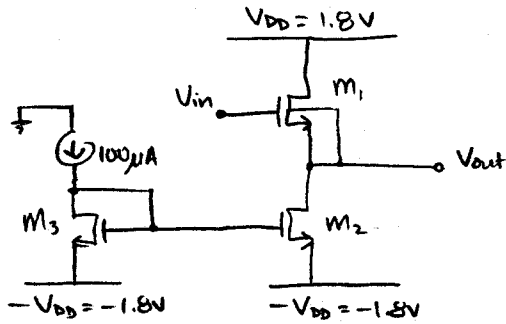
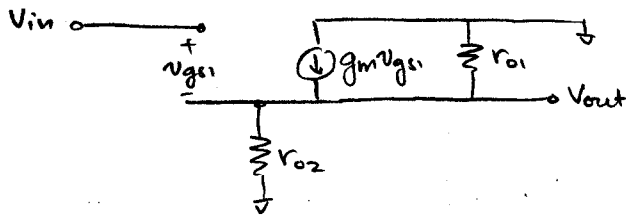


1)

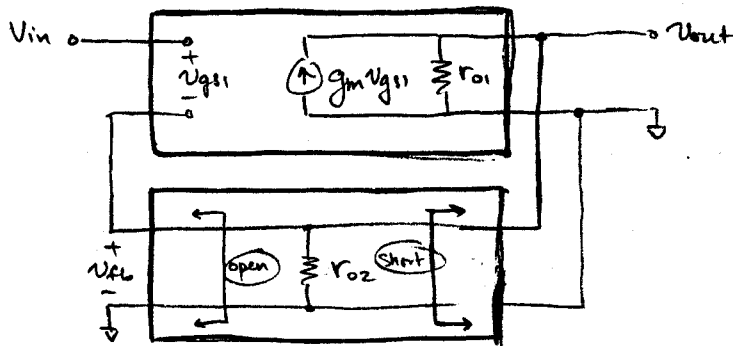


All $(\frac{W}{L}) = \frac{6}{0.18}$

a) The small-signal model for this circuit is:



Redrawing this gives:



Thus, the feedback is series-shunt.

b) The feedback factor is: $f = \frac{V_{fb}}{V_o} = 1$

c) $a_v' = g_m (r_{o1} || r_{o2})$

$T' = a_v' \cdot f = \boxed{g_m (r_{o1} || r_{o2})}$

$g_m = \sqrt{2(140 \mu\text{A}) \left(\frac{6}{0.18}\right) (100 \mu\text{m})} = 966 \mu\text{S}$

$r_{o1} = r_{o2} = \frac{1}{(0.1)(100 \mu\text{A})} = 100 \text{ k}\Omega$

$\Rightarrow \boxed{T' = 48.3}$

$r_{out}' = r_{o1} || r_{o2}$

$$1) \quad d) \quad \frac{v_{out}}{v_{in}} = \frac{1}{f} \cdot \frac{T}{1+T} = \boxed{\frac{g_m(r_{o1} \parallel r_{o2})}{1 + g_m(r_{o1} \parallel r_{o2})} = 0.98}$$

$$R_{out} = \frac{r_{out}'}{1+T} = \boxed{\frac{r_{o1} \parallel r_{o2}}{1 + g_m(r_{o1} \parallel r_{o2})} = 1.014 \text{ k}\Omega}$$

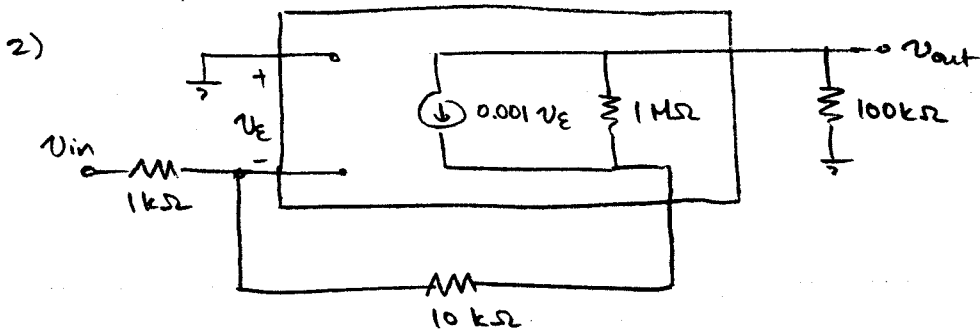
The exact expression for R_{out} is:

$$R_{out} = r_{o1} \parallel r_{o2} \parallel \frac{1}{g_m} = \frac{(r_{o1} \parallel r_{o2}) \frac{1}{g_m}}{\frac{1}{g_m} + (r_{o1} \parallel r_{o2})} = \boxed{\frac{r_{o1} \parallel r_{o2}}{1 + g_m(r_{o1} \parallel r_{o2})}}$$

The exact expression for $\frac{v_{out}}{v_{in}}$ is:

