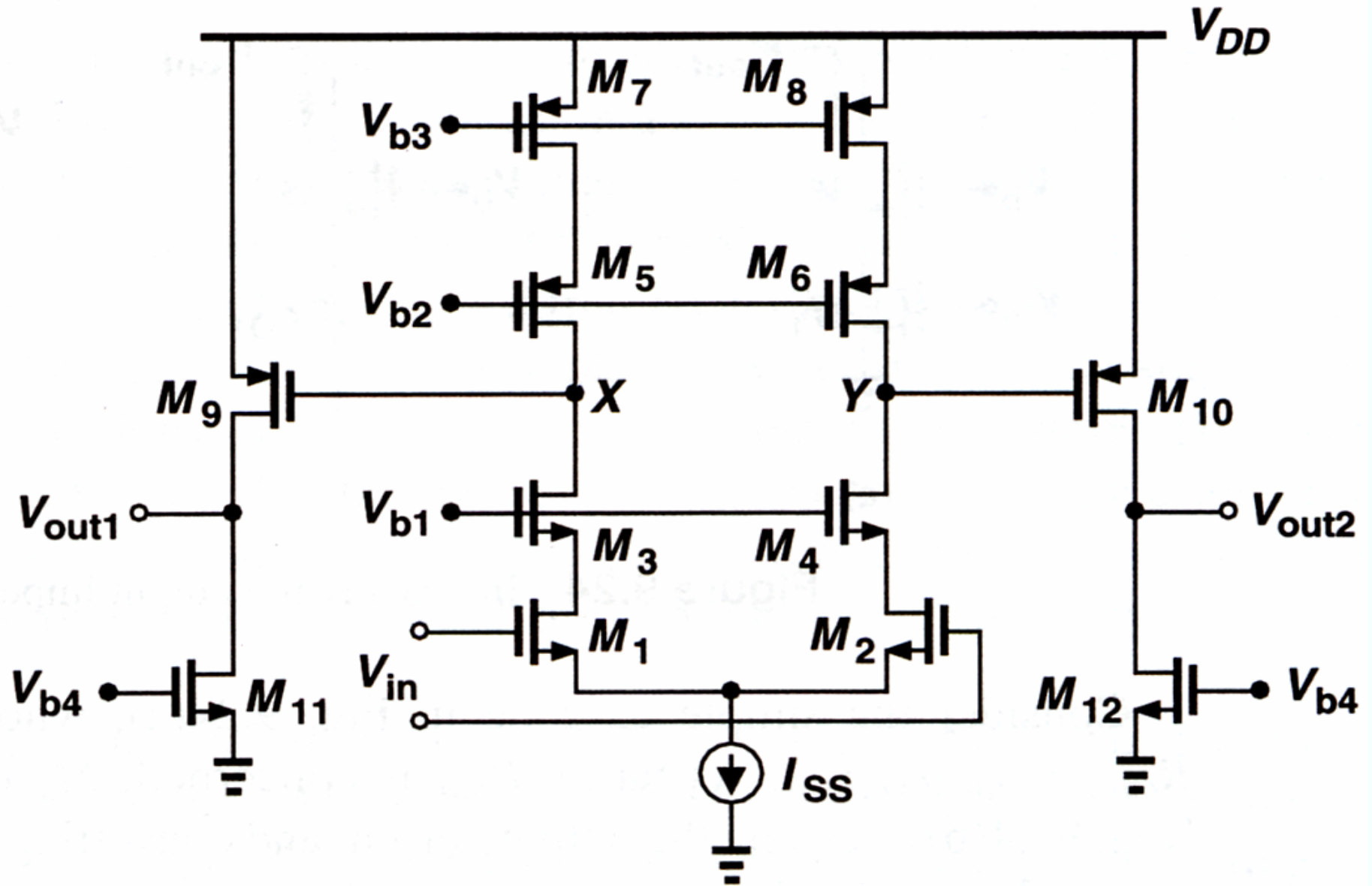


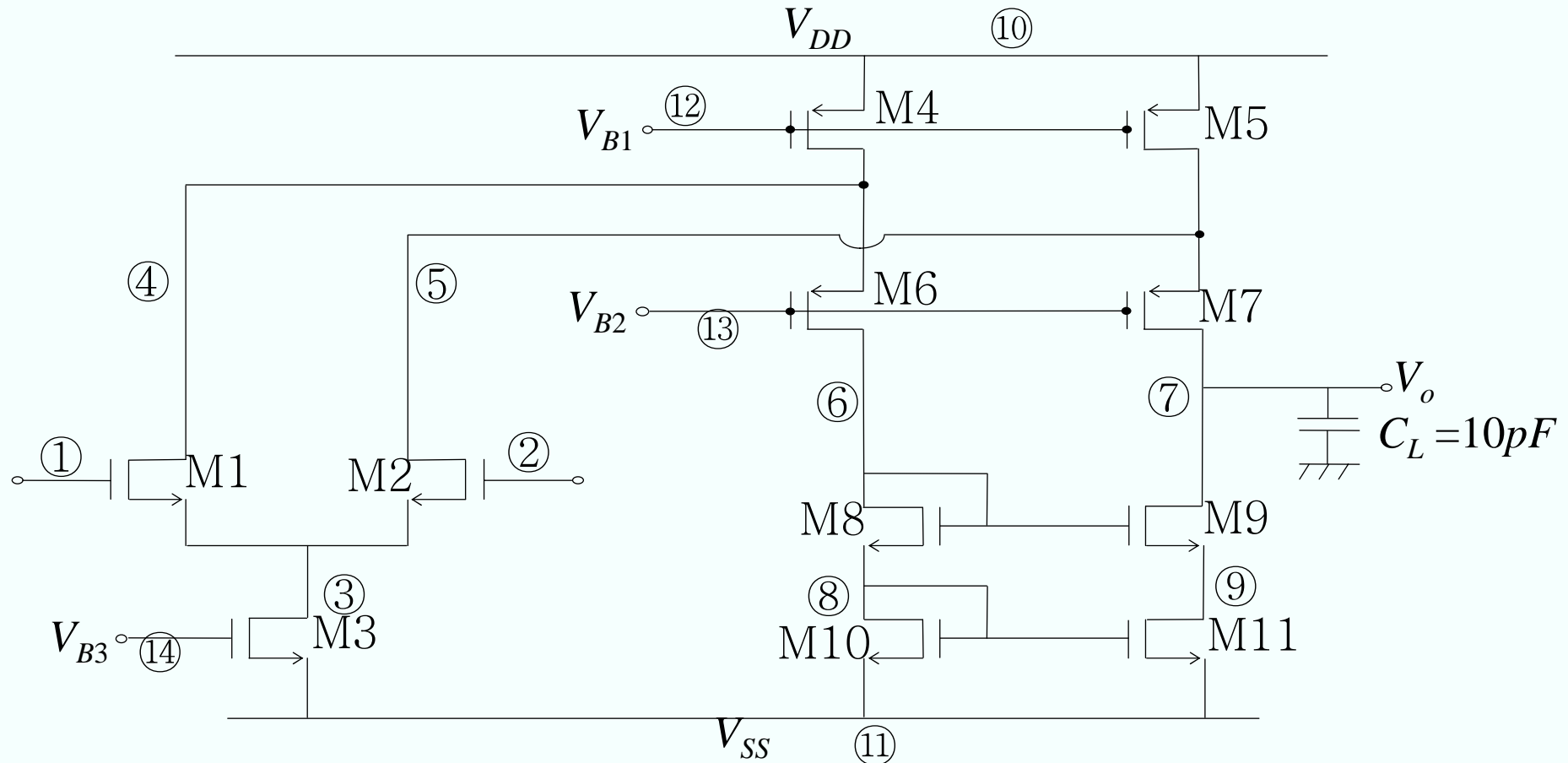




**Fig 9.1.22** 2-stage CMOS OP amp with a cascode 1st stage

M9 config. increases input common mode range





- (1) Input common mode range: extended up to VDD
- (2) Output voltage range increased compared to telescopic

