

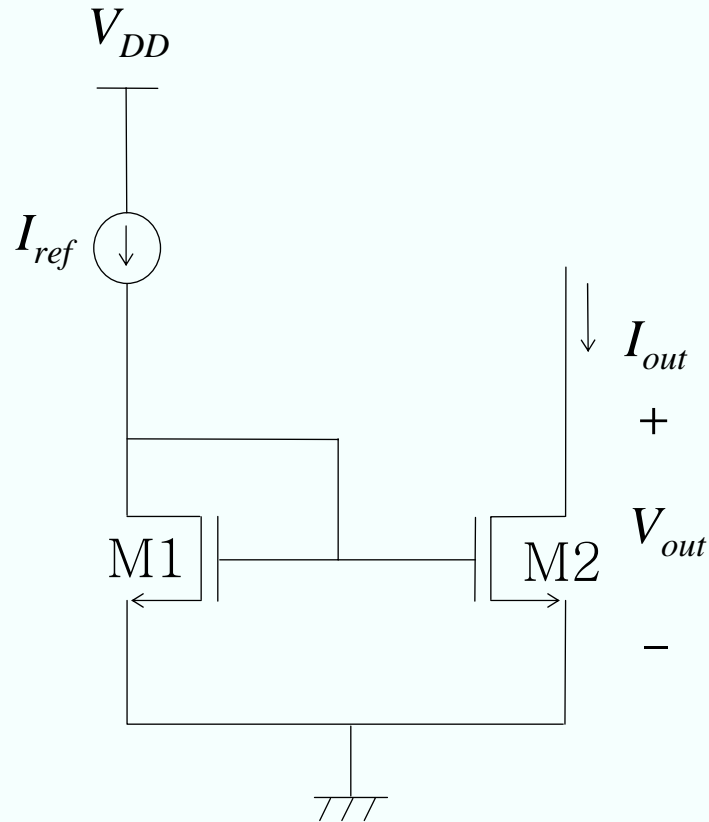
CH8 Current source and bias circuit

8.1 Current source

8.2 Bias circuit

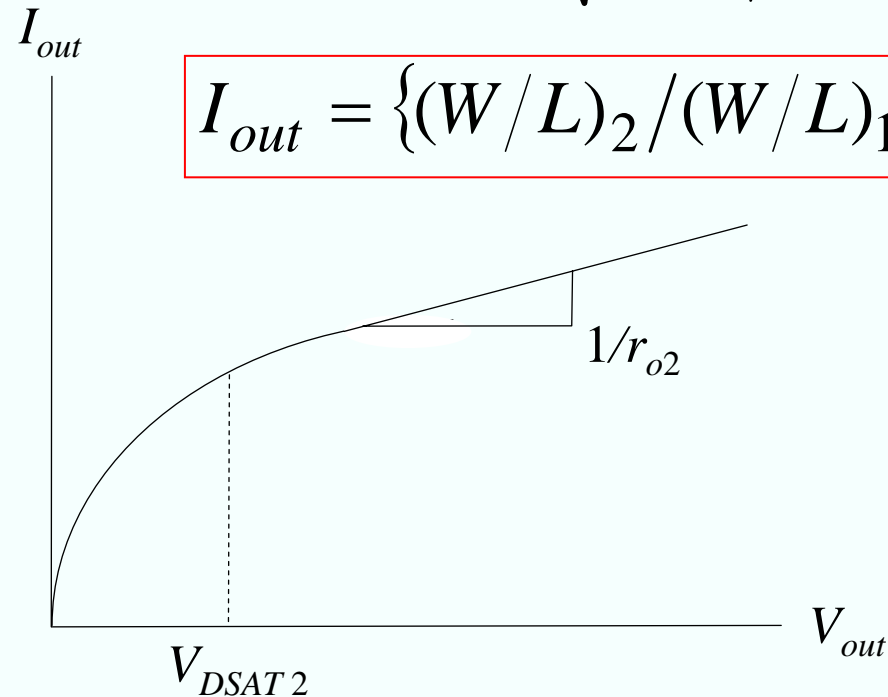
8.1 Current source

1. Current mirror current source
2. Cascode current source
3. Triple cascode current source
4. Multiple-output cascode current source
5. Wide swing cascode current sources 1, 2, 3



$$V_{GS2} = V_{TH} + \sqrt{2I_{ref} / \{\mu C_{ox} (W/L)_1\}}$$

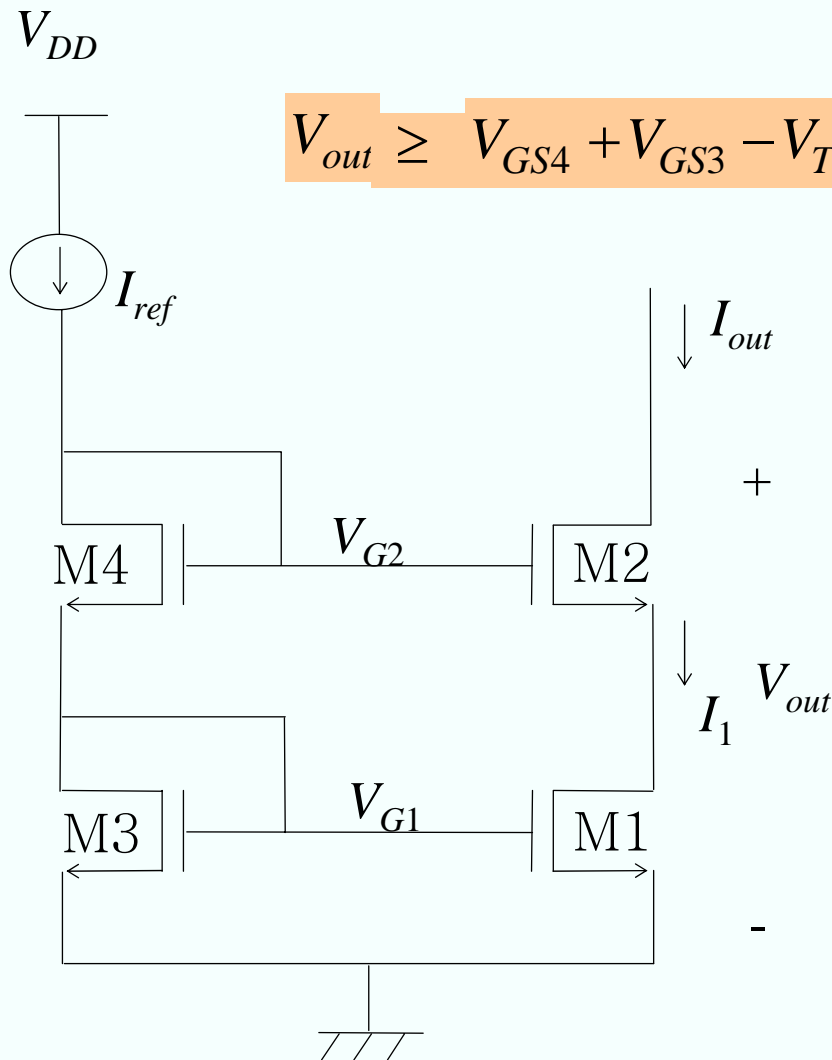
$$I_{out} = \{(W/L)_2 / (W/L)_1\} \cdot I_{ref}$$



I_{ref} and M1 decide V_{GS1} (V_{GS2}) \rightarrow $V_{GS2} = DC$ voltage

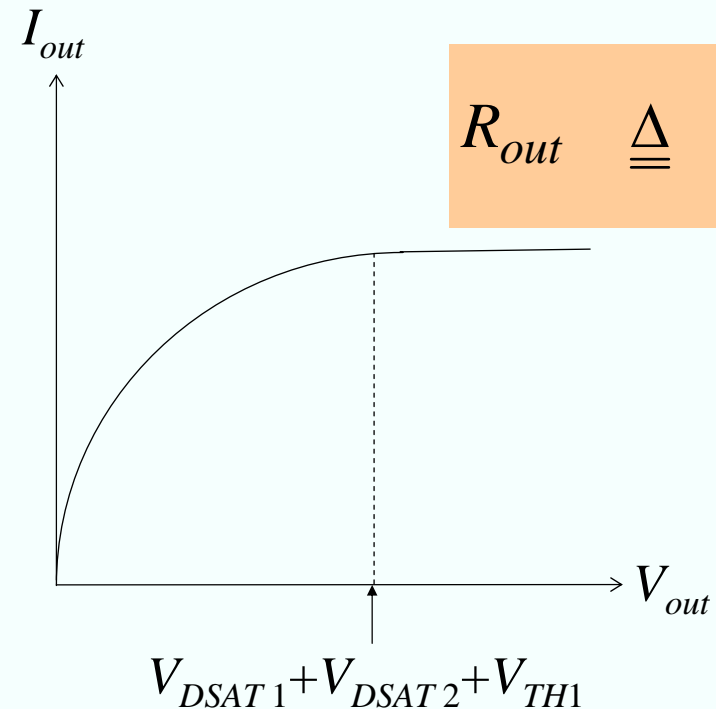
$$V_{DS1} = V_{GS4} + V_{GS3} - V_{GS2} = V_{GS3} = V_{GS1} > V_{GS1} - V_{TH}$$

M1 : saturation

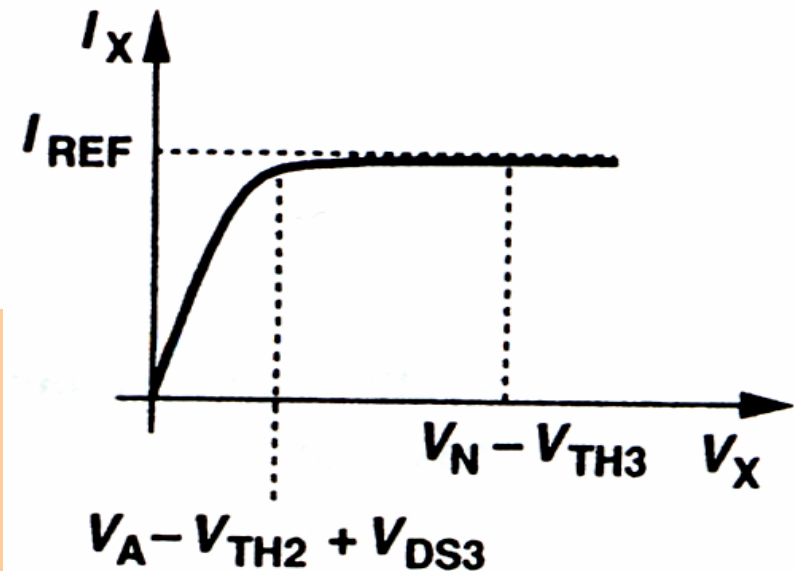
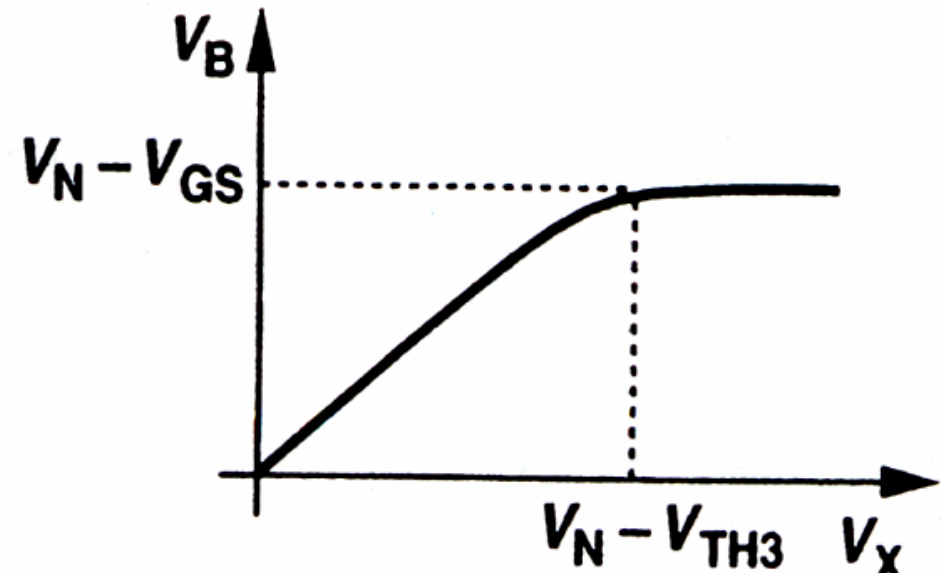
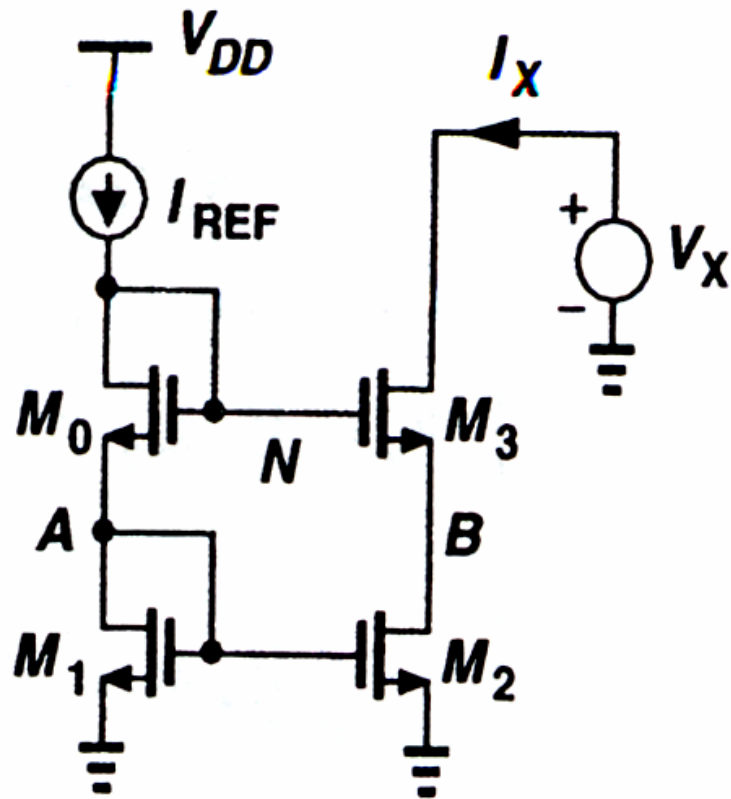


