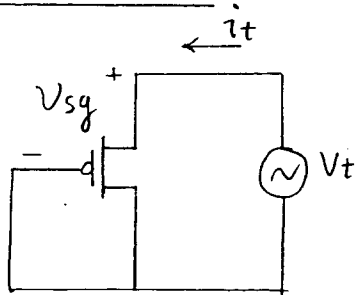


## Chapter 22.

### Problem 22.1

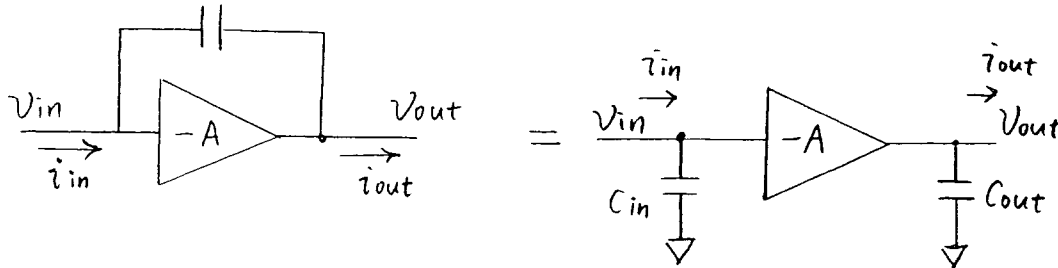


$$R_{eq} = \frac{V_t}{i_t} = \frac{V_{sg}}{g_m V_{sg}} = \frac{1}{g_m}$$

### Problem 22.2

See next page.

### Problem 22.3



$$i_{in} = \frac{V_{in} - V_{out}}{\frac{1}{j\omega C}} = [V_{in} - (-A)V_{in}]j\omega C = V_{in}(1+A)j\omega C$$

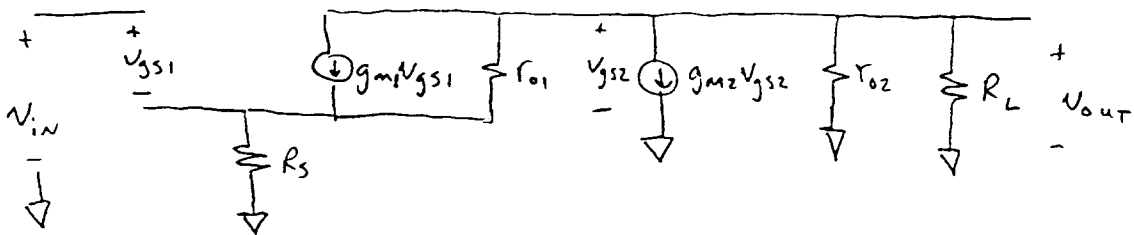
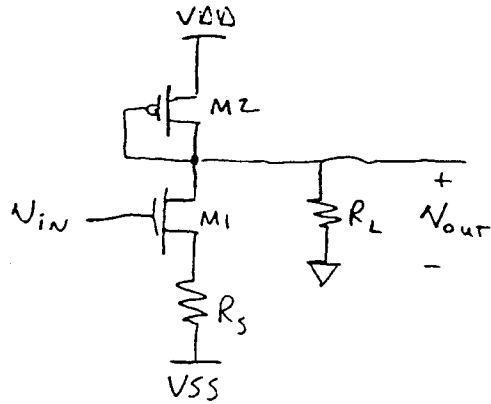
$$\frac{V_{in}}{i_{in}} = \frac{V_{in}}{V_{in}(1+A)j\omega C} = \frac{1}{j\omega(1+A)C} = \frac{1}{j\omega C_{in}} \Rightarrow \underline{\underline{C_{in} = (1+A)C}}$$

$$i_{out} = \frac{V_{in} - V_{out}}{\frac{1}{j\omega C}} = \left(-\frac{1}{A}V_{out} - V_{out}\right)j\omega C = -\left(1 + \frac{1}{A}\right)V_{out}j\omega C$$

$$\frac{V_{out}}{-i_{out}} = \frac{V_{out}}{V_{out}\left(1 + \frac{1}{A}\right)j\omega C} = \frac{1}{j\omega\left(1 + \frac{1}{A}\right)C} = \frac{1}{j\omega C_{out}} \Rightarrow \underline{\underline{C_{out} = \left(1 + \frac{1}{A}\right)C}}$$

## 22.2

Using small signal models, verify that the gain given in Ex. 22.1 is correct.



Assume  $\frac{1}{g_{m2}} \ll r_{o1} + r_{o2}$

$$V_o = -g_{m1} V_{gs1} \left( \frac{1}{g_{m2}} \parallel R_L \right)$$

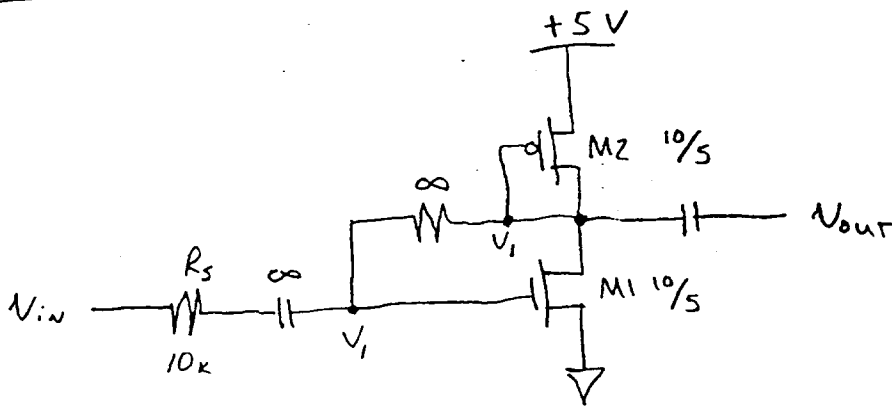
$$V_{in} = V_{gs1} + g_{m1} V_{gs1} (R_S)$$

$$\frac{V_o}{V_{in}} = \frac{V_o}{V_{gs1}} \cdot \frac{V_{gs1}}{V_{in}} = \left( -g_{m1} \left( \frac{1}{g_{m2}} \parallel R_L \right) \right) \left( \frac{1}{1 + g_{m1} R_S} \right)$$

$$\frac{V_o}{V_{in}} = \frac{- \left( \frac{1}{g_{m2}} \parallel R_L \right)}{\frac{1}{g_{m1}} + R_S}$$

checks!

22.4



(a) Determine DC voltages & currents:

$$I_{D1} = I_{D2}$$

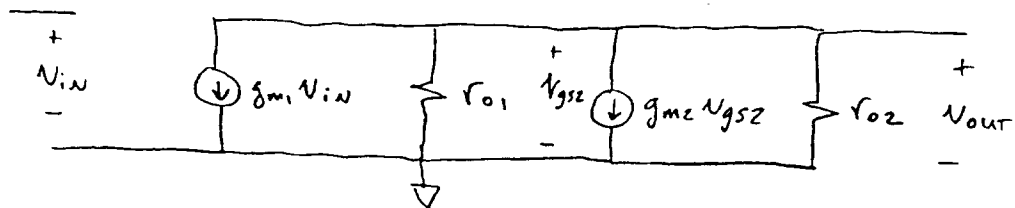
$$\frac{50 \mu\text{A}/\text{V}^2}{2} \frac{10}{5} (V_1 - 0.83)^2 = \frac{17 \mu\text{A}/\text{V}^2}{2} \frac{10}{5} (5 - V_1 - 0.91)^2$$

$$1.941 V_1^2 + 3.2979 V_1 - 14.7019 = 0$$

$$V_1 = \underline{\underline{2.031 \text{ V}}}$$

$$I_{D1} = I_{D2} = 50 \mu\text{A}/\text{V}^2 (2.031 - 0.83)^2 = \underline{\underline{72.12 \mu\text{A}}}$$