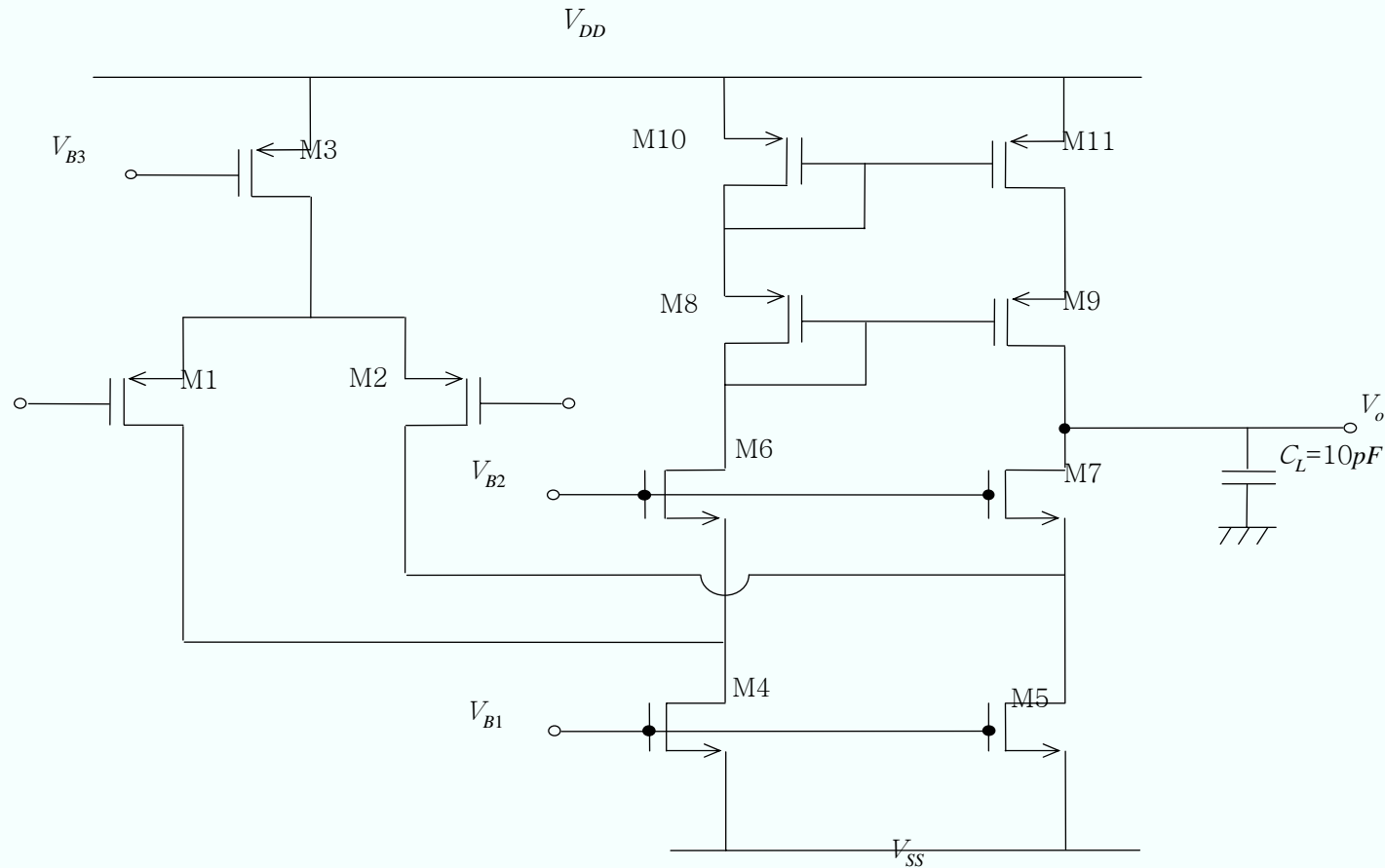
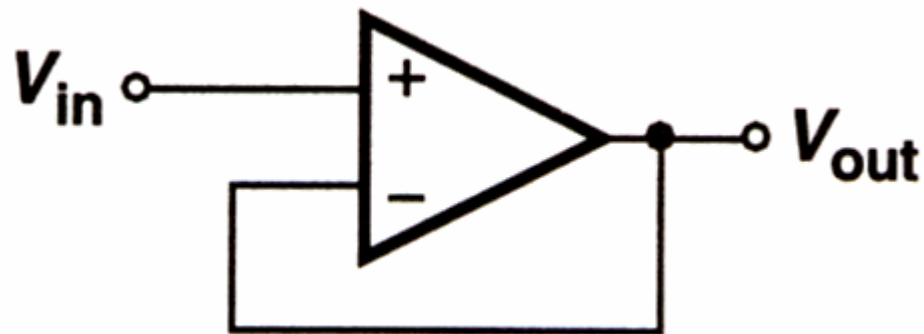