$$V_{out} \geq V_{GS4} + V_{GS3} - V_{TH2} = V_{GS2} + V_{GS1} - V_{TH2} = V_{DSAT2} + V_{DSAT1} + V_{TH1}$$

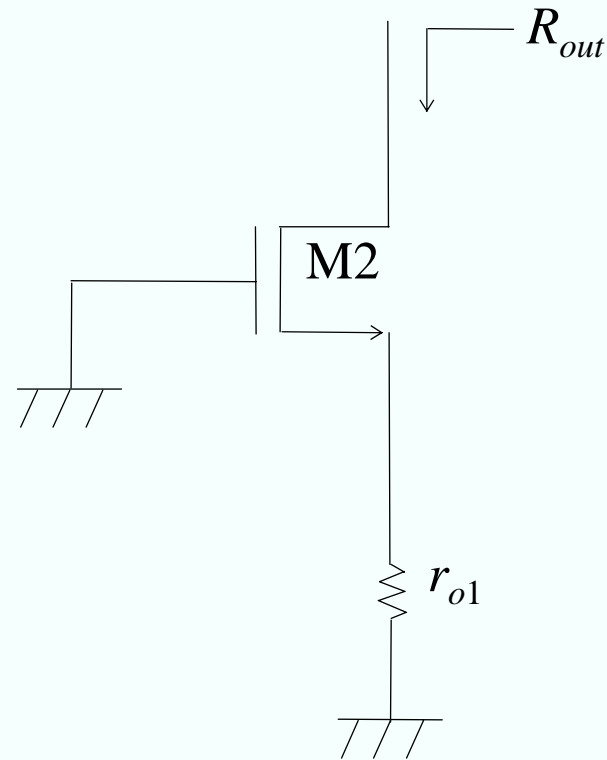
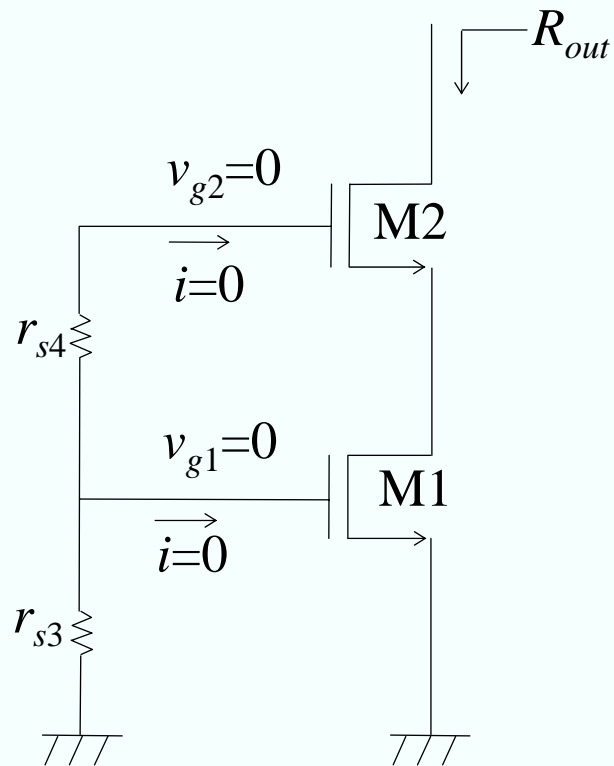
M2 : saturation



$$R_{out} \triangleq \frac{\Delta V_{out}}{\Delta I_{out}}$$

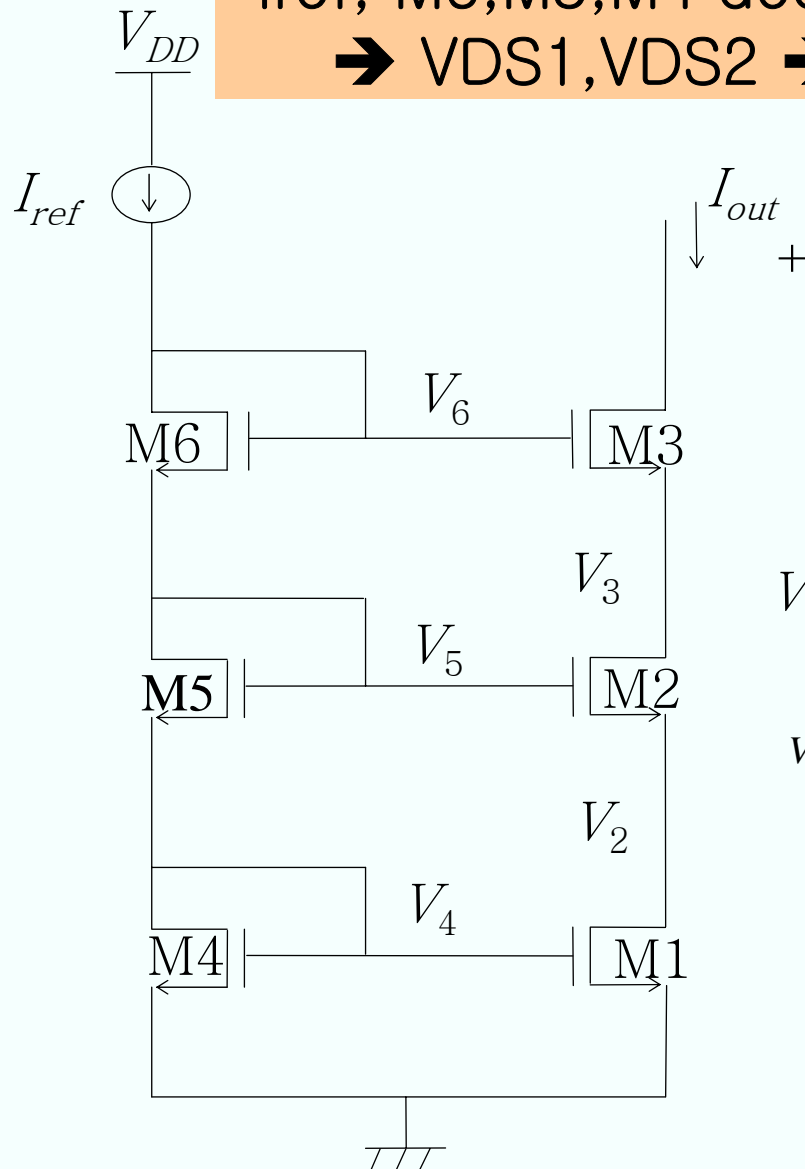


As V_x increases starting at 0, M_2 & M_3 in triode initially, M_2 in saturation & M_3 in triode, then M_2 & M_3 in saturation.



$$R_{out} = g_{m2}r_{o2} \cdot r_{o1} + r_{o1} + r_{o2} \approx g_{m2}r_{o2} \cdot r_{o1}$$

I_{ref} , M6, M5, M4 decide $V_6, V_5, V_4 \rightarrow V_{GS1} \rightarrow V_{GS2}, V_{GS3}$
 $\rightarrow V_{DS1}, V_{DS2} \rightarrow I_{out}$ almost constant \rightarrow very high R_{out}



$$V_{out} \quad V_{DS1} = V_{GS5} + V_{GS4} - V_{GS2} = V_{GS4} = V_{GS1} > (V_{GS1} - V_{TH1})$$

