

**Bandgap reference**

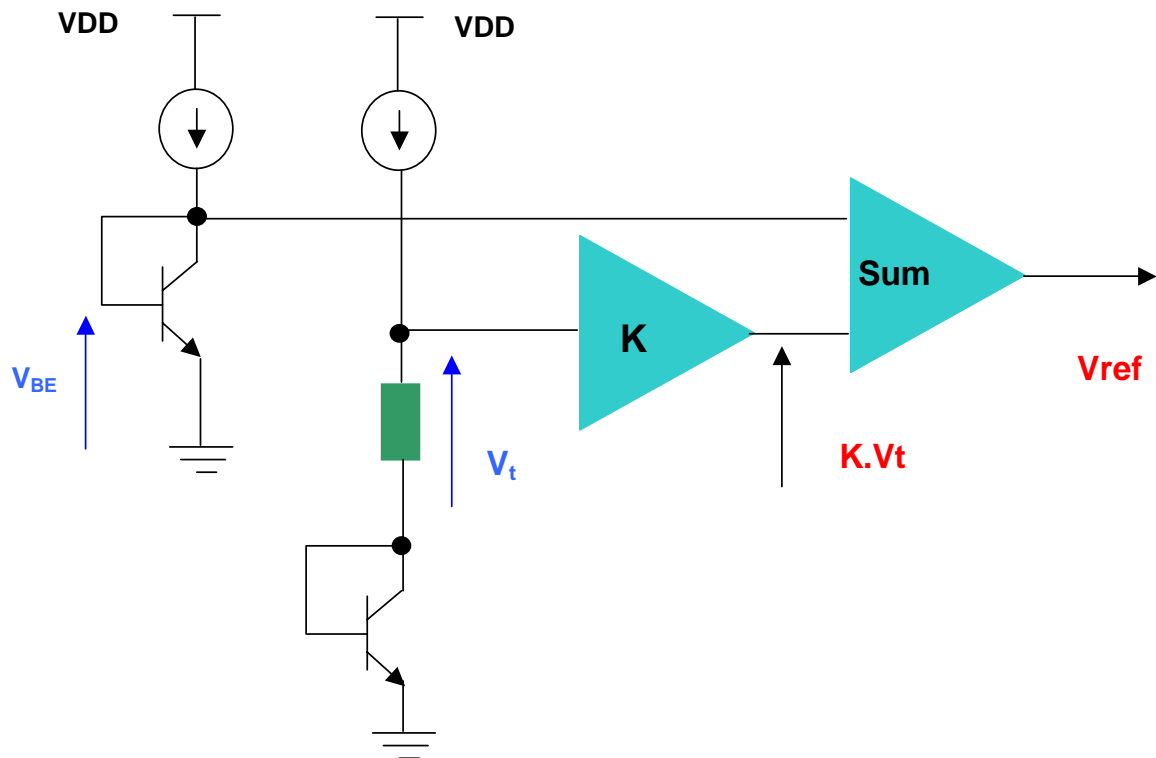
The schematic diagram of the bandgap voltage reference is shown in Figure 1. The bandgap reference has largely independent of temperature and the supply rails and is therefore used as the controlling current source for mirroring throughout a circuit eg an op-amp.

As shown in the diagram there are two voltage sources, one generated across a diode junction ie  $V_{BE}$  (eg the base-emitter junction on a bipolar transistor) and the other a thermal voltage  $V_t$ .

$V_{BE} = -2.2mV/^{\circ}C$  and  
 $V_t = +0.085mV/^{\circ}C$

Thus if multiply  $V_t$  by a constant  $K$  and combine with  $V_{BE}$  it is possible to cancel the temperature effects of each voltage source to leave a stable reference voltage  $V_{REF}$  ie