Fig 9.2.9 folded cascode CMOS OP amp with PMOS input transistors(M1, M2)

- (1) **Input common mode range: extended down to VSS**
- (2) **Output voltage range increased** compared to telescopic

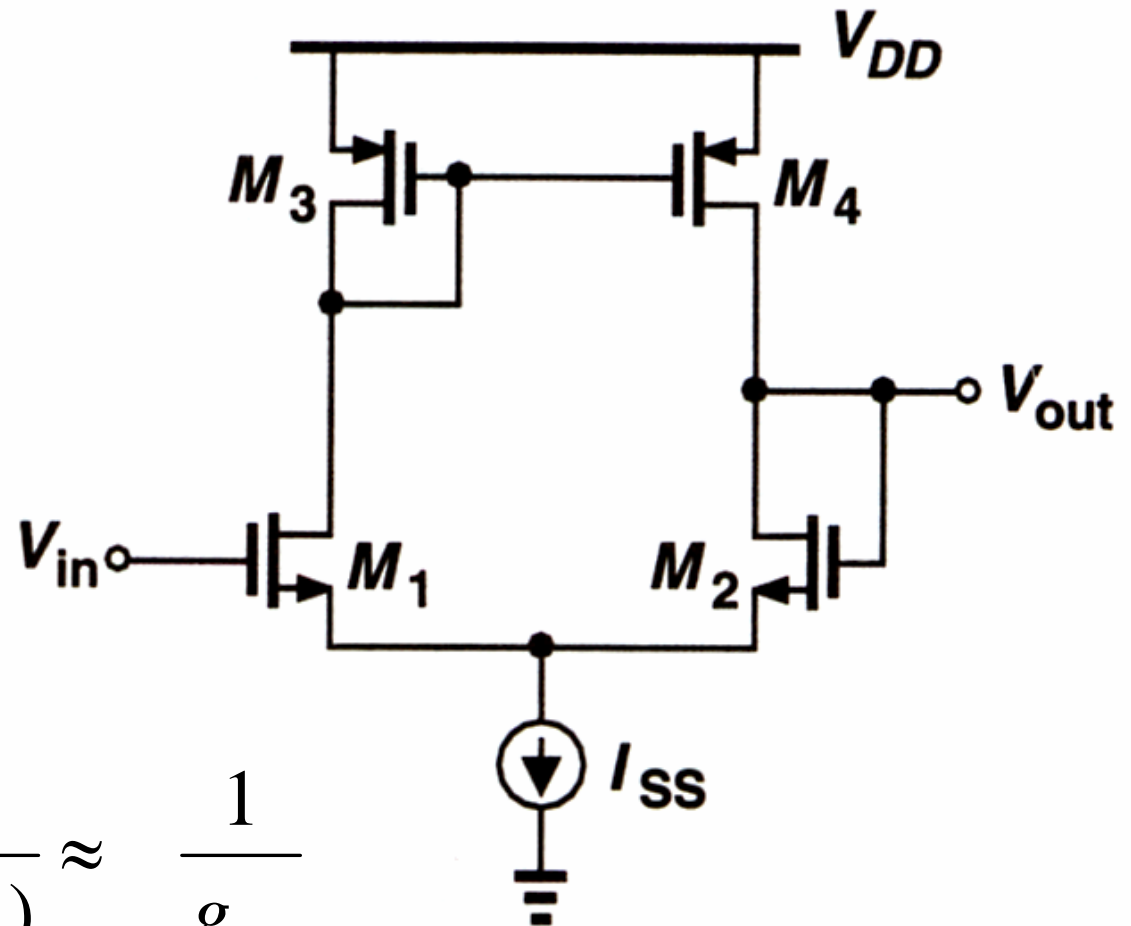
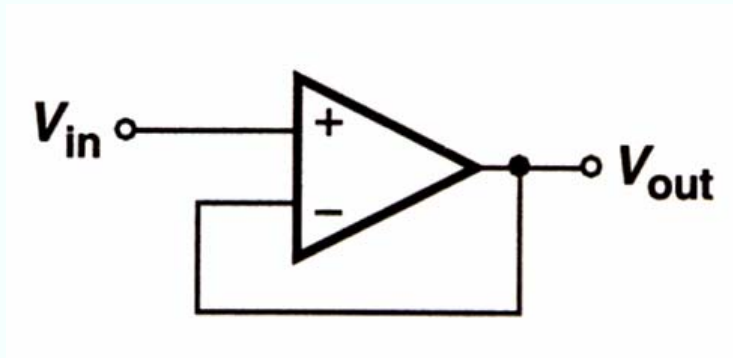