M1 : saturation

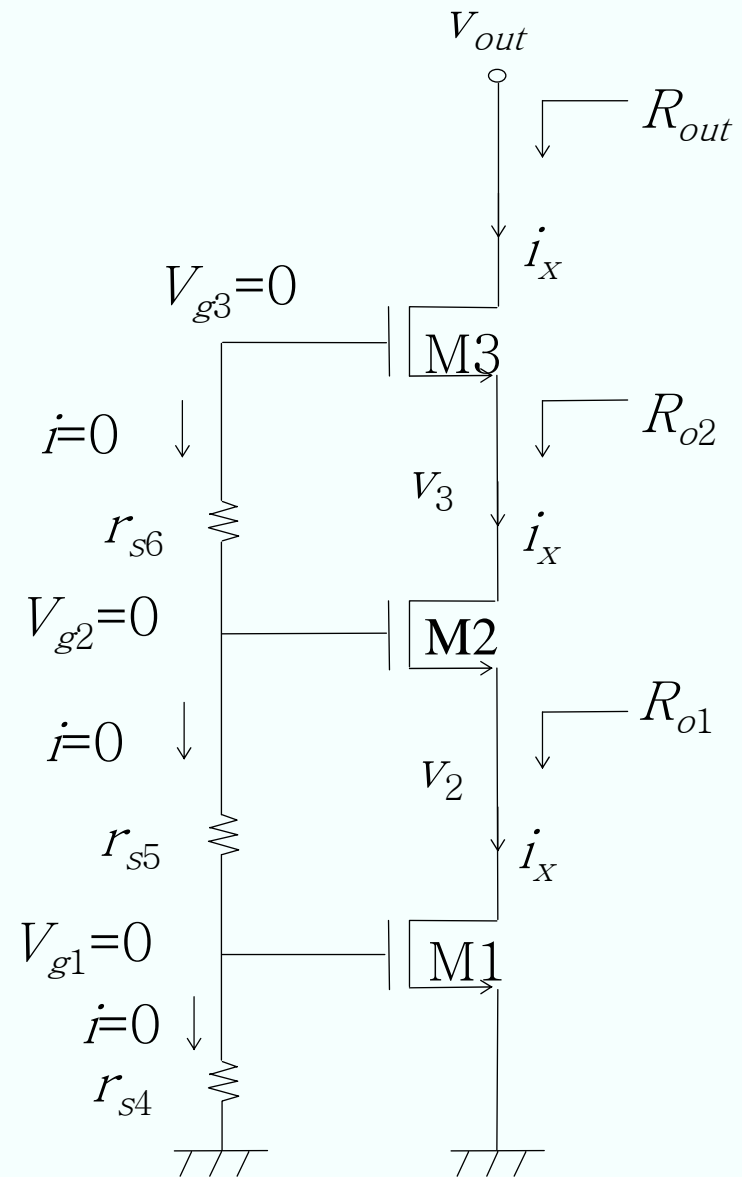
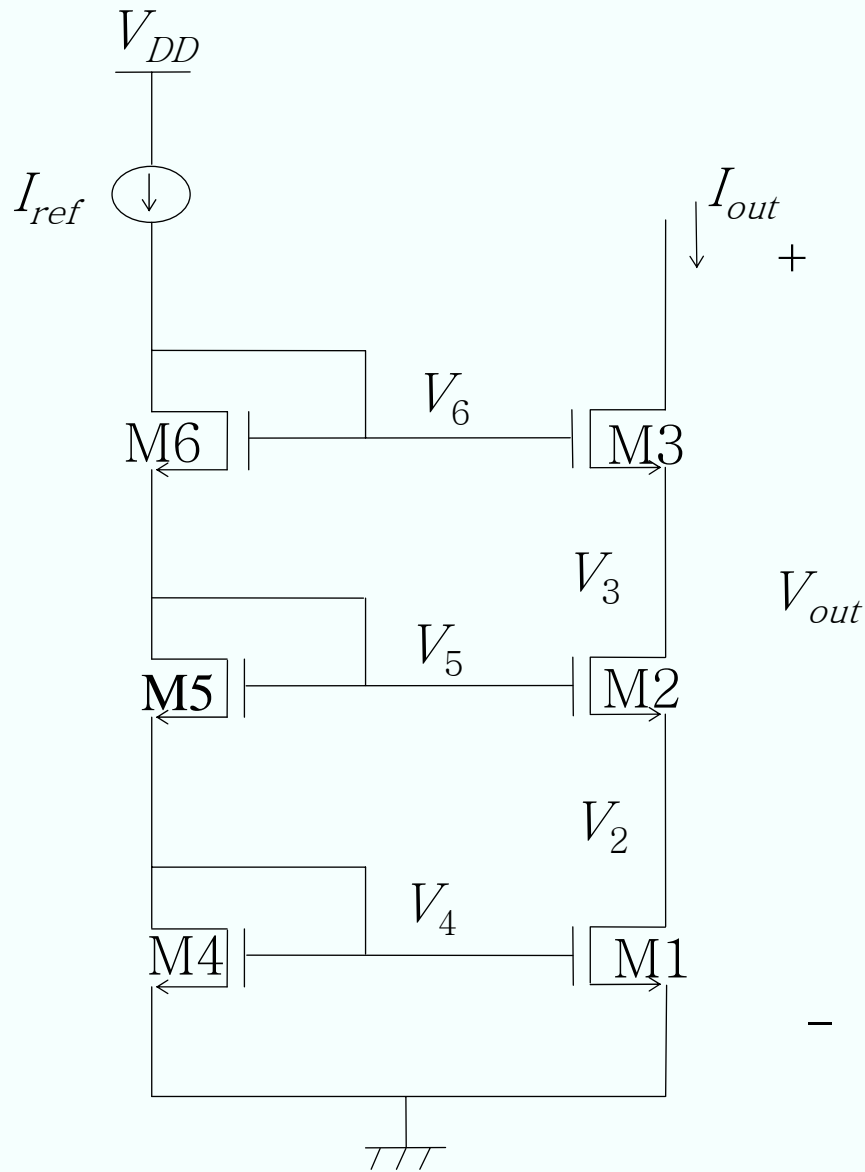
$$V_{DS2} = V_{GS6} + V_{GS5} + V_{GS4} - V_{GS3} - V_{DS1} = V_{GS5} = V_{GS2} > (V_{GS2} - V_{TH2})$$

M2 : saturation

$$V_{out} \geq V_6 - V_{TH3}$$

M3 : saturation

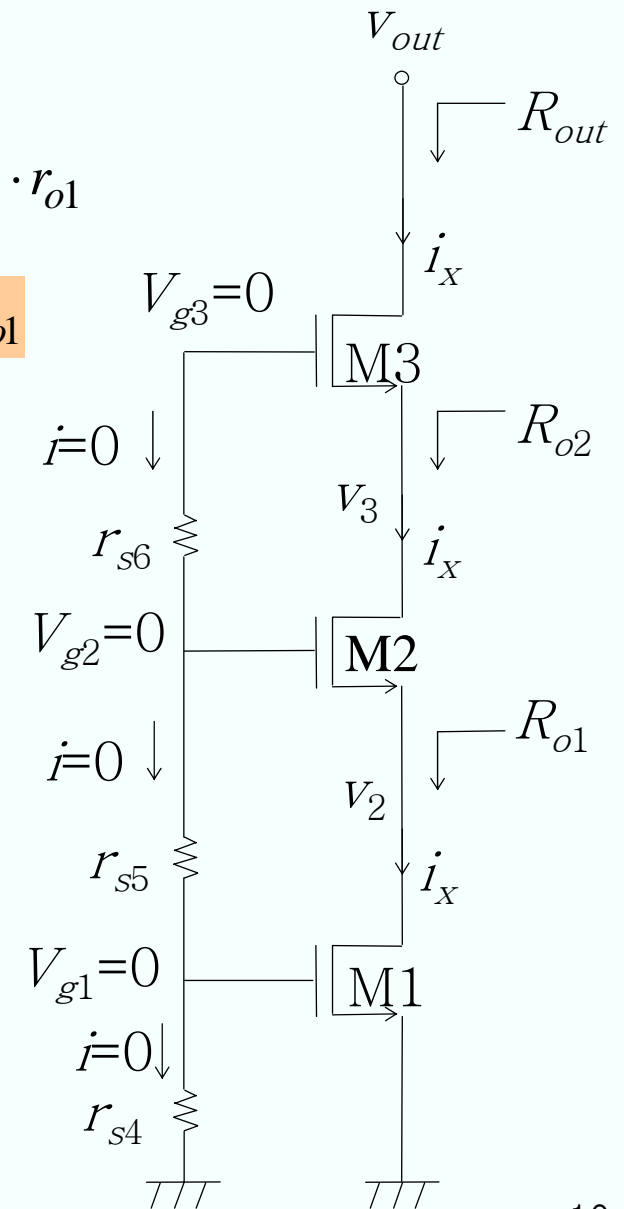
$$V_{out} \geq V_{DSAT3} + V_{DSAT2} + V_{DSAT1} + V_{TH2} + V_{TH1}$$



$$R_{o1} = r_{o1}$$

$$R_{o2} = g_{m2}r_{o2} \cdot R_{o1} + R_{o1} + r_{o2} \approx g_{m2}r_{o2} \cdot R_{o1} = g_{m2}r_{o2} \cdot r_{o1}$$

$$R_{out} = g_{m3}r_{o3} \cdot R_{o2} + R_{o2} + r_{o3} \approx g_{m3}r_{o3} \cdot R_{o2} = g_{m3}r_{o3} \cdot g_{m2}r_{o2} \cdot r_{o1}$$



$$v_{out} = i_x \cdot R_{out}$$

$$v_3 = i_x \cdot R_{o2}$$

$$v_2 = i_x \cdot R_{o1}$$

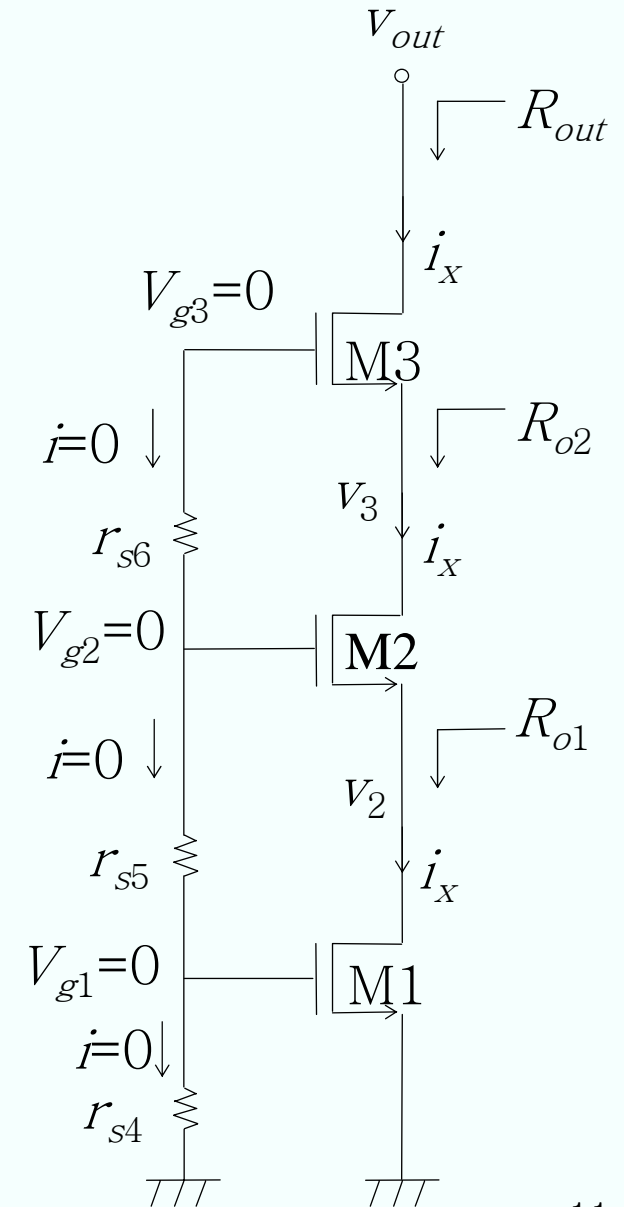
$$v_3 \approx \frac{v_{out}}{R_{out} / R_{o2}} = \frac{v_{out}}{g_{m3}r_{o3}}$$

Small,
Cascode effect

$$v_2 \approx \frac{v_3}{R_{o2} / R_{o1}} = \frac{v_{out}}{g_{m3}r_{o3} \cdot g_{m2}r_{o2}}$$

Very small,
Cascode effect

V_3, V_2 : almost DC voltage independent of v_{out}



I_{ref}, M_{b0}, M_{a0} decide V_{GS}, V_{DS} of $M_{a1}, M_{a2}, M_{a3}, M_{an}$
 $\rightarrow V_{GS}$ of M_{b1}, M_{b2}, M_{bn} $\rightarrow I_{out}$ almost constant