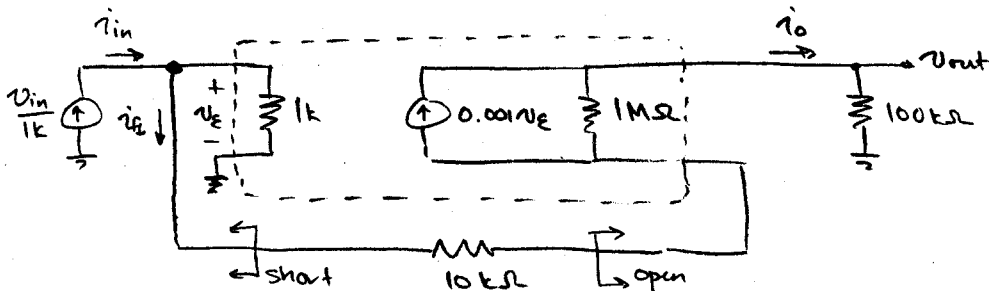
$$\frac{v_{out}}{v_{in}} = G_m R_{out} = g_m R_{out} = \boxed{\frac{g_m (r_{o1} \parallel r_{o2})}{1 + g_m (r_{o1} \parallel r_{o2})}}$$

Therefore, the feedback equations w/ loading are identical to the exact expressions calculated before.



a) The feedback is shunt-series.

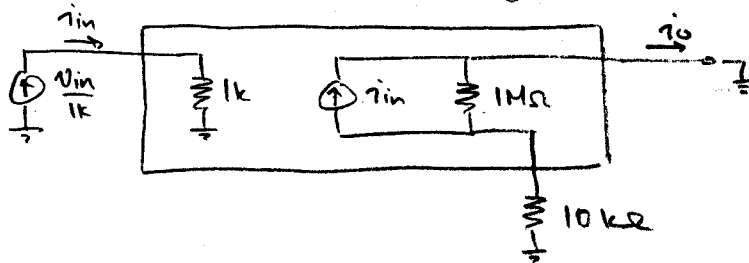
b) we should use a Norton equivalent source:



The feedback factor is: $f = \frac{r_{fb}}{r_o} = 1$

c) When considering loading effects, it is important to realize that the 100kΩ load should not be included when analyzing the feedback circuit, only at the very end. This is because it is not a part of either the main amplifier or the feedback amp.

The main amplifier with loading is:



Thus, with loading, the main amplifier becomes:

$$r_{in}' = r_{in} = 1 \text{ k}\Omega$$

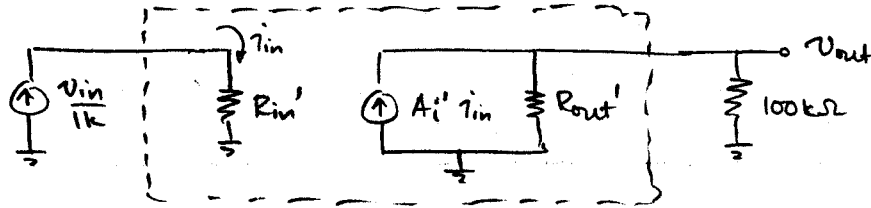
$$r_{out}' = 1 \text{ M}\Omega + 10 \text{ k}\Omega = 1.01 \text{ M}\Omega$$

$$a_i' = \frac{r_o}{r_{in}} = \frac{1 \text{ M}}{1 \text{ M} + 10 \text{ k}} = \frac{1}{1.01}$$

2) c) (cont.)

$$\text{Therefore } T' = a_i' f = \frac{1}{1.01}$$

So, the closed-loop circuit can be modeled as:



$$\text{where } R_{in}' = \frac{r_{in}'}{1+T} = \frac{1 \text{ k}\Omega}{1 + \frac{1}{1.01}} = 502 \Omega$$

$$R_{out}' = r_{out}' (1+T) = (1.01 \text{ M}) \left(1 + \frac{1}{1.01}\right) = 2.01 \text{ M}\Omega$$

$$A_i' = \frac{a_i'}{1+T'} = \frac{\frac{1}{1.01}}{1 + \frac{1}{1.01}} = \frac{1}{2.01}$$

$$\therefore R_{out} = 100 \text{ k}\Omega \parallel R_{out}' = \boxed{95.3 \text{ k}\Omega}$$

$$\begin{aligned} d) \frac{v_{out}}{v_{in}} &= \left(\frac{v_{out}}{i_{in}} \right) \left(\frac{i_{in}}{v_{in}} \right) = A_i' \left(\frac{R_{out}'}{R_{out}' + 100 \text{ k}} \right) (100 \text{ k}) \left(\frac{1}{1 \text{ k}} \right) \\ &= \frac{1}{2.01} \left(\frac{2.01}{2.01 + 0.1} \right) (100) \\ &= \frac{100}{2.11} \\ &= \boxed{47.4} \end{aligned}$$

$$e) \text{ From SPICE: } \boxed{\begin{array}{l} R_{out} = 95.3 \text{ k}\Omega \\ \frac{v_{out}}{v_{in}} = 47.4 \end{array}}$$

* hw9, 2: shunt-series feedback amplifier

```
vin    in 0 0
xamp   0 in- out+ out- opamp
r1     in in- 1k
r2     in- out- 10k
rl     out+ 0 100k
```

```
.subckt opamp in+ in- out+ out-
g1     out+ out- in+ in- 0.001
ro     out+ out- 1x
.ends
```

```
.options post=2 nomod
```

```
.tf v(out+) vin
```

```
.end
```

**** small-signal transfer characteristics

```
v(out+)/vin          = 47.4183
input resistance at  vin  = 2.1089k
output resistance at v(out+) = 95.2629k
```