$$V_{out} \approx V_{in}$$

→ Must meet both output swing requirement and input CM voltage range requirement simultaneously

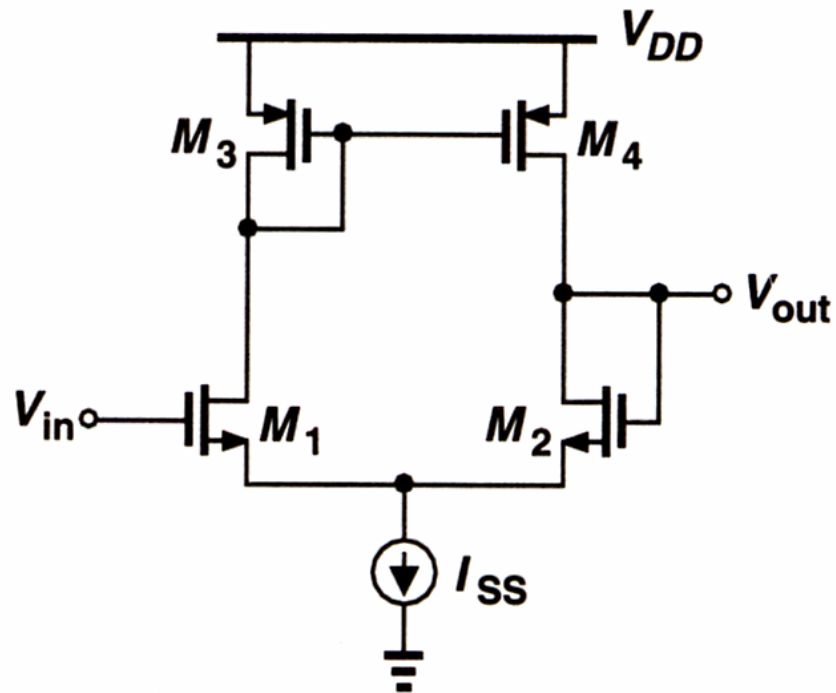
Telescopic OP amp : narrow output swing and narrow input common mode range → not suitable for unity-gain buffer application (folded cascode OK)