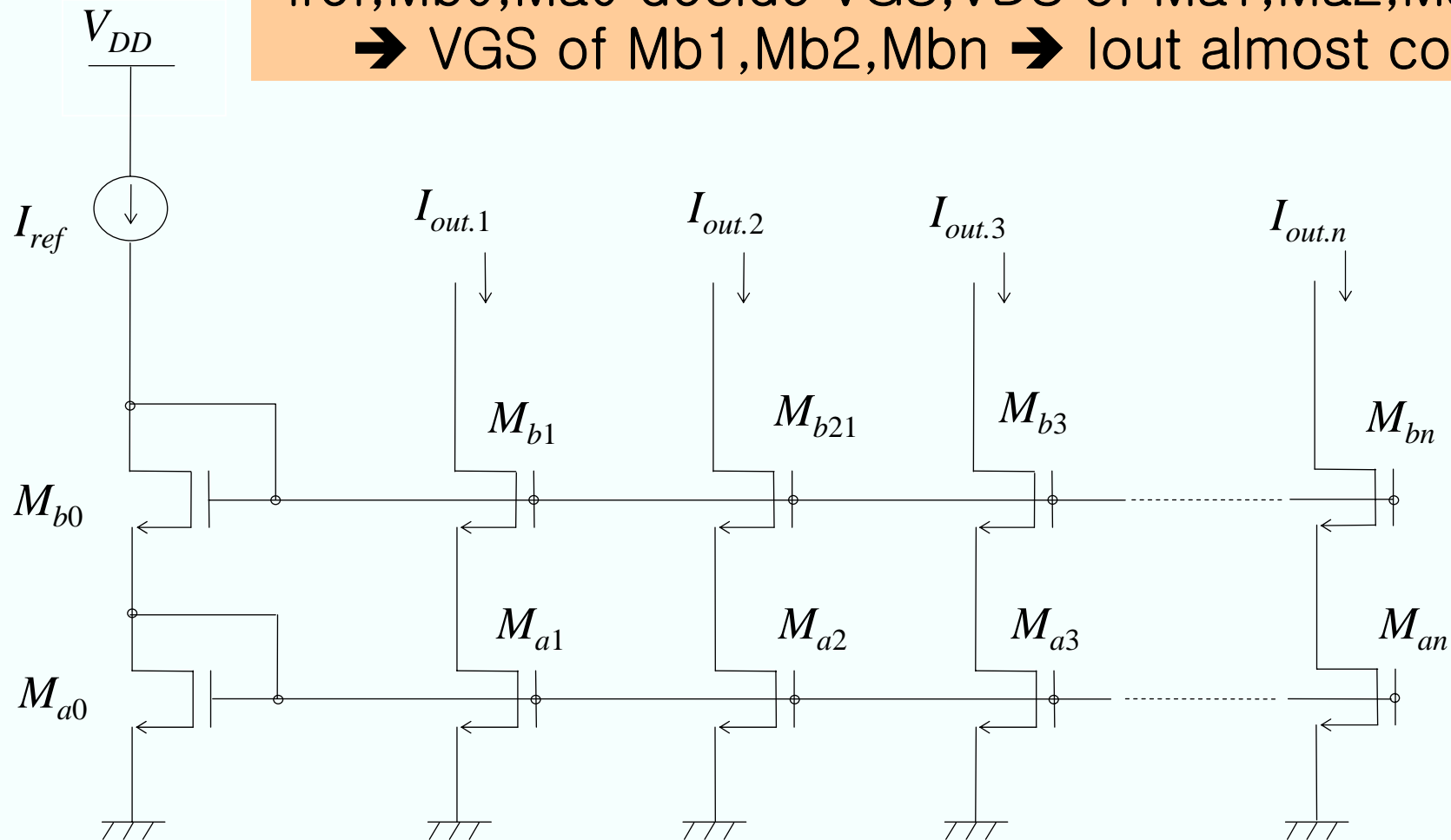
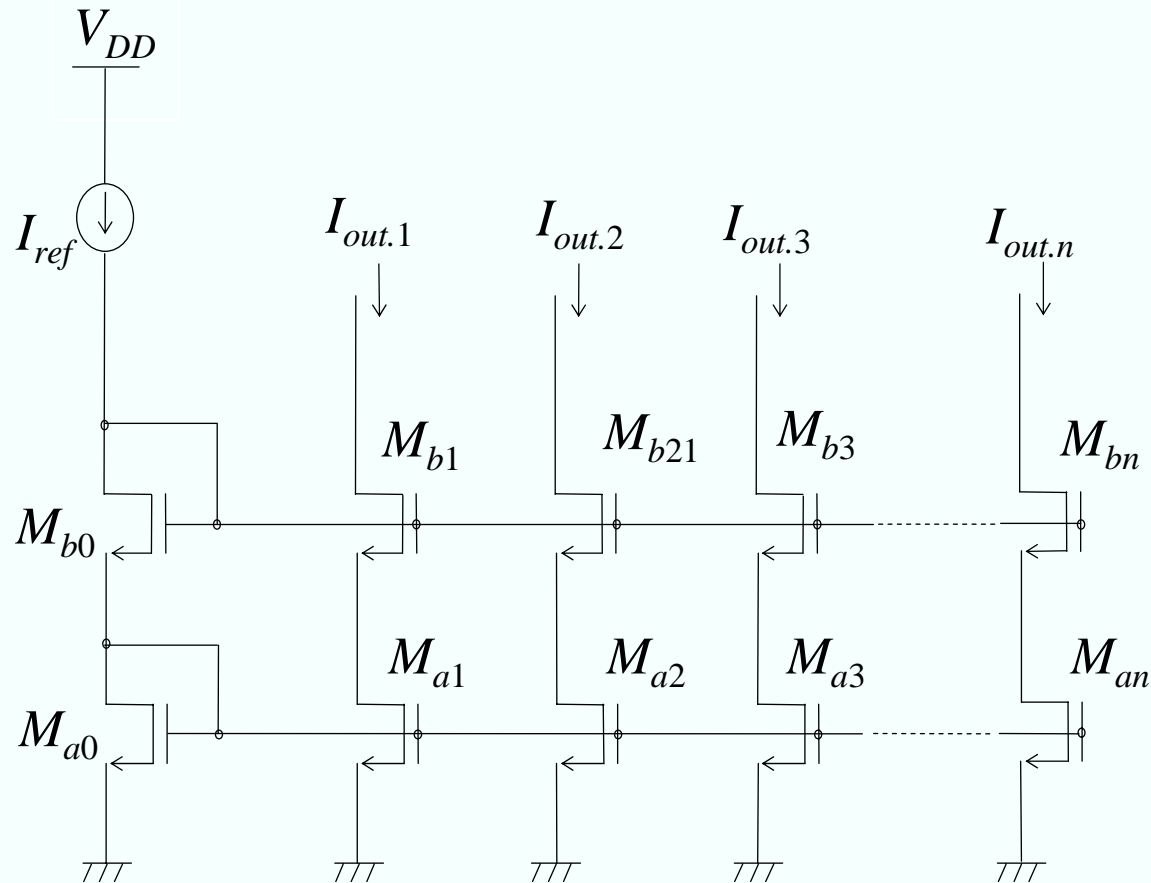


Fig8.1.4 Multi-output cascode current source



$$I_{out.1} = I_{ref} \cdot \frac{(W/L)_{Ma1}}{(W/L)_{Ma0}}$$

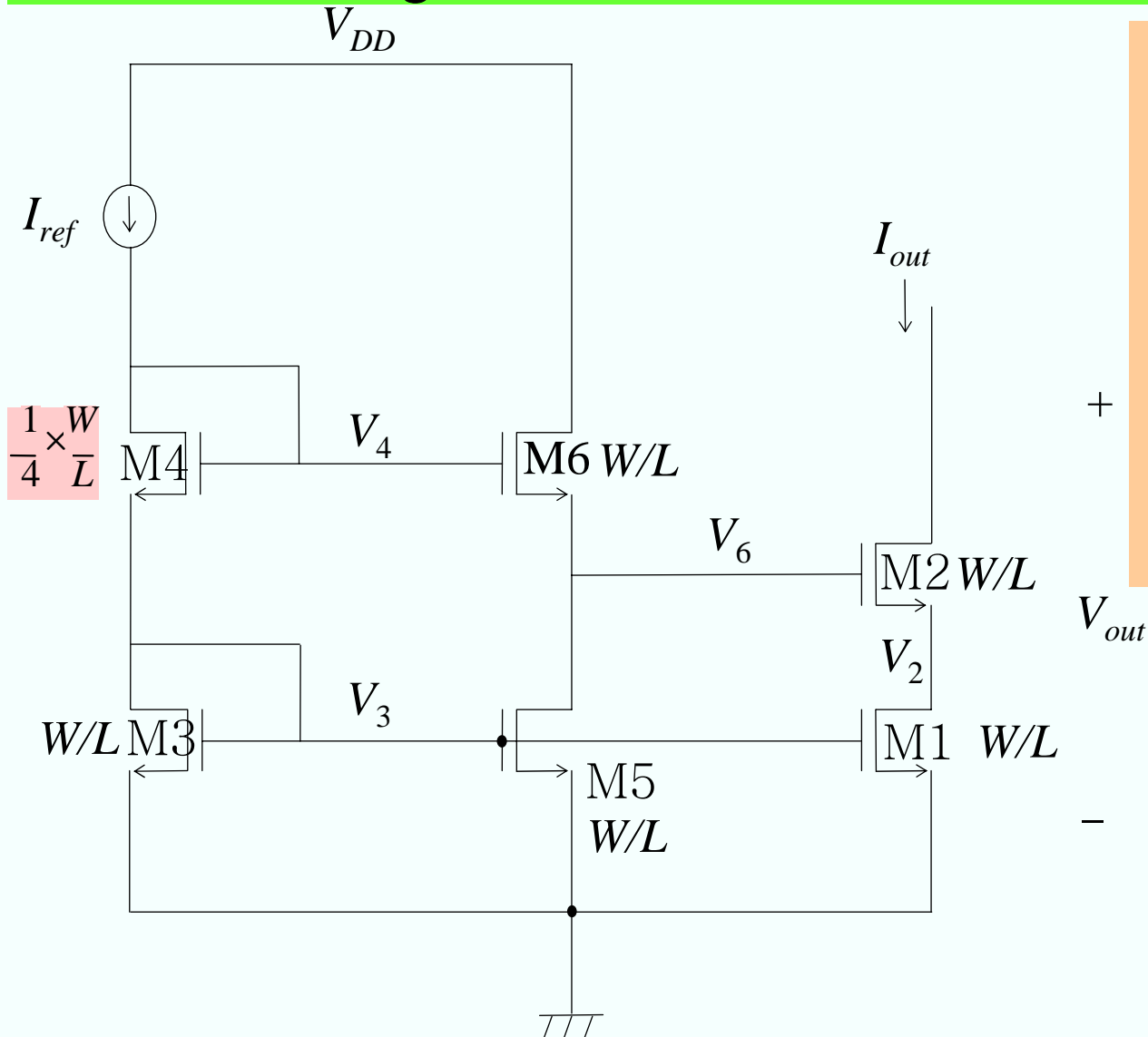
$$I_{out.2} = I_{ref} \cdot \frac{(W/L)_{Ma2}}{(W/L)_{Ma0}}$$