(b) Determine the small signal low frequency gain:



$$\frac{V_{out}}{V_{in}} = -g_{m1} \left( \frac{1}{g_{m2}} \parallel r_{o1} \parallel r_{o2} \right)$$

$$g_{m1} = \sqrt{2(50 \mu\text{A}) \left(\frac{10}{5}\right) (72.12 \mu\text{A})} = 120 \mu\text{A}/\text{V}$$

$$g_{m2} = \sqrt{2(17 \mu\text{A}) \left(\frac{10}{5}\right) (72.12 \mu\text{A})} = 70 \mu\text{A}/\text{V}$$

$$r_{o1} = r_{o2} = \frac{1}{\lambda I_0} = \frac{1}{0.06(72.12 \mu\text{A})} = 231.1 \text{ k}\Omega$$

$$\frac{V_{out}}{V_{in}} = -1.53 \frac{\text{V}}{\text{V}}$$

c) Determine  $C_{sg2}$ ,  $C_{db2}$ ,  $C_{gd1}$ ,  $C_{gs1}$ , and  $C_{db1}$ . Assume the areas of the drains and sources of the MOSFETs measure  $6\mu\text{m} \times 10\mu\text{m}$ .

$$C_{sg2} = \frac{2}{3} \cdot C_{ox}' \cdot W_2 \cdot L_2 = \frac{2}{3} (800 \text{ aF}/\mu\text{m}^2) (10\mu\text{m} \cdot 5\mu\text{m})$$

$$= 26.7 \text{ fF}$$

$$C_{db2} = C_{jdep} = C_j \cdot A_d = (3.24 \cdot 10^{-4} \text{ F/m}^2) (6\mu\text{m} \times 10\mu\text{m})$$

$$= 19.4 \text{ fF}$$

$$C_{gd1} = C_{GDO} \cdot W_1 = (0.38 \text{ aF/m}) (10\mu\text{m})$$

$$= 3.8 \text{ fF}$$

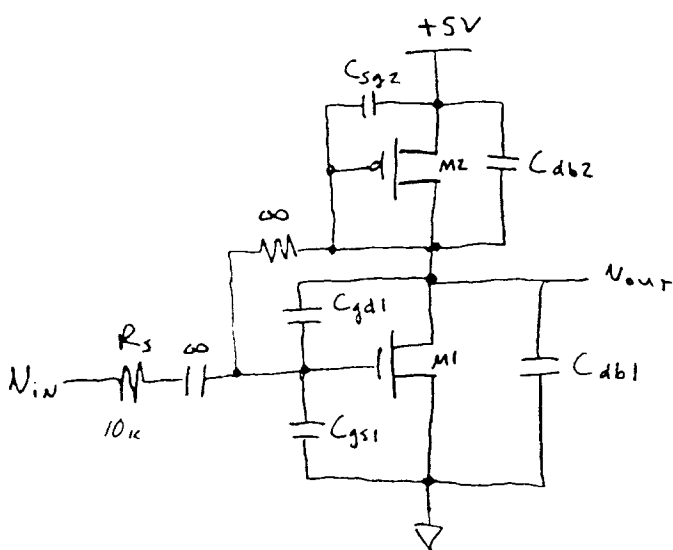
$$C_{gs1} = \frac{2}{3} C_{ox}' \cdot W_1 \cdot L_2 = \frac{2}{3} (800 \text{ aF}/\mu\text{m}^2) (10\mu\text{m} \cdot 5\mu\text{m})$$

$$= 26.7 \text{ fF}$$

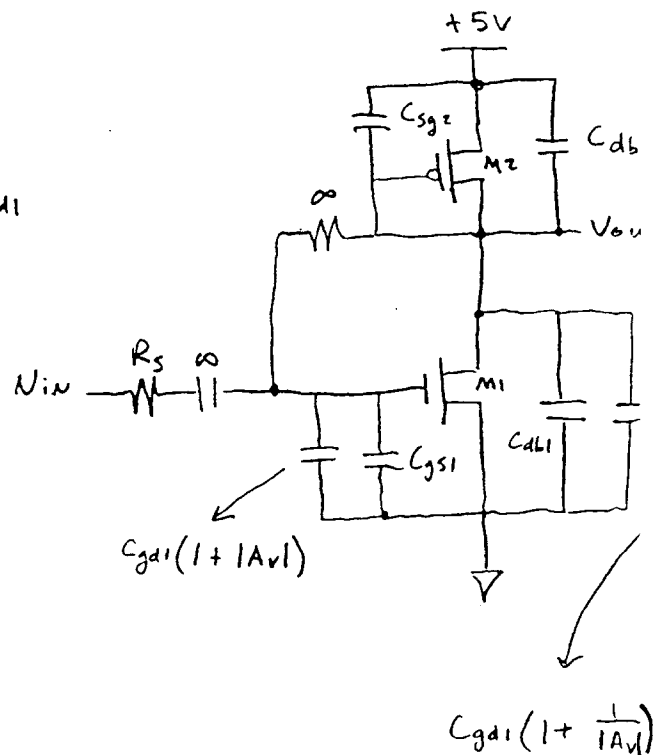
$$C_{db1} = C_{jdep} = C_j \cdot A_d = (1.04 \cdot 10^{-4} \text{ F/m}^2) (6\mu\text{m} \times 10\mu\text{m})$$

$$= 6.24 \text{ fF}$$

d) Determine the frequency response:

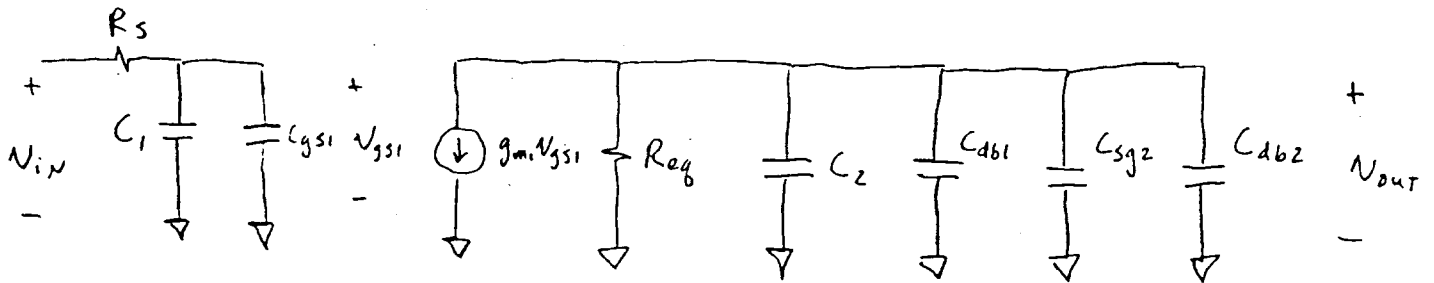


Using Miller's Theorem on  $C_{gd1}$



\* note: Using Miller's Theorem a zero is neglected.