Unity gain buffer using simple diff pair



$$R_{out} = \frac{r_{o2} \parallel r_{o4}}{1 + g_{m1} \cdot (r_{o2} \parallel r_{o4})} \approx \frac{1}{g_{m1}}$$

Unity gain buffer using simple diff pair



Assume the same V_{DSAT}

(For open loop)

Input CM min: $2 V_{DSAT} + V_{TH}$

Input CM max: $V_{DD} - V_{DSAT}$

Output min: $2 V_{DSAT}$

Output max: $V_{DD} - V_{DSAT}$

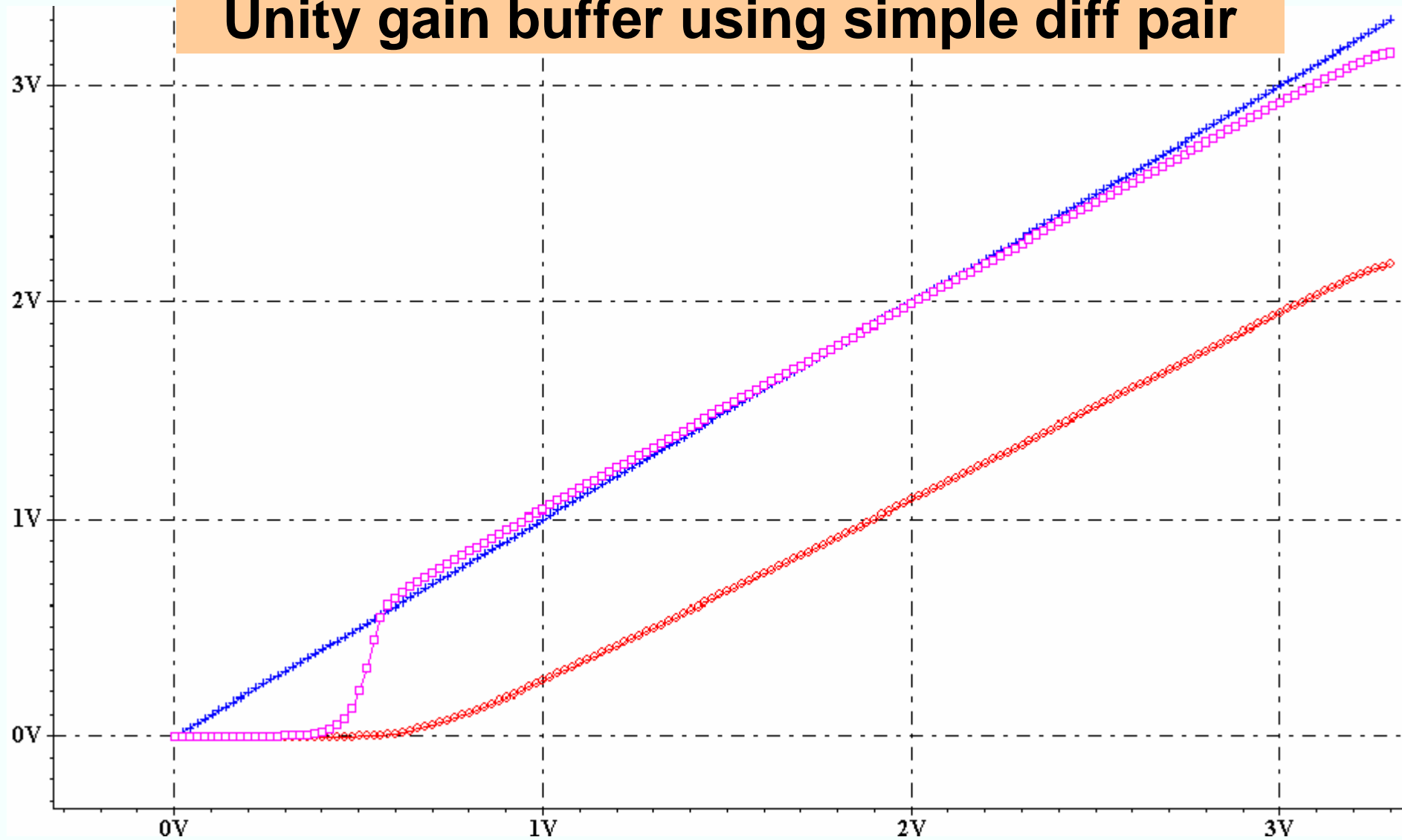
(For unity-gain feedback)