$$I_{out.3} = I_{ref} \cdot \frac{(W/L)_{Ma3}}{(W/L)_{Ma0}}$$

⋮

$$I_{out.n} = I_{ref} \cdot \frac{(W/L)_{Man}}{(W/L)_{Ma0}}$$

Wide-swing cascode current source: circuit 1



$I_{ref}, M3, M4$

→ V_3, V_4

→ VGS of M5

→ VGS of M6, VDS of M5

→ V_6

+ → VGS of M2, VDS of M1

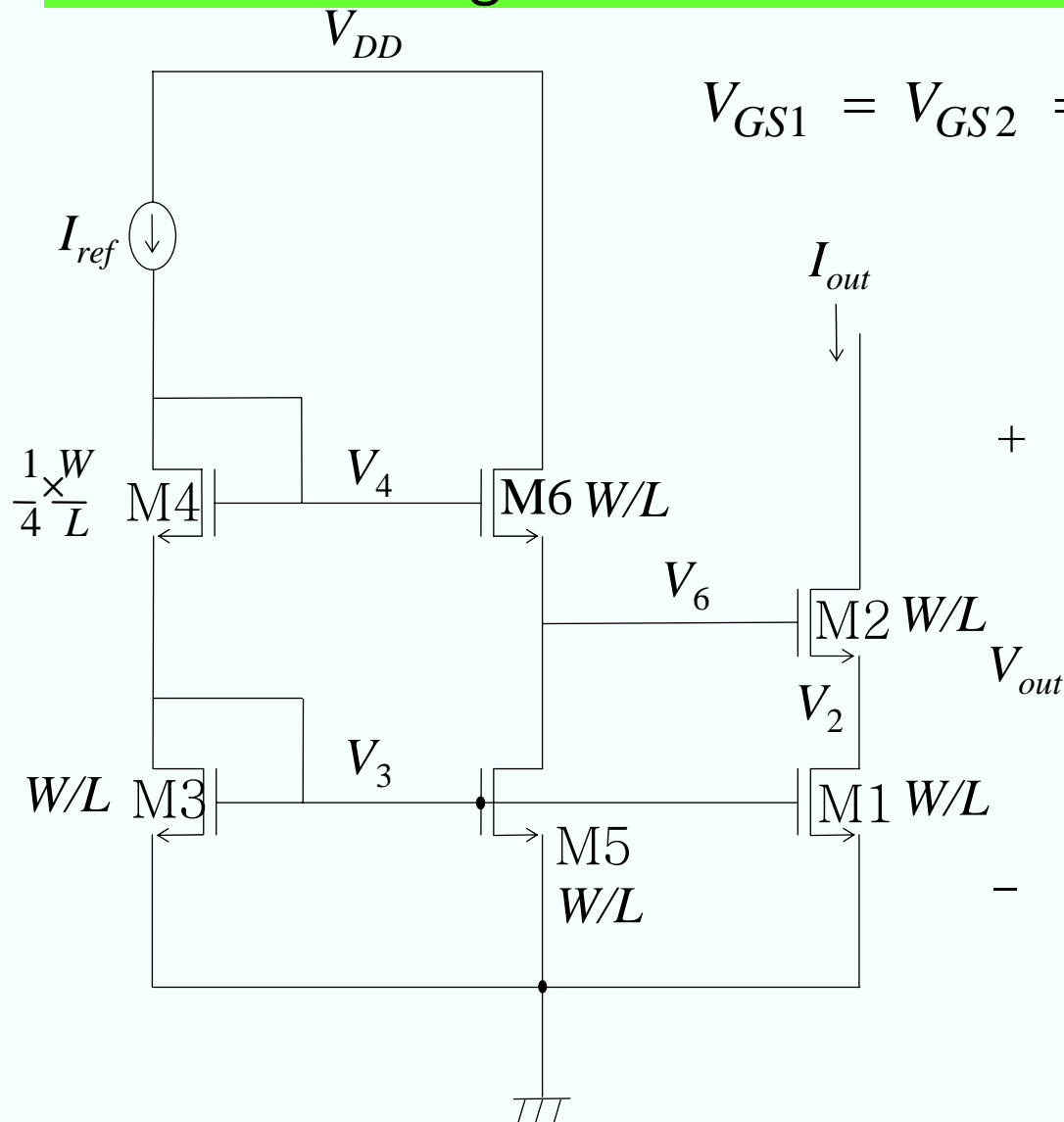
→ VGS, VDS of M1: $\sim = DC$

→ I_{out} constant

V_{out}

-

Wide-swing cascode current source: circuit 1



$$V_{GS1} = V_{GS2} = V_{GS3} = V_{GS5} = V_{GS6} = V_{TH} + \Delta$$

$$V_{GS4} = V_{TH} + 2\Delta$$

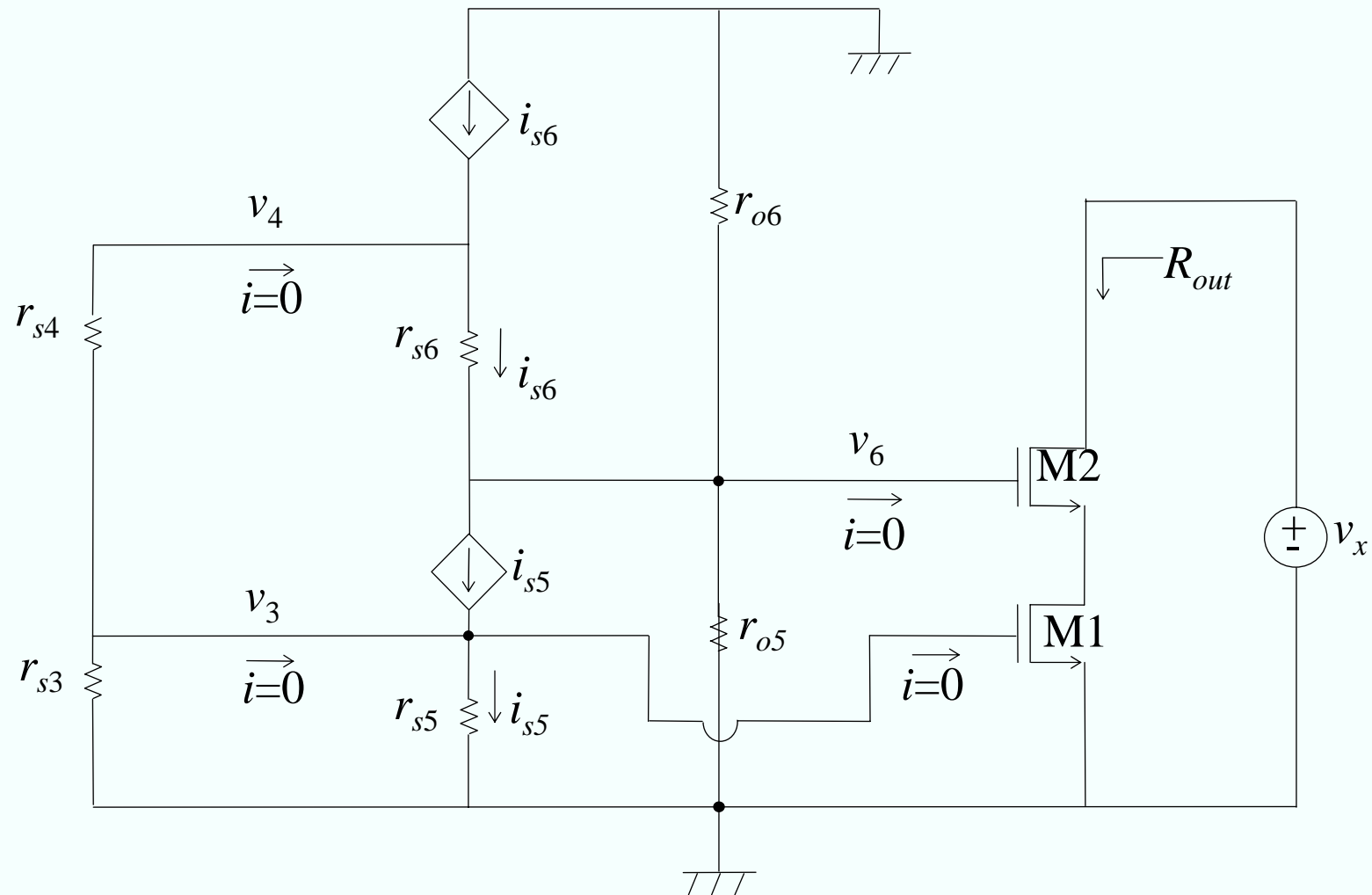
$$+ \quad V_3 = V_{GS3} = V_{TH} + \Delta$$

$$V_4 = V_{GS4} + V_3 = 2V_{TH} + 3\Delta$$

$$V_6 = V_4 - V_{GS6} = V_{TH} + 2\Delta$$

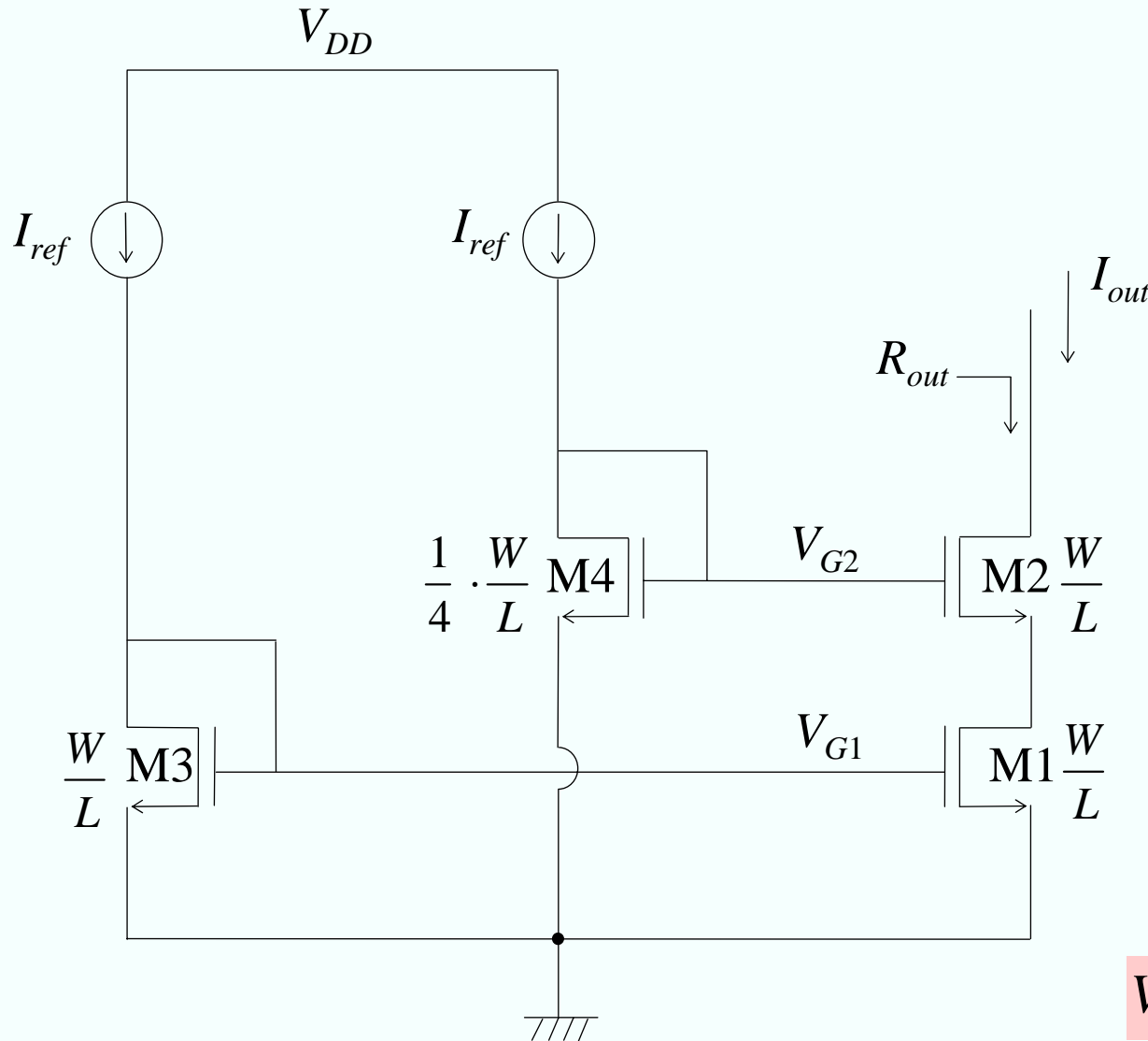
$$- \quad V_2 = V_6 - V_{GS2} = \Delta$$

$$V_{out} \geq V_6 - V_{TH} = 2\Delta$$



$$R_{out} = g_{m2}r_{o2} \cdot r_{o1} + r_{o1} + r_{o2} \approx g_{m2}r_{o2} \cdot r_{o1}$$