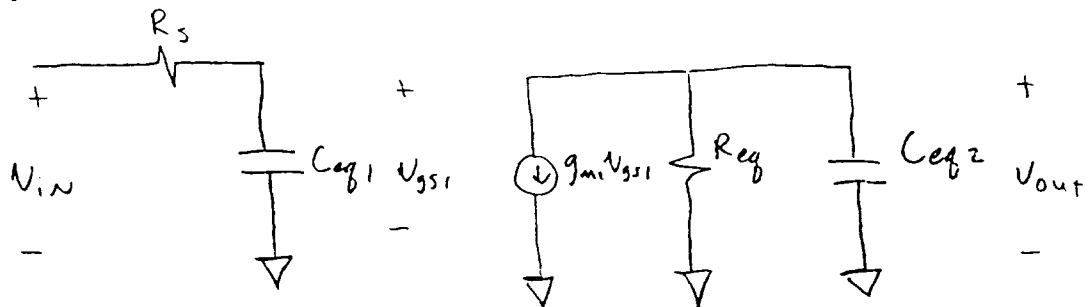
small signal model:



$$C_1 = C_{gd1} (1 + |A_{v1}|) = 9.614 \text{ fF}$$

$$C_2 = C_{gd1} \left(1 + \frac{1}{|A_{v1}|}\right) = 6.284 \text{ fF}$$

Simplify model



$$C_{eq1} = C_1 + C_{gs1}$$

$$C_{eq2} = C_2 + C_{db1} + C_{sg2} + C_{db2}$$

$$\frac{V_{out}}{V_{gs1}} = -g_{m1} \left( \frac{1}{R_{eq}} + j\omega C_{eq2} \right)$$

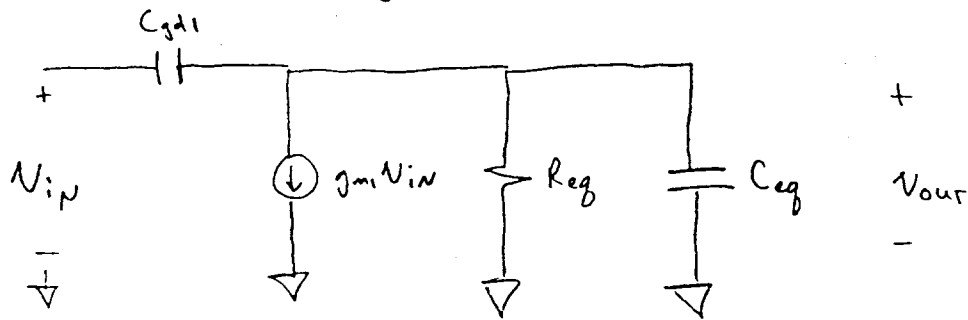
$$\frac{V_{gs1}}{V_{in}} = \frac{\frac{1}{j\omega C_{eq1}}}{\frac{1}{j\omega C_{eq1}} + R_s} = \frac{1}{1 + j\omega C_{eq1} R_s}$$

$$\frac{V_{out}}{V_{in}} = \frac{V_{out}}{V_{gs1}} \cdot \frac{V_{gs1}}{V_{in}} = -g_{m1} \left( \frac{1}{R_{eq}} + j\omega C_{eq2} \right) \left( \frac{1}{1 + j\omega C_{eq1} R_s} \right)$$

$$\frac{V_{out}}{V_{in}} = \left( \frac{-g_{m1} R_{eq}}{1 + j\omega C_{eq2} R_{eq}} \right) \left( \frac{1}{1 + j\omega C_{eq1} R_s} \right)$$

### e) The location of the zero

To determine the location of the zero use the following small signal model:



$$R_{eq} = r_{o1} \parallel \frac{1}{g_{m2}} \parallel r_{o2}$$

$$C_{eq} = C_{sg2} + C_{cd1} + C_{cb2}$$

$$V_{out} = \left[ (V_{in} - V_{out}) j\omega C_{gd1} - g_{m1} V_{in} \right] \frac{1}{\frac{1}{R_{eq}} + j\omega C_{eq}}$$

$$V_{out} \left( 1 + \frac{j\omega C_{gd1}}{\frac{1}{R_{eq}} + j\omega C_{eq}} \right) = V_{in} (j\omega C_{gd1} - g_{m1}) \frac{1}{\frac{1}{R_{eq}} + j\omega C_{eq}}$$

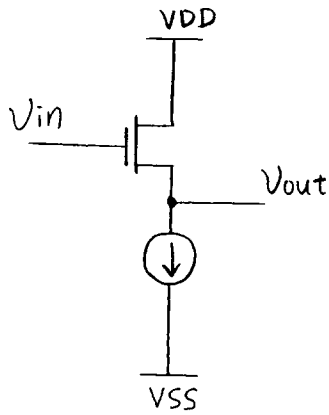
$$\frac{V_{out}}{V_{in}} = \frac{(j\omega C_{gd1} - g_{m1}) \left( \frac{1}{\frac{1}{R_{eq}} + j\omega C_{eq}} \right)}{\left( 1 + \frac{j\omega C_{gd1}}{\frac{1}{R_{eq}} + j\omega C_{eq}} \right)}$$

$$= \frac{j\omega C_{gd1} - g_{m1}}{\frac{1}{R_{eq}} + j\omega C_{eq} + j\omega C_{gd1}}$$

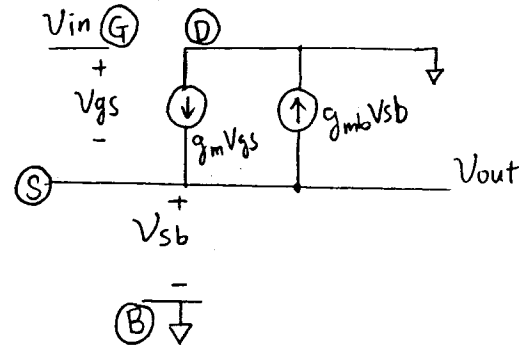
$$= \frac{-g_{m1} R_{eq} \left( j\omega \frac{C_{gd1}}{g_{m1}} - 1 \right)}{1 + j\omega (C_{eq} + C_{gd1}) R_{eq}}$$

$$\omega_z = \frac{g_{m1}}{C_{gd1}}$$

### Problem 22.5



replaced by Small  
Signal Values  $\Rightarrow$



Notice, usually  $r_o$  is very big  $r_o \gg \frac{1}{g_m}$ . So, ignore the  $r_o$  (treat it as infinite).

Obviously,  $g_m V_{gs} = g_{mb} V_{sb}$

$$V_{gs} = V_{in} - V_{out}, \quad V_{sb} = V_{out} \quad \text{and} \quad g_{mb} = \eta g_m$$

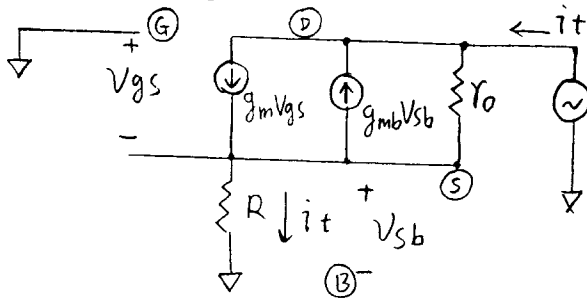
$$\Rightarrow g_m (V_{in} - V_{out}) = \eta g_m V_{out}$$

$$\Rightarrow (g_m + \eta g_m) V_{out} = g_m V_{in}$$

$$\Rightarrow \frac{V_{out}}{V_{in}} = \frac{g_m}{g_m + \eta g_m} = \frac{1}{1 + \eta}$$