V_{out} min: $2 V_{DSAT} + V_{TH}$ (limited by input CM)

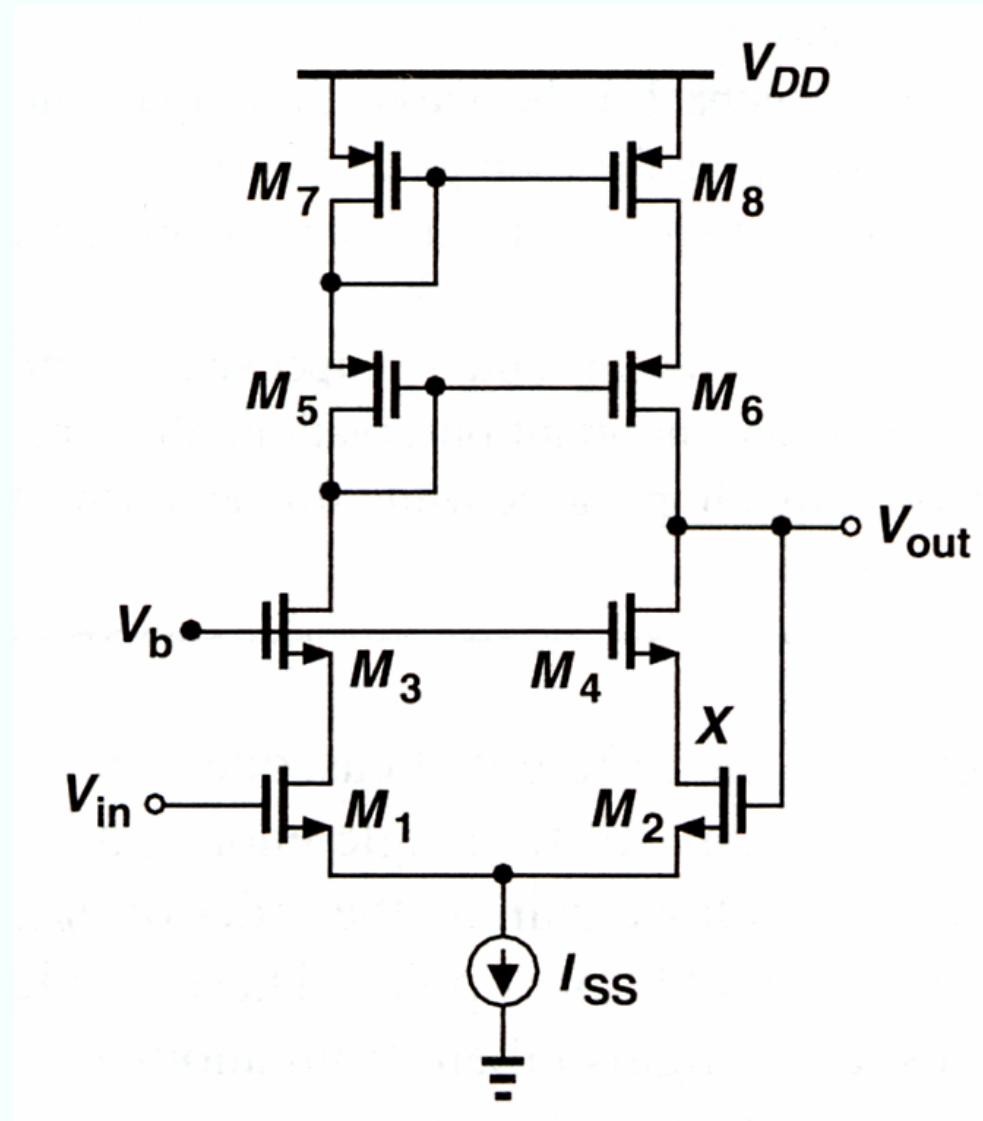
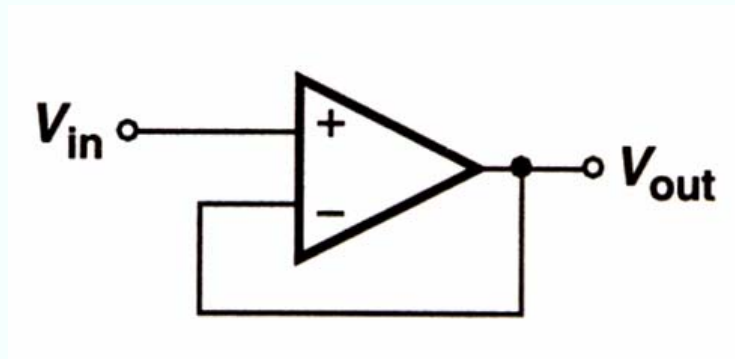
V_{out} max: $V_{DD} - V_{DSAT}$