Wide-swing cascode current source: circuit 2



$I_{ref,M3}, I_{ref,M4}$

→ V_{G1}, V_{G2}

→ V_{GS} of $M1$

→ V_{GS} of $M2$, V_{DS} of $M1$

→ I_{out} almost constant

+

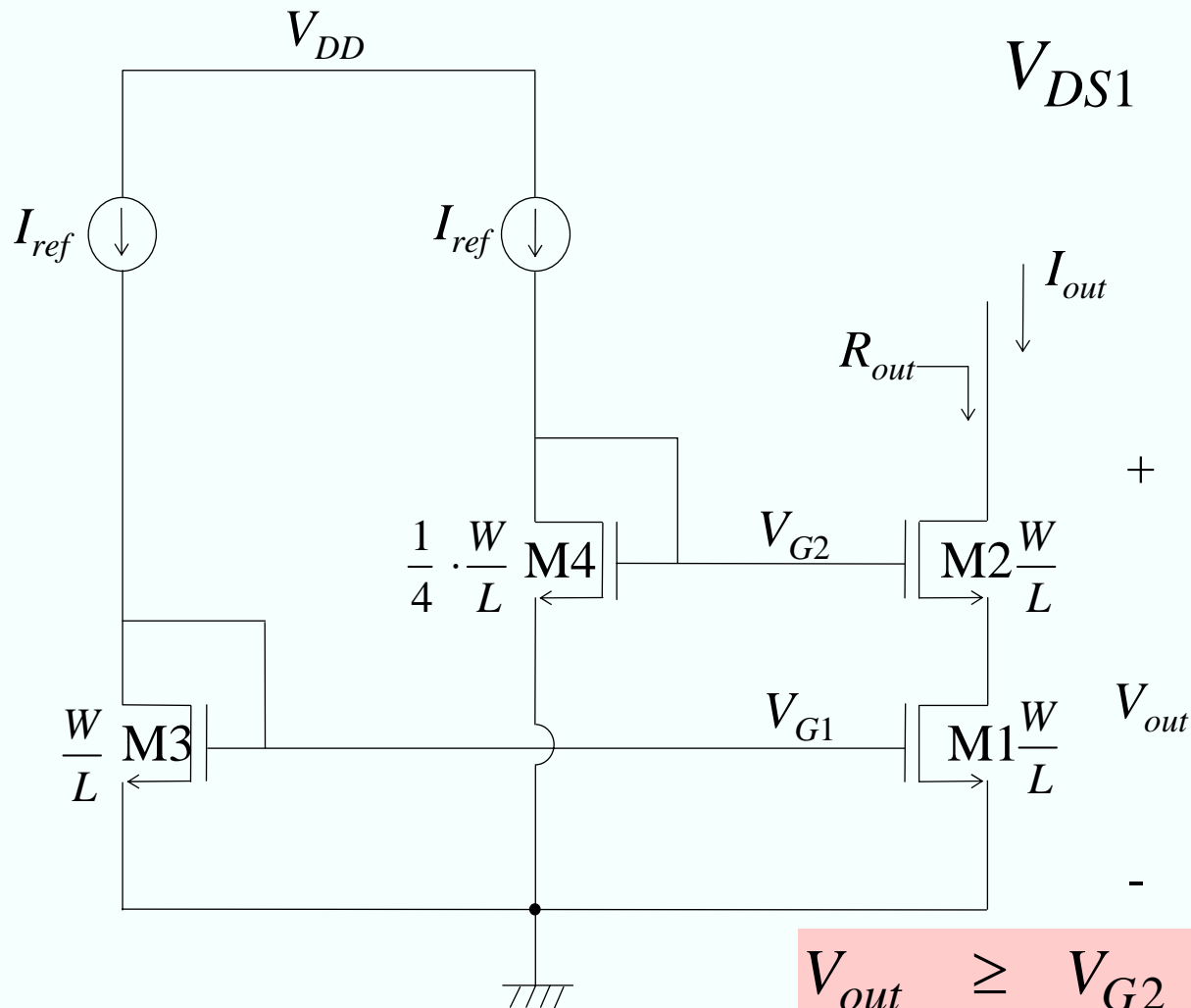
$$V_{DS1} = V_{G2} - V_{GS2}$$

$$V_{out} = (V_{TH} + 2\Delta) - (V_{TH} + \Delta)$$

$$= \Delta$$

-

$$V_{out} \geq V_{G2} - V_{TH} = 2\Delta$$

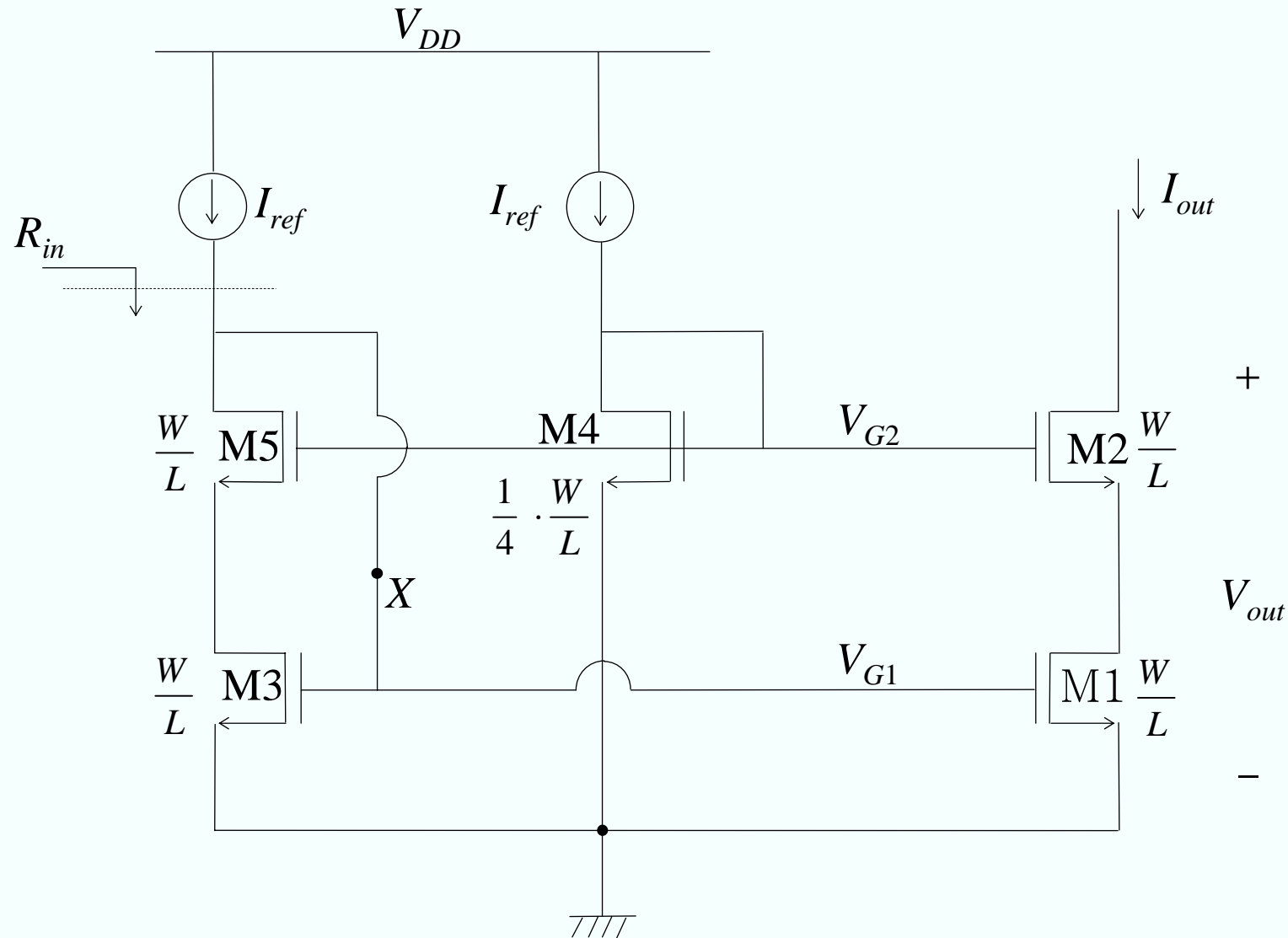


$$V_{G2} = V_{TH} + 2\Delta + V_{margin}$$

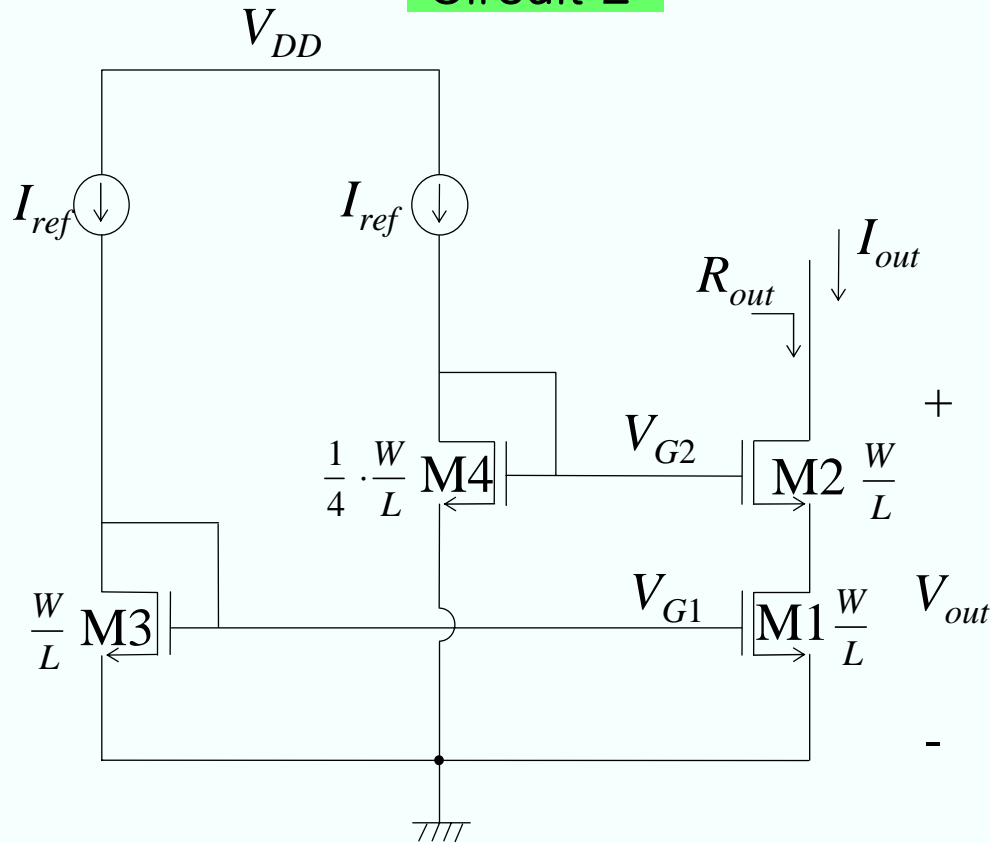
$$\begin{aligned} V_{DS1} &= V_{G2} - V_{GS2} \\ &= (V_{TH} + 2\Delta + V_{margin}) - (V_{TH} + \Delta) \\ &= \Delta + V_{margin} \end{aligned}$$

$$V_{out} \geq V_{G2} - V_{TH} = 2\Delta + V_{margin}$$

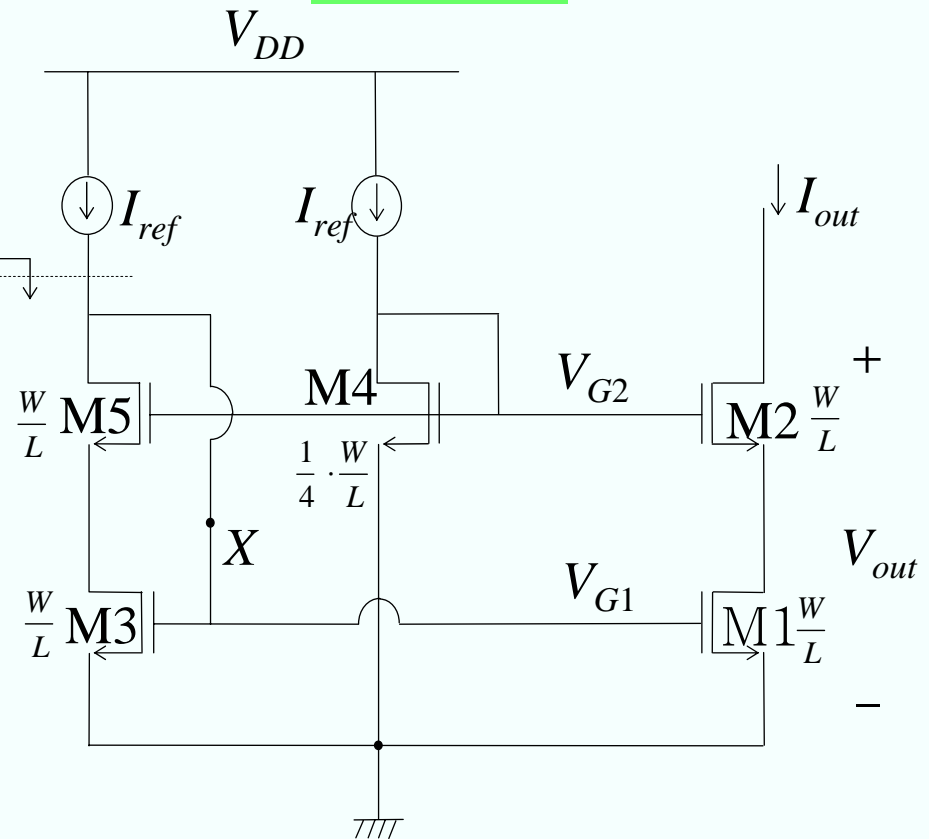
Wide-swing cascode current source: circuit 3