### Problem 22.6

Small signal Model is shown below (Test source  $V_t$  is used):



$$V_t = (i_t - g_m V_{gs} + g_{mb} V_{sb}) r_o + i_t R$$

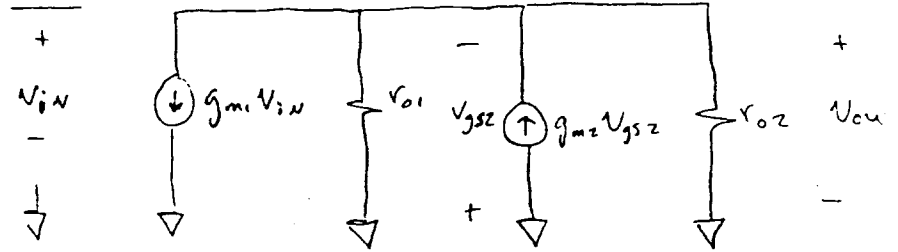
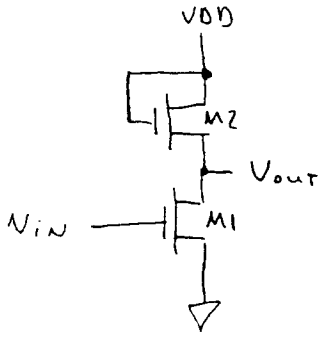
$$V_{sb} = i_t R; \quad V_{gs} = -V_{sb} = -i_t R; \quad g_{mb} = \eta g_m$$

$$\Rightarrow V_t = (i_t + g_m i_t R + \eta g_m i_t R) r_o + i_t R$$

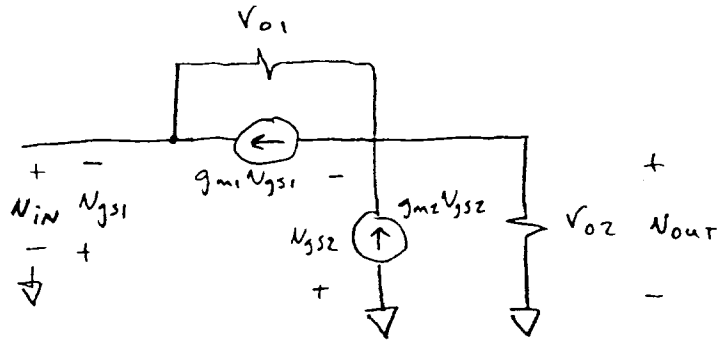
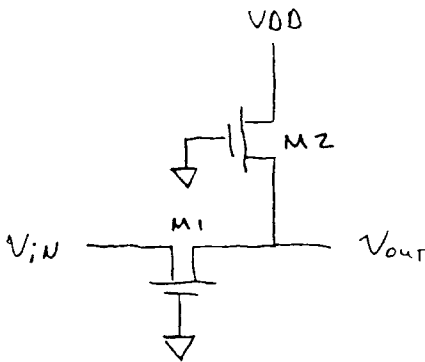
$$R_o = \frac{V_t}{i_t} = [1 + (1 + \eta) g_m R] r_o + R \approx \underline{\underline{[1 + (1 + \eta) g_m R] r_o}}$$

22.7

For the amplifiers shown in Fig P22.7, derive the small signal voltage gains using small signal models. Assume the MOSFETs used in these amplifiers are biased in the saturation region.



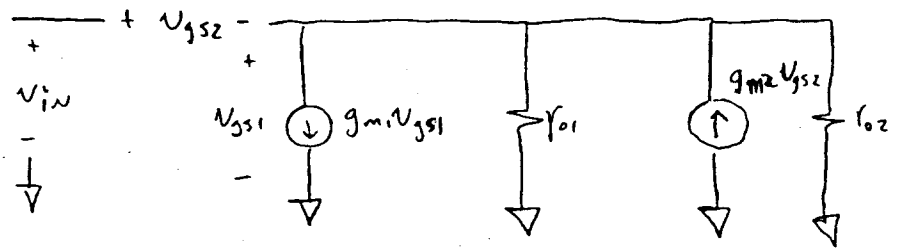
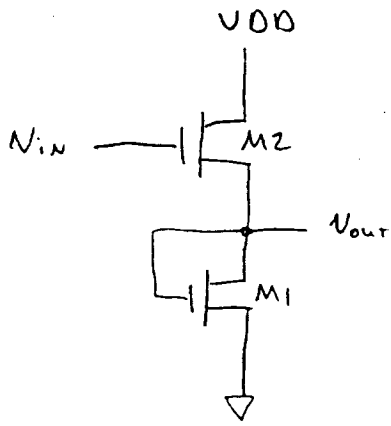
$$\frac{V_{out}}{V_{in}} = \underline{\underline{-g_{m1} \left( \frac{1}{g_{m2}} \parallel r_{o1} \parallel r_{o2} \right)}}$$



$$V_{in} = \left( \frac{V_{out}}{\frac{1}{g_{m2}} \parallel r_{o2}} - g_{m1} V_{in} \right) r_{o1} + V_{out}$$

$$V_{in} (1 + g_{m1} r_{o1}) = V_{out} \left( \frac{r_{o1}}{\frac{1}{g_{m2}} \parallel r_{o2}} + 1 \right)$$

$$\frac{V_{out}}{V_{in}} = \frac{1 + g_m r_{o1}}{\frac{1}{g_{m2}} \parallel r_{o2} + 1}$$



$$I_{out} = g_{m2} V_{gs2} \left( \frac{1}{g_{m1}} \parallel r_{o1} \parallel r_{o2} \right)$$

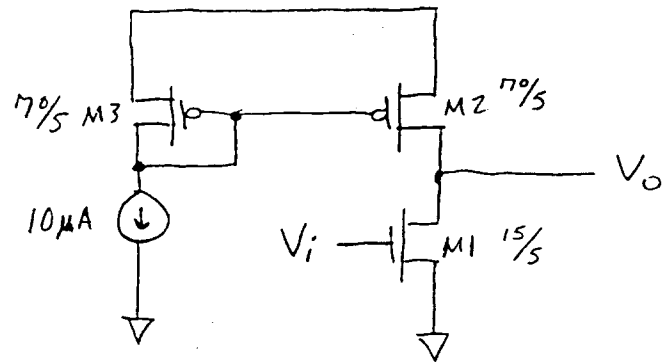
$$V_{gs2} = V_{in} - V_{out}$$

$$I_{out} = g_{m2} (V_{in} - V_{out}) \left( \frac{1}{g_{m1}} \parallel r_{o1} \parallel r_{o2} \right)$$

$$\frac{I_{out}}{I_{in}} = \frac{g_{m2} \left( \frac{1}{g_{m1}} \parallel r_{o1} \parallel r_{o2} \right)}{1 + g_{m2} \left( \frac{1}{g_{m1}} \parallel r_{o1} \parallel r_{o2} \right)}$$

22.8

Estimate the small signal voltage gain of the amplifier shown in Fig. 22.13 assuming that both M1 and M2 are biased in the saturation region.



$$\frac{V_o}{V_i} \approx - \frac{\text{resistance in the drain}}{\text{resistance in the source}}$$

$$\approx - \frac{r_{o2}}{g_{m1}} \approx -g_{m1} r_{o2}$$

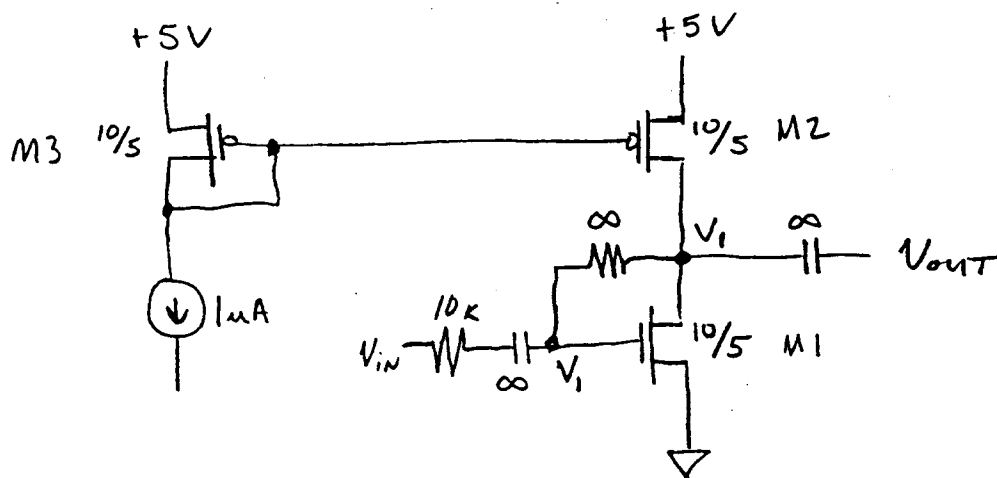
$$g_{m1} = \sqrt{2(50\mu)(15/5)(10\mu)} = 55 \mu\text{A/V}$$

$$r_{o2} = \frac{1}{\lambda I_D} = \frac{1}{(0.01)(10\mu)} = 1.67 \text{ M}\Omega$$

$$\frac{V_o}{V_i} \approx \underline{\underline{-91.85 \text{ V/V}}}$$

22.9

Repeat Problem 4 for the amplifier shown in Fig. P22.9



(a) Determine the AC voltages + currents.