V_{out} swing: $V_{DD} - 3 V_{DSAT} - V_{TH}$

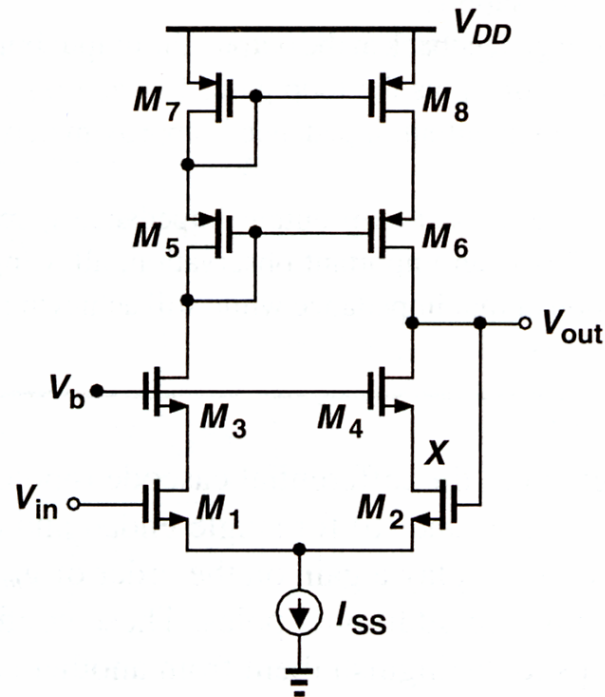
Unity gain buffer using simple diff pair



Unity gain buffer using telescopic OP amp



Unity gain buffer using telescopic OP amp



Assume the same V_{DSAT}

(For open loop, optimum V_b)

Input CM min: $2 V_{DSAT} + V_{TH}$

Input CM max: $V_{DD} - 3 V_{DSAT} - V_{TH}$

Output min: $3 V_{DSAT}$

Output max: $V_{DD} - 2 V_{DSAT} - V_{TH}$

(For unity-gain feedback , optimum V_b)

V_{out} min: $2 V_{DSAT} + V_{TH}$ (limited by input CM)

V_{out} max: $V_{DD} - 3 V_{DSAT} - V_{TH}$ (limited by input CM)

V_{out} swing: $V_{DD} - 5 V_{DSAT} - 2 V_{TH}$ (severely limited)