$V_{REF} = V_{BE} + K.V_t$



**Figure 1 Schematic diagram of a bandgap reference.  $V_{ref} = K.V_t + V_{BE}$ .**

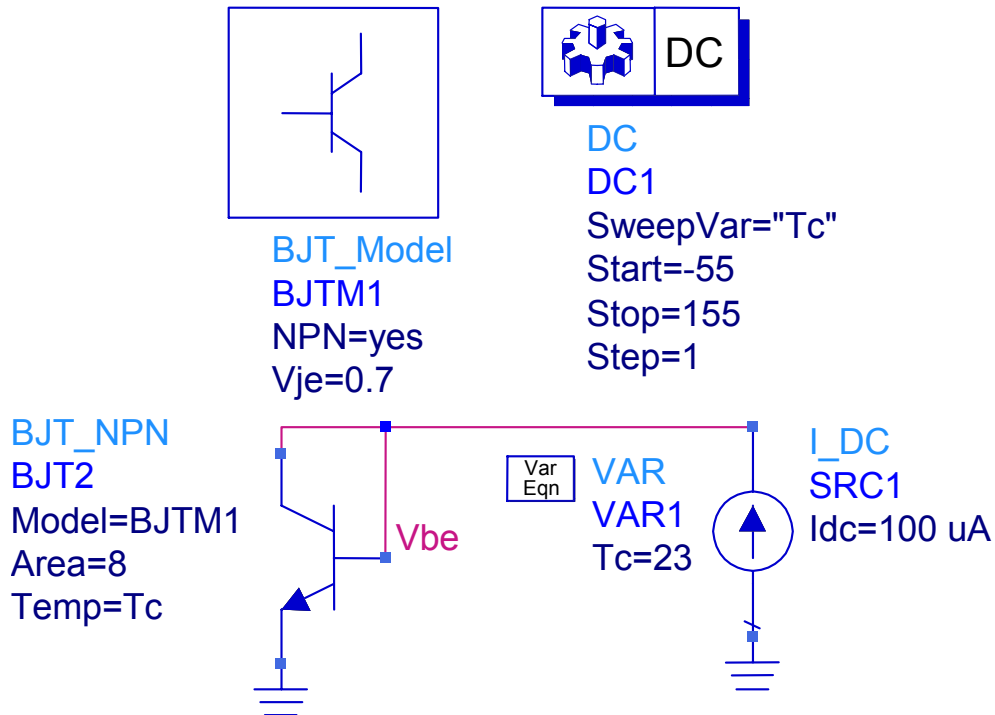


Figure 2 ADS simulation setup to determine the temperature dependence of Vbe. The temperature variable of the BJT model Tc is sweep by the DC simulation from -55 to 155 degrees C.

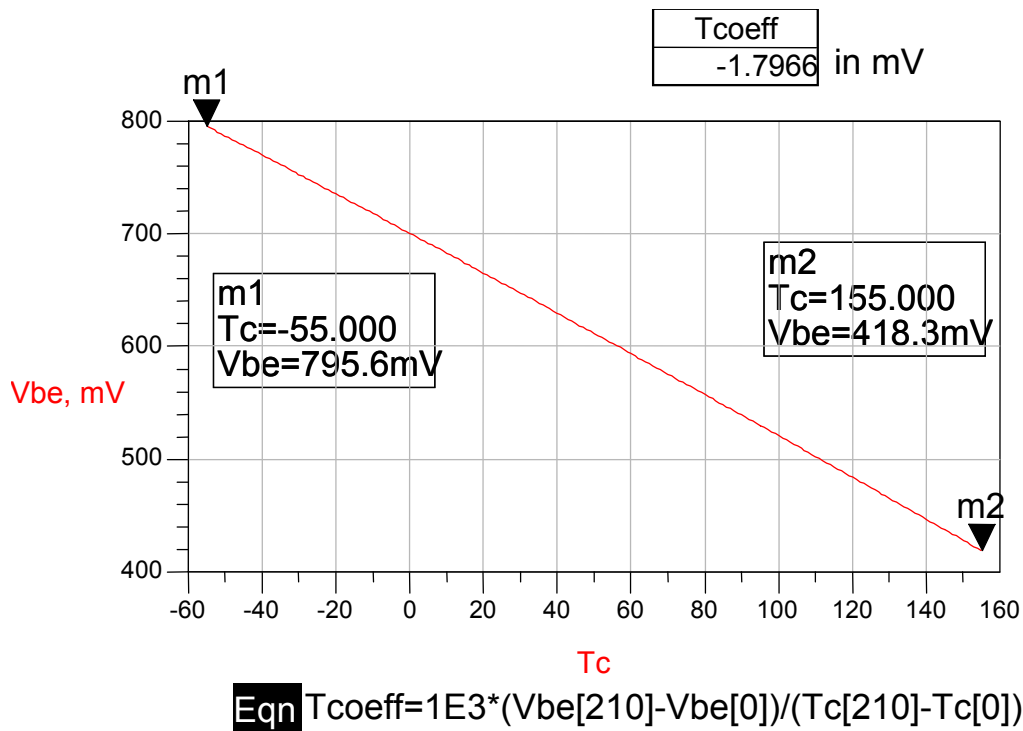


Figure 3 Temperature dependance of Vbe as simulated from the ADS simulation of Figure 2. Temperature coefficient of VBE ~ -1.79mV/°C.

$$\text{Eqn } T_{\text{coeff}} = 1E3 * (V_{\text{be}}[210] - V_{\text{be}}[0]) / (T_{\text{c}}[210] - T_{\text{c}}[0])$$



### Temperature dependance of VBE

We can simulate the temperature effect of  $V_{BE}$  by using the ADS simulation shown in Figure 2. In this simulation the temperature parameter of the generic spice BJT model (TC) is sweep by the DC simulation from  $-55$  to  $155$  degrees C.