$$I_{D1} = I_{D2} = \underline{1\mu A}$$

$$1\mu A = \frac{50\mu A/V^2}{2} (2) (V_1 - 0.83)^2$$

$$.02 = V_1^2 - 1.66 V_1 + .6889$$

$$0 = V_1^2 - 1.66 V_1 + .6689$$

$$V_1 = \underline{\underline{0.97 V}}$$

Find  $V_{G2}$

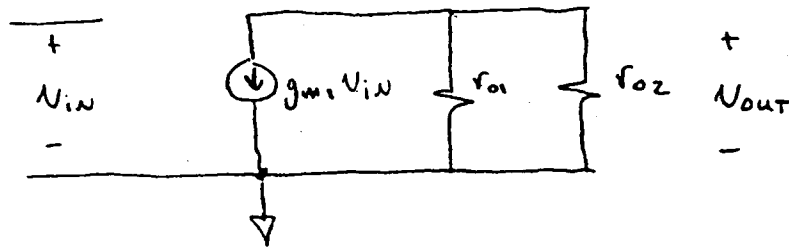
$$1\mu A = \frac{17\mu A/V^2}{2} (2) (5 - V_{G2} - .91)^2$$

$$.0588 = V_{G2}^2 - 8.18 V_{G2} + 16.7281$$

$$0 = V_{G2}^2 - 8.18 V_{G2} + 16.6693$$

$$V_{G2} = \underline{\underline{3.85 V}}$$

(b) Determine the small signal low frequency gain



$$\frac{V_{out}}{V_{in}} = -g_{m1} (r_{o1} || r_{o2})$$

$$g_{m1} = \sqrt{2\beta_1 I_{D1}} = \sqrt{2(50\mu\text{A/V}^2)(2)(1\mu\text{A})} = 14.1 \mu\text{A/V}$$

$$r_{o1} = r_{o2} = \frac{1}{\lambda I_D} = \frac{1}{0.06(1\mu\text{A})} = 16.7 \text{ M}\Omega$$

$$\frac{V_{out}}{V_{in}} = \underline{-117.85 \text{ V}}$$

(c) Determine  $C_{sg1}$ ,  $C_{db2}$ ,  $C_{gd2}$ ,  $C_{gd1}$ ,  $C_{gs1}$ , &  $C_{db1}$ . Assume the areas of the drains and sources measure  $6\mu\text{m} \times 10\mu\text{m}$ .

$$C_{sg2} = \frac{2}{3} \cdot C_{ox}' \cdot W \cdot L = \frac{2}{3} (800 \text{ fF}/\mu\text{m}^2) (10\mu\text{m} \cdot 5\mu\text{m}) = 26.7 \text{ fF}$$

$$C_{db2} = C_{jdep} = \frac{c_j \cdot A_d}{\left(1 - \frac{V_{db2}}{\phi_b}\right)^{m_j}} + \frac{c_{jsw} \cdot P_d}{\left(1 - \frac{V_{db2}}{\phi_{bsw}}\right)^{m_{jsw}}}$$

$$= \frac{3.25(10)^{-4} \text{ F/m} (10\mu\text{m} \cdot 6\mu\text{m})}{\left(1 - \frac{4.03}{1.8}\right) \cdot 0.604} + \frac{2.54(10)^{-10} \text{ F/m} (32\mu\text{m})}{\left(1 - \frac{4.03}{1.8}\right) \cdot 0.24} = 11.81$$

$$C_{gd2} = C_{GDO} \cdot W = .5026 \text{ nF/m} (10\mu\text{m}) = 5.03 \text{ fF}$$

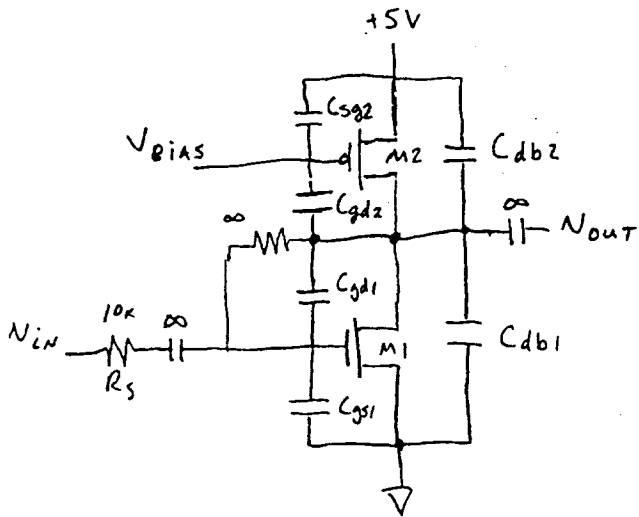
$$C_{gd1} = C_{GDO} \cdot W = .380 \text{ nF/m} (10\mu\text{m}) = 3.8 \text{ fF}$$

$$C_{gs1} = \frac{2}{3} C_{ox}' \cdot W \cdot L = \frac{2}{3} (800 \text{ fF}/\mu\text{m}^2) (10\mu\text{m} \cdot 5\mu\text{m}) = 26.7 \text{ fF}$$

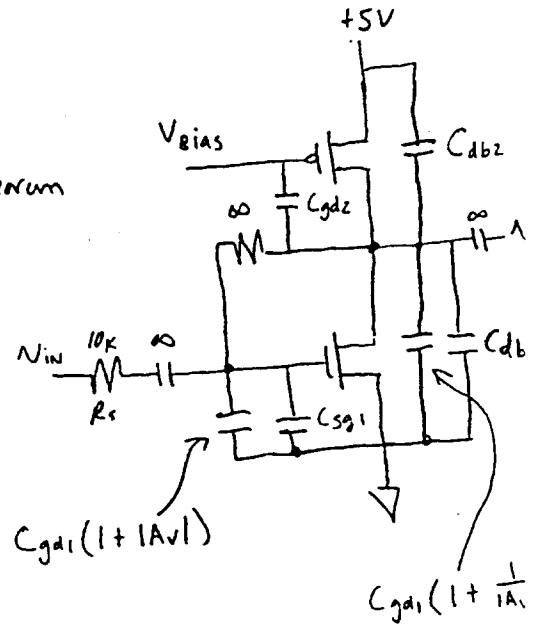
$$C_{db1} = C_{jdep} = \frac{c_j \cdot A_d}{\left(1 - \frac{V_{db1}}{\phi_b}\right)^{m_j}} + \frac{c_{jsw} \cdot P_d}{\left(1 - \frac{V_{db1}}{\phi_{bsw}}\right)^{m_{jsw}}}$$

$$= \frac{1.04(10)^{-4} \text{ F/m}^2 (10\mu\text{m} \cdot 6\mu\text{m})}{\left(1 + \frac{.97}{1.8}\right) \cdot 0.62} + \frac{2.17(10)^{-10} \text{ F/m} (32\mu\text{m})}{\left(1 + \frac{.97}{1.8}\right) \cdot 0.179} = 9.71 \text{ fF}$$