Circuit 2



Circuit 3



$$V_{DS1} = \Delta$$

$$V_{DS3} = \Delta + V_{TH}$$

$$I_{out} < I_{ref}$$

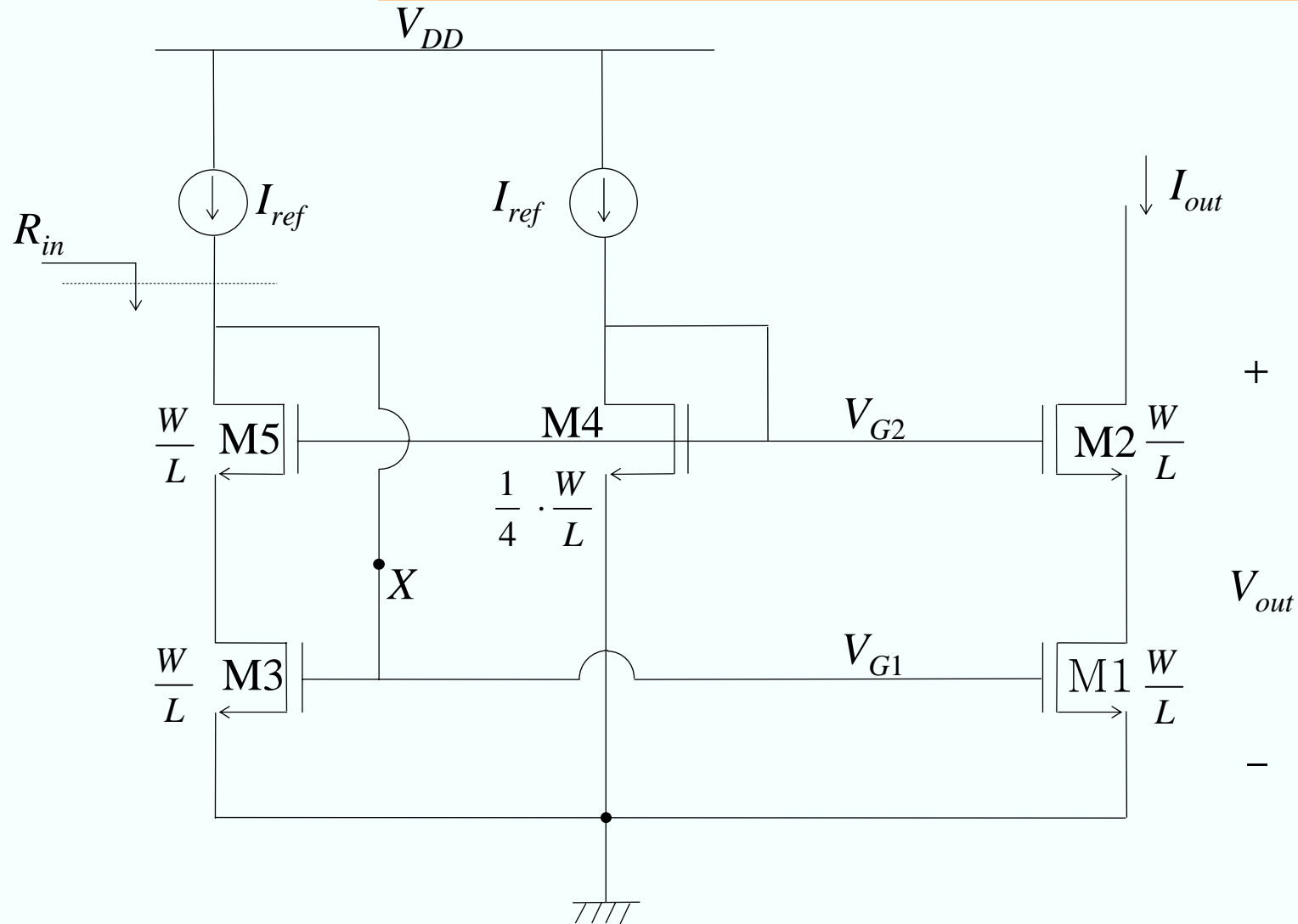
Current gain < 1
Active load application

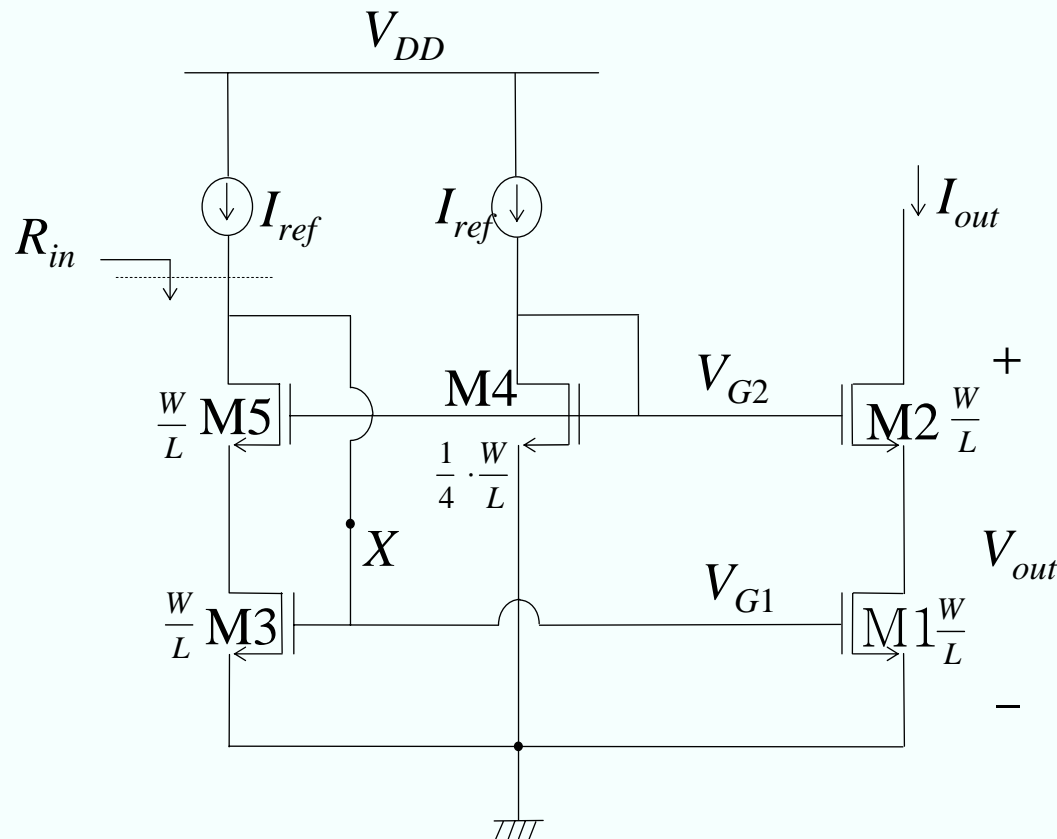
$$V_{DS1} = V_{DS3} = \Delta$$

$$I_{out} = I_{ref}$$

Current gain = 1

$I_{ref}, M4, I_{ref}, M5, M3 \rightarrow V_{G1}, V_{G2} \rightarrow V_{GS2}, V_{DS1} \rightarrow$
 $V_{GS1}, V_{DS1}: \text{constant} \rightarrow I_{out} \text{ almost constant}$





