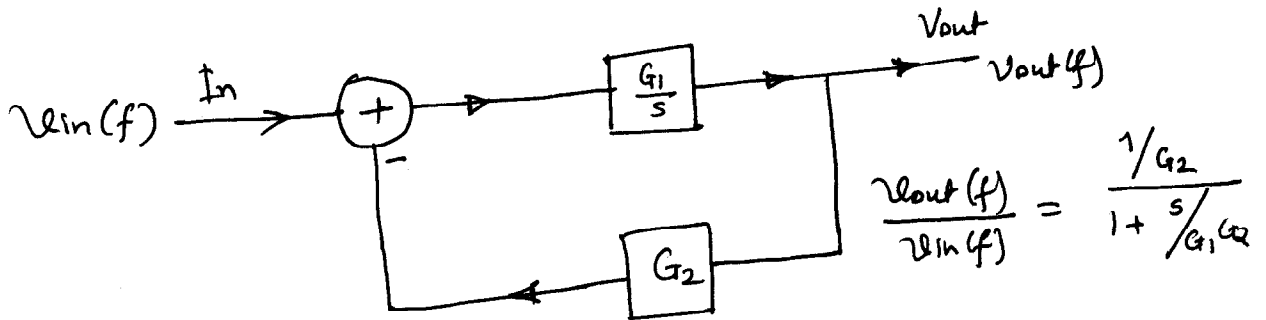


Solution of 35.12 by Pandurang K. Irkar

Prob 35.12 show the derivation details that result in equations (35.44) and (35.46)

Soln: The general implementation of a lowpass first order filter.



The schematic diagram of a Discrete Analog Integrator (DAI)

→ ^{Basically} ^(Ref. 21.78) To begin with the output of the DAI is connected to the OPAMP through ϕ_1 switch. When the ϕ_1 switches are closed (ϕ_1 is high) at $n-1 \rightarrow$ switches shut off, the charge stored on C_I is

$$Q_1 = C_I (V_{cm} - V_1 [(n-1)T_s]) \quad \text{--- } \phi$$

When ϕ_2 switches turn on the charge stored on C_I becomes

$$Q_2 = C_I (V_{cm} - V_2 [(n-1/2)T_s]) \quad \text{--- } \textcircled{2}$$

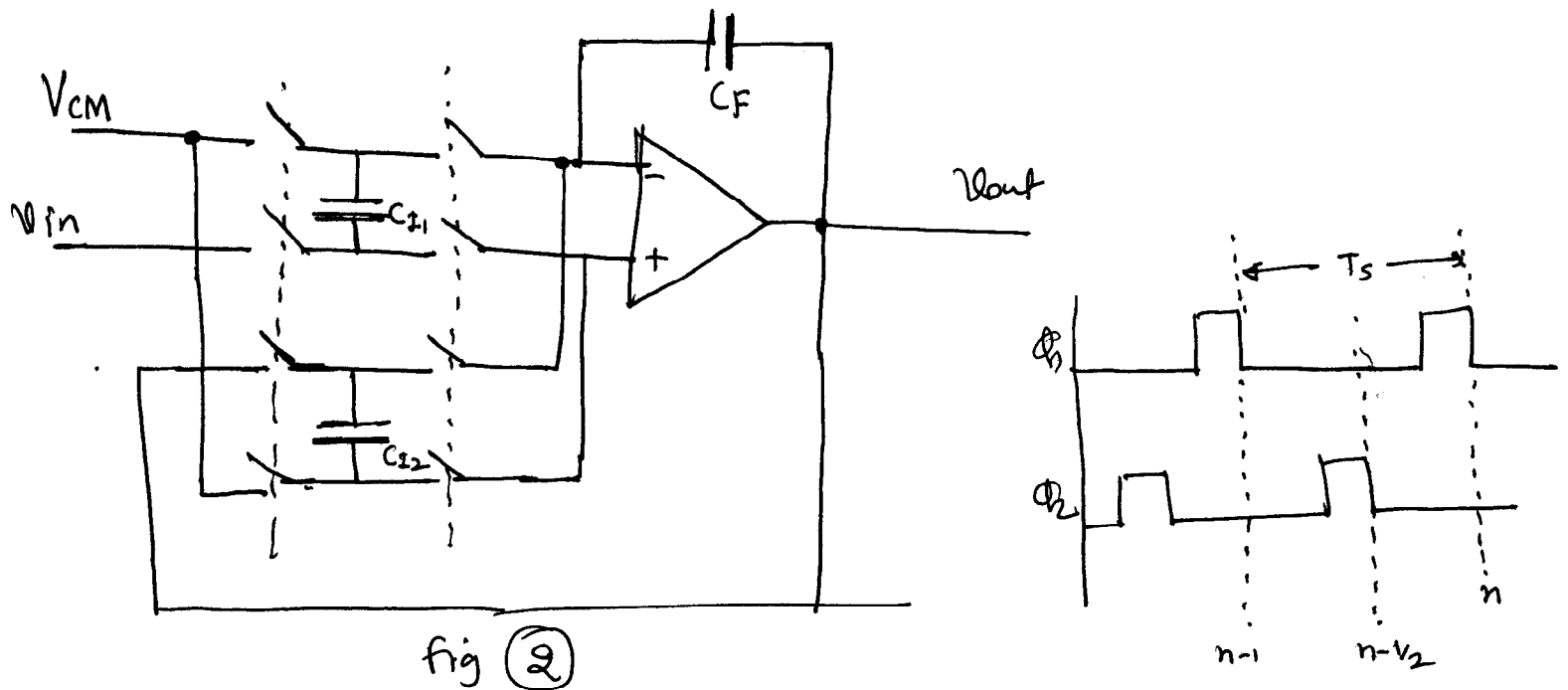
The difference in these charges, $Q_2 - Q_1 \rightarrow$ Resulting in output voltage change. This change can be written as