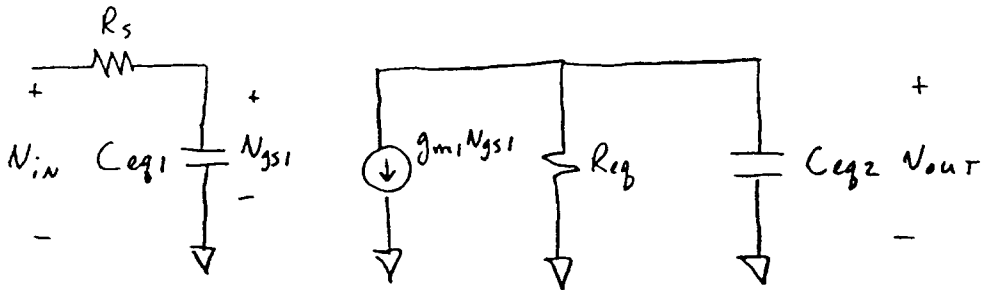
d) Determine the frequency response



Use Miller's Theorem on  $C_{gd1}$



\* Note: using Miller's Theorem neglects a zero



$$C_{eq1} = C_{gs1} + C_{gd1}(1 + |A_{v1}|) = 478.33 \text{ fF}$$

$$C_{eq2} = C_{db1} + C_{gd1}\left(1 + \frac{1}{|A_{v1}|}\right) + C_{gd2} + C_{db2} = 30.4 \text{ fF}$$

$$R_{eq} = r_{o1} \parallel r_{o2} = 8.35 \text{ M}\Omega$$

$$\frac{V_{out}}{V_{gs1}} = -g_{m1} \left( \frac{1}{\frac{1}{R_{eq}} + j\omega C_{eq2}} \right) = -g_{m1} R_{eq} \left( \frac{1}{1 + j\omega C_{eq2} R_{eq}} \right)$$

$$\frac{V_{gs1}}{V_{in}} = \frac{\frac{1}{j\omega C_{eq1}}}{R_s + \frac{1}{j\omega C_{eq1}}} = \frac{1}{1 + j\omega C_{eq1} R_s}$$

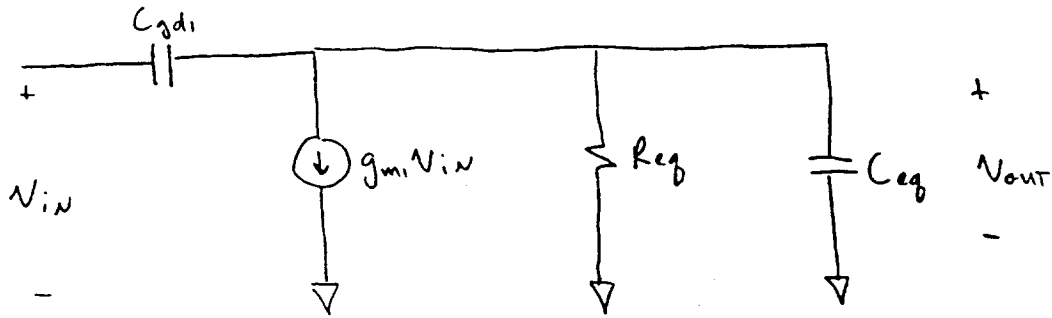
$$\frac{V_{out}}{V_{in}} = \frac{V_{out}}{V_{gs1}} \cdot \frac{V_{gs1}}{V_{in}} = -g_{m1} R_{eq} \left( \frac{1}{(1 + j\omega C_{eq2} R_{eq})(1 + j\omega C_{eq1} R_s)} \right)$$

$$\omega_{p1} = \frac{1}{C_{eq2} R_{eq}} = \frac{3.94(10)^6 \text{ rad/s}}{} \Rightarrow f_{p1} = \underline{627 \text{ kHz}}$$

$$\omega_{p2} = \frac{1}{C_{eq1} R_s} = \frac{209.06(10)^6 \text{ rad/s}}{} \Rightarrow f_{p2} = \underline{33.27 \text{ MHz}}$$

e) Determine the location of the zero in the frequency response.

Use the following small signal model ignoring  $C_{gs1}$ .



$$R_{eq} = r_{o1} || r_{o2} = 8.35 \text{ M}\Omega$$

$$C_{eq} = C_{db1} + C_{db2} + C_{gd2}$$

$$V_{out} = \left[ (V_{in} - V_{out}) j\omega C_{gd1} - g_{m1} V_{in} \right] \frac{1}{\frac{1}{R_{eq}} + j\omega C_{eq}}$$

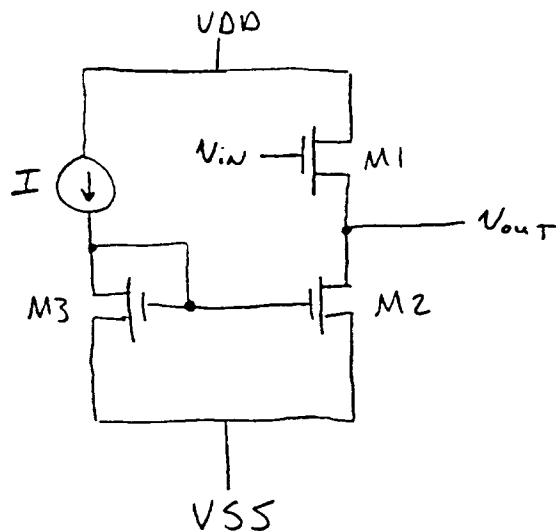
$$\frac{V_{out}}{V_{in}} = \frac{\frac{j\omega C_{gd1} - g_{m1}}{\frac{1}{R_{eq}} + j\omega C_{eq}}}{1 + \frac{j\omega C_{gd1}}{\frac{1}{R_{eq}} + j\omega C_{eq}}} = \frac{j\omega C_{gd1} - g_{m1}}{\frac{1}{R_{eq}} + j\omega C_{eq} + j\omega C_{gd1}}$$

$$= \frac{-g_{m1} R_{eq} \left( 1 - j\omega \frac{C_{gd1}}{g_{m1}} \right)}{1 + j\omega (C_{eq} + C_{gd1}) R_{eq}}$$

$$\omega_{z1} = \frac{g_{m1}}{C_{gd1}} = 3.710 (10)^9 \text{ rad/s}$$

22.10

With respect to Fig. 21.17a, what is the small-signal resistance looking into the source of M1? the drain of M2? What is the small signal resistance from the gate of M2 to ground?