$$V_{G2} = 2\Delta + V_{TH}$$

$$V_{G1} = \Delta + V_{TH}$$

$$V_{GS5} = \Delta + V_{TH}$$

$$V_{GS2} = \Delta + V_{TH}$$

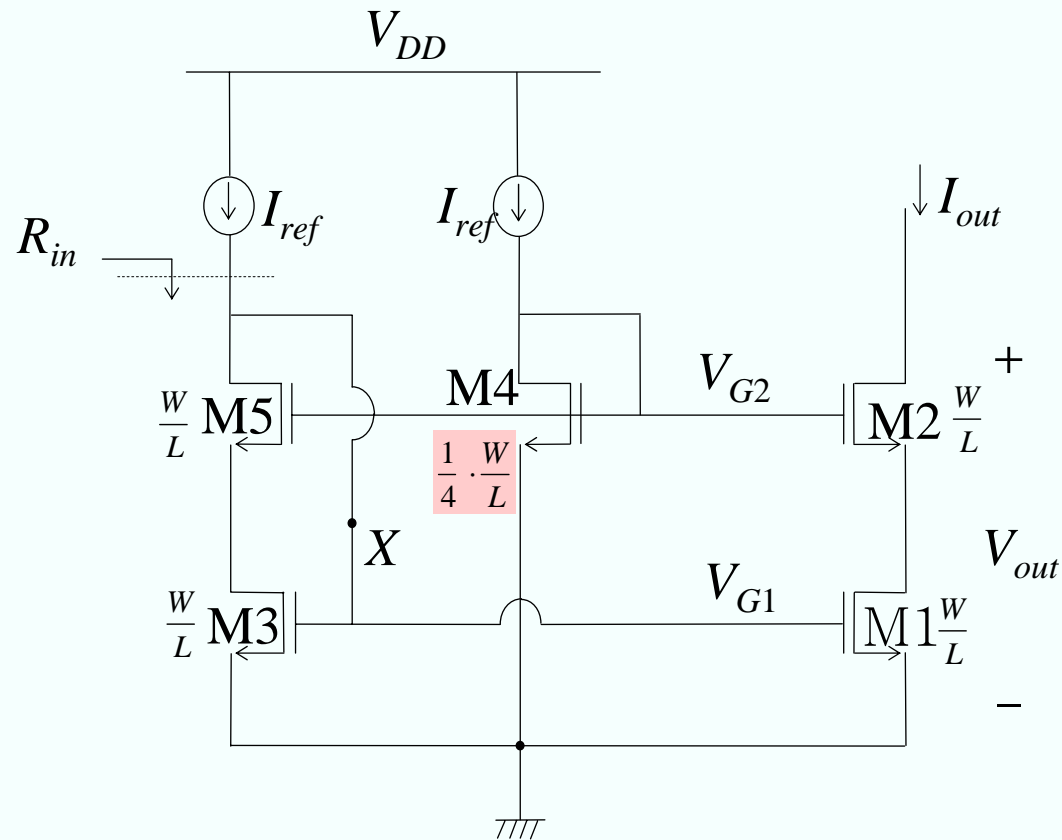
$$V_{DS3} = V_{G2} - V_{GS5} = \Delta$$

$$V_{DS5} = V_{G1} - V_{DS3} = V_{TH}$$

$$V_{DS1} = V_{G2} - V_{GS2} = \Delta$$

$$I_{out} = I_{ref}$$

Current gain = 1

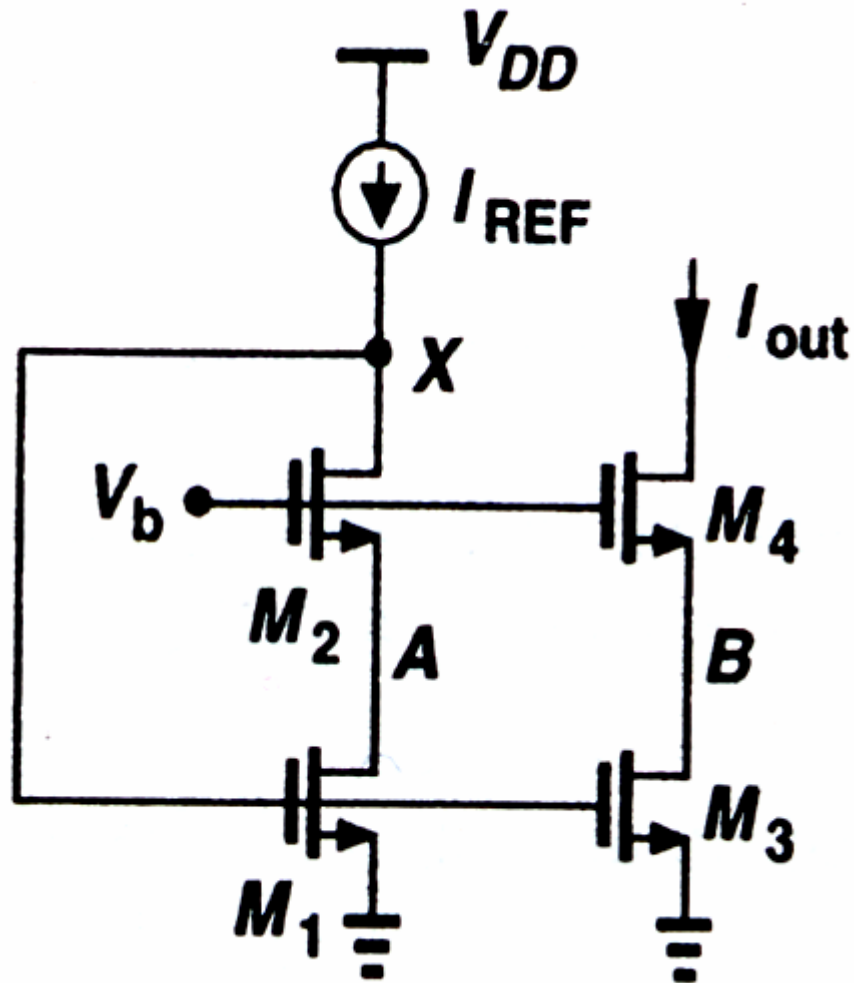


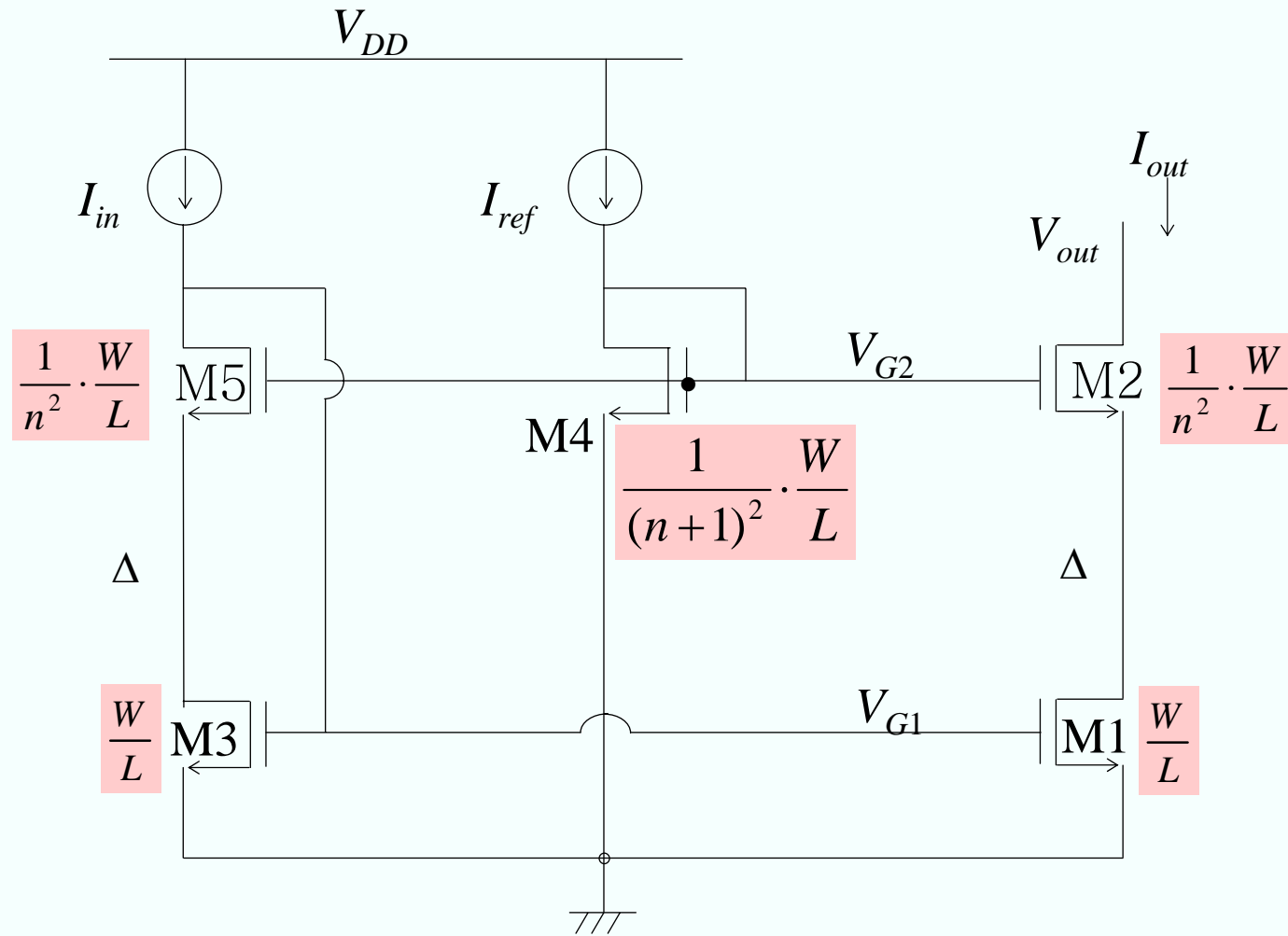
Negative feedback at M3, M5 (shunt)

$$V_{out} \geq V_{G2} - V_{TH} = 2\Delta$$

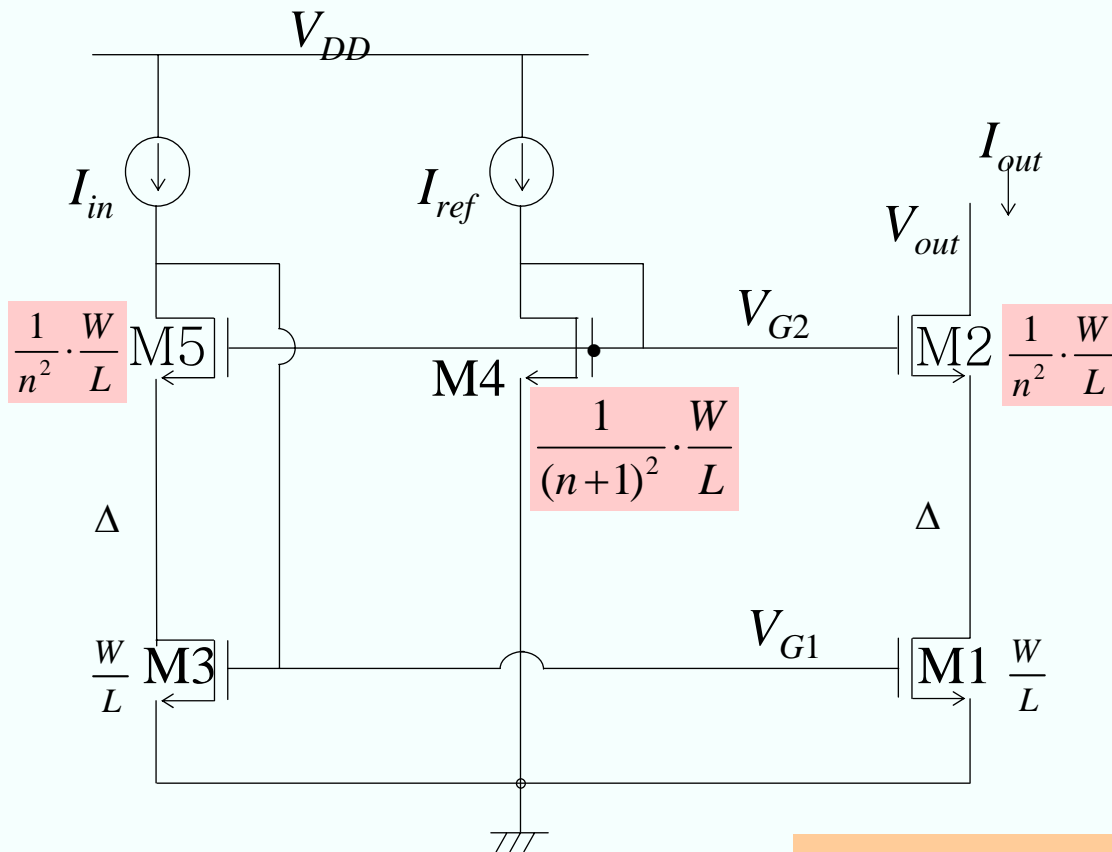
$$R_{in} = \frac{R_i}{(1 + \text{loop gain})} \approx \frac{1}{g_{m3}}$$

$$R_{out} = g_{m2}r_{o2} \cdot r_{o1} + r_{o1} + r_{o2} \approx g_{m2}r_{o2} \cdot r_{o1}$$





$$V_{out} \geq V_{G2} - V_{TH} = (n+1) \cdot \Delta \cdot \sqrt{\frac{I_{ref}}{I_{in}}}$$



$$V_{G1} = V_{TH} + \Delta$$

$$V_{GS5} = V_{TH} + n \cdot \Delta$$

$$V_{GS2} = V_{TH} + n \cdot \Delta$$

$$V_{G2} = V_{TH} + (n+1) \cdot \Delta \cdot \sqrt{\frac{I_{ref}}{I_{in}}}$$

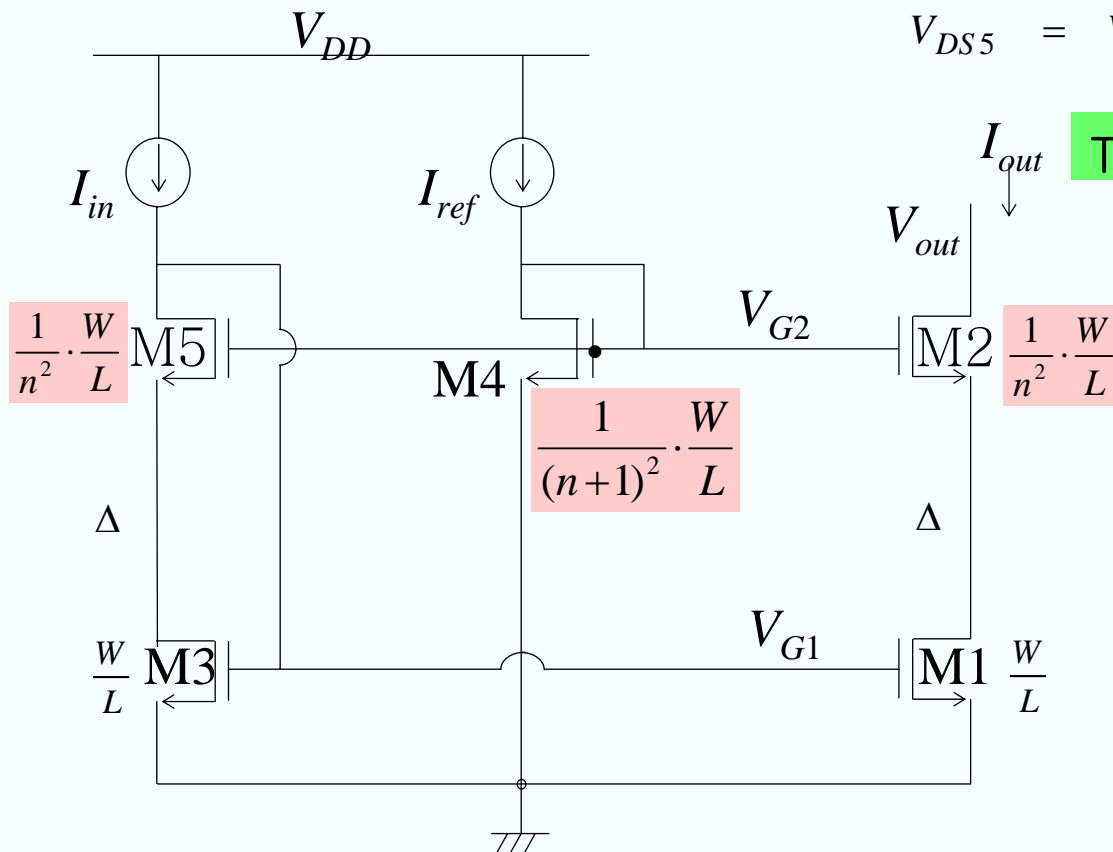
$$V_{DS3} = V_{G2} - V_{GS5} = \Delta \cdot \sqrt{\frac{I_{ref}}{I_{in}}} + n \cdot \Delta \cdot \left(\sqrt{\frac{I_{ref}}{I_{in}}} - 1 \right)$$

$$V_{DS1} = V_{G2} - V_{GS2} = \Delta \cdot \sqrt{\frac{I_{ref}}{I_{in}}} + n \cdot \Delta \cdot \left(\sqrt{\frac{I_{ref}}{I_{in}}} - 1 \right)$$

$$V_{DS3} = V_{G2} - V_{GS5} = \Delta \cdot \sqrt{\frac{I_{ref}}{I_{in}}} + n \cdot \Delta \cdot \left(\sqrt{\frac{I_{ref}}{I_{in}}} - 1 \right)$$

$$V_{DS1} = V_{G2} - V_{GS2} = \Delta \cdot \sqrt{\frac{I_{ref}}{I_{in}}} + n \cdot \Delta \cdot \left(\sqrt{\frac{I_{ref}}{I_{in}}} - 1 \right)$$

$$V_{DS5} = V_{G1} - V_{DS3} = V_{TH} - (n+1) \cdot \Delta \cdot \left(\sqrt{\frac{I_{ref}}{I_{in}}} - 1 \right)$$



To satisfy the following three conditions

$$V_{DS3} \geq \Delta$$

$$V_{DS5} \geq n \cdot \Delta$$

$$V_{DS1} \geq \Delta$$



$$I_{in} \leq I_{ref}$$

$$n \leq \frac{V_{TH} + \Delta}{\Delta} \cdot \sqrt{\frac{I_{in}}{I_{ref}}} - 1$$