$$(V_{out} [nT_s] - V_{out} [(n-1)T_s]) C_F = C_I (V_1 [(n-1)T_s] - V_2 [(n-1/2)T_s]) \quad \text{--- } \textcircled{3}$$

Writing in Z-domain results in

$$V_{out}(z) (1 - z^{-1}) = \frac{C_I}{C_F} (V_1(z) - z^{-1} - V_2(z) z^{-1/2}) \quad \text{--- } \textcircled{4}$$

Depending upon the output connected to ϕ_1 or ϕ_2 ; we have different topologies. and one of them is as shown in following fig.



Similarly as above procedure we can write the equation for the above fig. 2. topology

Begin with ϕ_1 and at $n-1$ shutting off, we can write charges

$$Q_1 = C_{I1} (V_{cm} - V_{in} [(n + \frac{1}{2}) T_s]) \quad \text{--- (1)}$$

with C_{I2}

$$Q_2 = C_{I2} (V_{out} [(n + \frac{1}{2}) T_s] - V_{cm}) \quad \text{--- (2)}$$

The output charge across the feedback capacitor is

$$V_{out} [(n T_s)] - V_{out} [(n-1) T_s] C_F = C_{I1} (V_{cm} - V_{in} [(n + \frac{1}{2}) T_s]) - C_{I2} (V_{out} [(n + \frac{1}{2}) T_s] - V_{cm})$$

writing into z domain

$$V_{out}(z) = \frac{z^{-1}}{1 - z^{-1}}$$

$$V_{out}(z) (1-z^{-1})C_F = C_{I1} (V_{in}(z)) - C_{I2} (V_{out}(z))$$

$$V_{out}(z) = \frac{z^{-1}}{1-z^{-1}} \cdot \left[\frac{C_{I1}}{C_F} \cdot V_{in}(z) \cdot z^{1/2} - \frac{C_{I2}}{C_F} \cdot V_{out}(z) \right]$$

With this equation we can write for general block diagram

$$G_1 = \frac{C_{I1}}{C_F} \cdot f_s \quad \text{and} \quad G_2 = \frac{C_{I2}}{C_F} \cdot f_s \cdot \frac{1}{G_1} = \frac{C_{I2}}{C_{I1}}$$

$$f_{3dB} = \frac{G_1 G_2}{2\pi}$$