- Source of M1

$$R_{inS1} = \frac{1}{g_{m1}}$$

- Drain of M2

$$R_{inD2} = r_{o2}$$

- The Gate of M2 to ground

$$R_{inG3} = \frac{1}{g_{m3}}$$

22.11

Verify that Eq. (22.51) is correct. With respect to Fig. 22.20, what is the small signal resistance looking into the drain of M4 (in terms of  $g_{m1}$ ,  $g_{m2}$ ,  $r_{o1}$ , and  $r_{o2}$ ); the source of M3? the drain of M3? the source of M2? the drain of M1? the drain of M2? the total small-signal resistance at the output?

$$R_{in4} = r_{op}$$

$$R_{in3} = \frac{r_{op} + R_{in2}}{1 + g_{mp} r_{op}}$$

$$R_{in3} = r_{op} (1 + g_{mp} r_{op}) + r_{op}$$

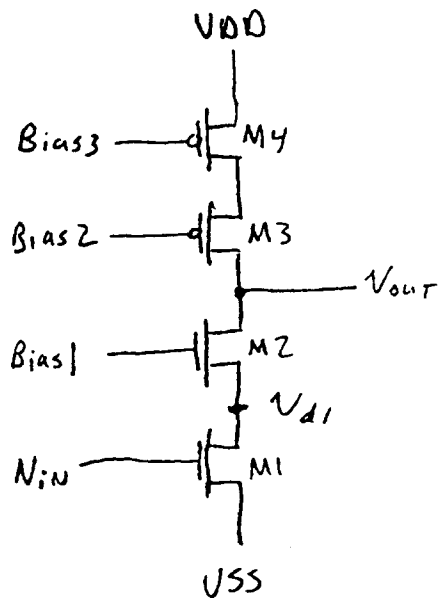
$$R_{in2} = \frac{r_{on} + R_{in1}}{1 + g_{mn} r_{on}}$$

$$R_{in1} = r_{on}$$

$$R_{in2} = r_{on} (1 + g_{mn} r_{on}) + r_{on}$$

$$R_{out} = R_{in2} \parallel R_{in3}$$

$$R_{out} = \frac{[r_{on} + r_{on} (1 + g_{mn} r_{on})] \parallel [r_{op} (1 + g_{mp} r_{op}) + r_{op}]}{1}$$



$$\frac{V_{d1}}{V_{in}} = - \frac{\cancel{R_{in2}} \parallel R_{in1}}{\frac{1}{g_{m1}}} \cdot \frac{R_{in2} \parallel R_{in3}}{\cancel{R_{in2}} \parallel R_{in1}}$$

$$\frac{V_{out}}{V_{d1}} = - g_{m1} \cdot R_{out}$$

Problem 22.12

Choosing sizes,  $M_1, M_2 \rightarrow 15\mu/5\mu$ ,  $M_3, M_4 \rightarrow 70\mu/5\mu$

$$g_{mn} = \sqrt{2\beta_n I} = \sqrt{2 \times 50 \mu\text{A}/\text{V}^2 \times \frac{15\mu}{5\mu} \times 5\mu\text{A}} = 5\sqrt{60} \mu\text{A}/\text{V} = 38.7 \mu\text{A}/\text{V}$$

$$g_{mp} = \sqrt{2\beta_p I} = \sqrt{2 \times 17 \mu\text{A}/\text{V}^2 \times \frac{70\mu}{5\mu} \times 5\mu\text{A}} = 48.8 \mu\text{A}/\text{V}$$

$$\gamma_{on} = \gamma_{op} = \frac{1}{\lambda I} = \frac{1}{0.06 \times 5\mu\text{A}} = \frac{10}{3} \text{M}\Omega$$

Therefore, from problem 22.4, we have

$$R_{d1} = \gamma_{on} = 3.33 \text{M}\Omega \quad R_{d4} = \gamma_{op} = 3.33 \text{M}\Omega$$

$$R_{d2} = g_{mn} \gamma_{on}^2 = 38.7 \mu\text{A}/\text{V} \times \left(\frac{10}{3} \text{M}\Omega\right)^2 = 430 \text{M}\Omega$$

$$R_{s2} = \frac{g_{mp}}{g_{mn}} \cdot \frac{\gamma_{op}^2}{\gamma_{on}} = \frac{48.8}{38.7} \times \frac{10}{3} \mu = 4.20 \text{M}\Omega$$

$$R_{d3} = g_{mp} \gamma_{op}^2 = 48.8 \times \left(\frac{10}{3}\right)^2 = 542.22 \text{M}\Omega$$

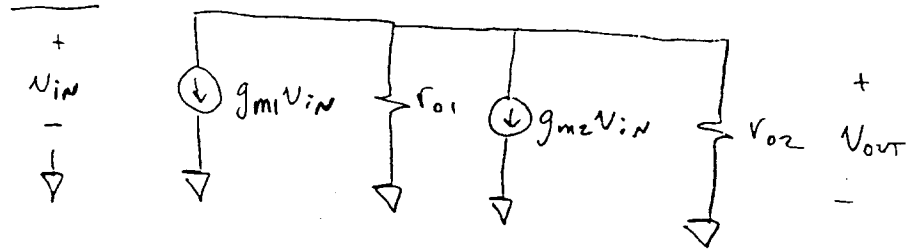
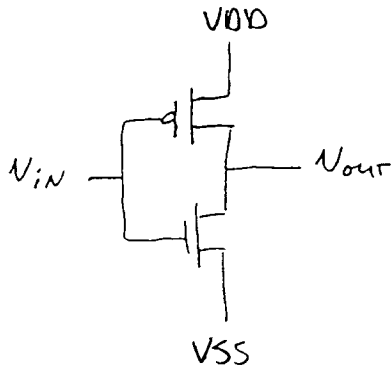
$$R_{s3} = \frac{g_{mn}}{g_{mp}} \frac{\gamma_{on}^2}{\gamma_{op}} = \frac{38.7}{48.8} \times \frac{10}{3} \text{M} = 2.64 \text{M}\Omega$$

$$R_o = \frac{g_{mn} g_{mp} \gamma_{on}^2 \gamma_{op}^2}{g_{mn} \gamma_{on}^2 + g_{mp} \gamma_{op}^2} = \frac{38.7 \times 48.8}{38.7 + 48.8} \times \left(\frac{10}{3}\right)^2 = 239.82 \text{M}\Omega$$

$$A_v = -g_{m1} R_o = -38.7 \mu \times 239.82 \text{M} = \underline{\underline{-9281 \text{V}/\text{V}}}$$

22.13

Using the small signal models, verify that Eq. (22.62) is correct.



$$V_{out} = -(g_{m1} + g_{m2})V_{in}(r_{o1} || r_{o2})$$

$$\frac{V_{out}}{V_{in}} = -(g_{m1} + g_{m2})(r_{o1} || r_{o2}) \quad \underline{\underline{\text{checks!}}}$$

22.14

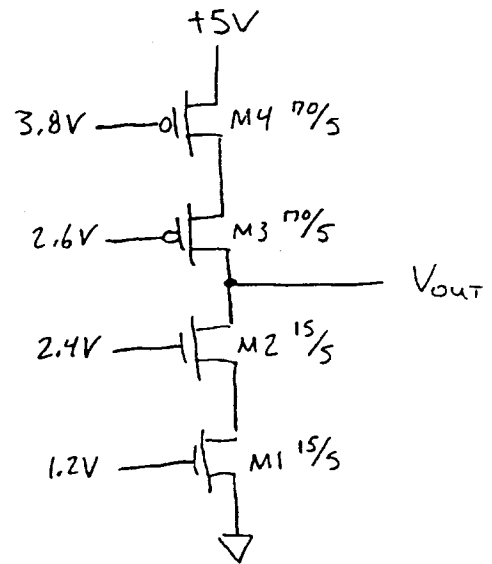
For the amplifier section shown in Fig. P22.14, estimate the minimum and maximum voltages allowable on the output in order to keep all MOSFETs in the saturation region.

Find  $V_{out(min)}$ :

$$V_{DS2} \geq V_{GS2} - V_{THN}$$

$$V_{out(min)} = 2.4 - .83$$

$$V_{out(min)} = \underline{\underline{1.57 V}}$$



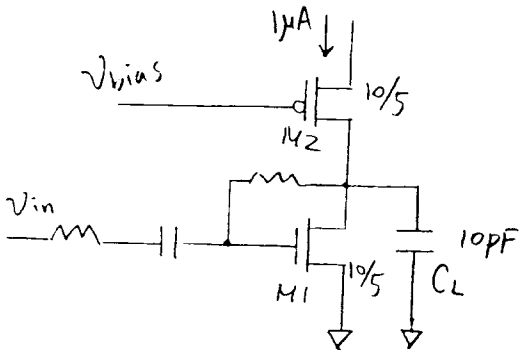
Find  $V_{out(max)}$ :

$$V_{SD3} \geq V_{SG3} - |V_{THP}|$$

$$V_{out(max)} = 2.6 + .91$$

$$V_{out(max)} = \underline{\underline{3.51 V}}$$

Problem 22.15



The maximum rate the load capacitance can be charged is:

$$SR = \frac{1\mu A}{10pF} = \underline{\underline{0.1V/\mu s}}$$

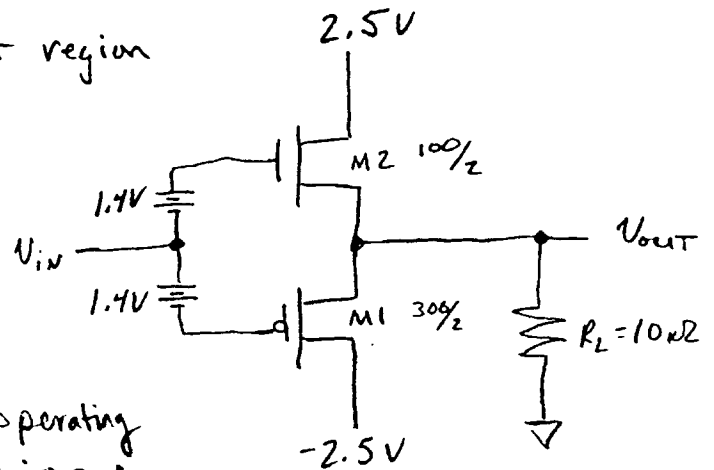
Since the voltage on gate of M1 is not fixed, there is no slew-rate limitation for discharging the capacitor.

## 22.16

For the circuit shown in Fig. P22.16, use SPICE to plot the output voltage against the input voltage. What limits the minimum and maximum output voltage swing? Also plot the current through  $M1$  &  $M2$  against the input voltage.

If we don't care what region  $M1$  &  $M2$  are operating:

$V_{o(max)}$  &  $V_{o(min)}$  are limited by  $V_{DD}$  &  $V_{SS}$ .



Keeping both  $M1$  &  $M2$  operating in the saturation region:

$V_{o(max)}$  is limited by the point where  $M2$  becomes nonsat.

$$V_{DS1} = V_{GS1} - V_{THN}$$

$$2.5 \approx V_{IN} + 1.4 - 0.83$$

$$V_{IN} \approx \underline{1.93 \text{ V}} \leftarrow \text{this is neglecting the bulk effect so this value is little low}$$

$V_{o(min)}$  is limited by the point where  $M1$  becomes nonsat.

$$V_{SD2} = V_{SG2} - V_{THP}$$

$$2.5 \approx -V_{IN} + 1.4 - 0.91$$

$$V_{IN} \approx \underline{-2.01} \leftarrow \text{neglecting bulk effect}$$

\* Problem 22.16

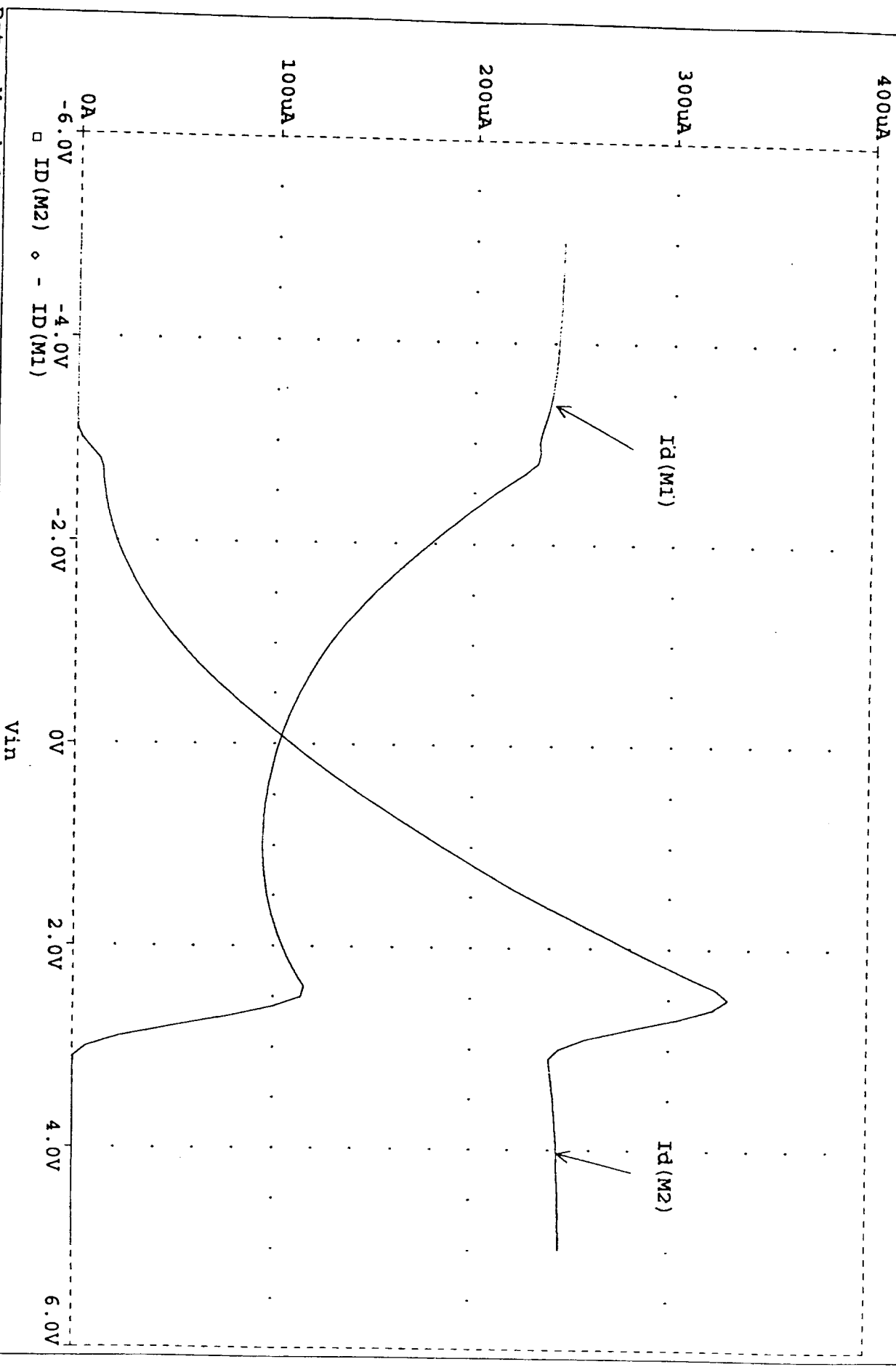
```
M1 1 2 3 4 CMOSPB L=2U W=300U
M2 4 5 3 1 CMOSNB L=2U W=100U
V1 5 6 DC 1.4
V2 6 2 DC 1.4
Vin 6 0 DC 0
RL 3 0 10k
VDD 4 0 DC 2.5
VSS 1 0 DC -2.5
```

```
* BSIM model for n-channel CN20
.MODEL CMOSNB NMOS LEVEL=4
```

```
* BSIM model for p-channel CN20
.MODEL CMOSPB PMOS LEVEL=4
```

```
.probe
.DC Vin -5 5 .1
.end
```

(A) Prob22\_16.dat



(A) Prob22\_16.dat