The resulting plot of Vbe vs temperature is shown in Figure 3. An equation has been added to calculate the temperature coefficient by taking the first and last data points [0] and [210] to calculate the slope of the graph.

Bipolar collector current is given by :-

$$I_c = I_s \cdot \exp\left(\frac{V_{BE}}{V_t}\right)$$

Where

$$V_t = \text{Thermal Voltage given by Where } V_t = \frac{kT}{q}$$

$$q = \text{charge on electron} = 1.602 \times 10^{-19} \text{ C}$$

$$K = \text{Boltzmanns constant} = 1.3807 \times 10^{-23} \text{ J.K}^{-1}$$

$$I_s \propto \mu \cdot K \cdot T \cdot n_i^2 \quad - (1)$$

Where

$$n_i^2 = \text{Intrinsic carrier concentration in Silicon } (1.5 \times 10^{10} \text{ cm}^{-3})$$

$\mu$  = Mobility of minority carriers

Temperature dependance of key variables

$$\mu \propto \mu_0 \cdot T^m \quad \text{Where } m \approx -\frac{3}{2} \quad - (2)$$

$$n_i^2 \propto T^3 \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] \quad - (3) \quad \text{Where } E_g = \text{bandgap voltage} = 1.12 \text{ eV for silicon}$$



Sub equations 3 & 2 into 1

$$I_s \propto \mu_o \cdot T^m \cdot K \cdot T \cdot T^3 \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] = A \cdot T^{4+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] \text{ Where constant A includes } \mu_o \cdot K$$

$$V_{BE} = V_T \cdot \ln\left(\frac{I_c}{I_s}\right)$$

$$\frac{\partial V_{BE}}{\partial T} \text{ of } V_T \cdot \ln\left(\frac{I_c}{I_s}\right) = \frac{\partial V_T}{\partial T} \cdot \ln\left(\frac{I_c}{I_s}\right)$$

$$\text{To find } \frac{\partial I_s}{\partial T} \text{ expand out to get } V_T \ln I_c - V_T \ln I_s \therefore \frac{\partial I_s}{\partial T} \Rightarrow -V_T \cdot \frac{1}{I_s} \cdot \frac{\partial I_s}{\partial T}$$

$$\text{As } \ln ax = \frac{1}{x} \frac{\partial y}{\partial x}$$

$$\frac{\partial V_{BE}}{\partial T} = \frac{\partial V_T}{\partial T} \cdot \ln\left(\frac{I_c}{I_s}\right) - \frac{V_T}{I_s} \cdot \frac{\partial I_s}{\partial T}$$

$$I_s = A \cdot T^{4+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] \text{ Use } ax^n = anx^{n-1} \cdot \frac{dy}{dx}$$

$$\frac{\partial I_s}{\partial T} = (4+m)A \cdot T^{3+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] + A \cdot T^{4+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] \cdot \left[\frac{-E_g}{K \cdot T^2}\right]$$

$$\frac{V_T}{I_s} \cdot \frac{\partial I_s}{\partial T} = \frac{V_T(4+m)A \cdot T^{3+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right]}{A \cdot T^{4+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right]} + \frac{V_T A \cdot T^{4+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right] \cdot \left[\frac{-E_g}{K \cdot T^2}\right]}{A \cdot T^{4+m} \cdot \exp\left[\frac{-E_g}{K \cdot T}\right]}$$

$$\frac{V_T}{I_s} \cdot \frac{\partial I_s}{\partial T} = \frac{V_T(4+m)}{T} + V_T \left[\frac{-E_g}{K \cdot T^2}\right]$$



$$\frac{\partial V_{BE}}{\partial T} = \frac{\partial V_T}{\partial T} \cdot \ln\left(\frac{I_C}{I_S}\right) - \frac{V_T}{I_S} \cdot \frac{\partial I_S}{\partial T}$$

$$= \frac{V_T}{T} \cdot \ln\left(\frac{I_C}{I_S}\right) + \frac{V_T(4+m)}{T} + V_T \left[ \frac{-E_g}{K \cdot T^2} \right] \quad V_{BE} = V_T \cdot \ln\left(\frac{I_C}{I_S}\right) \text{ \& } V_T = \frac{kT}{q}$$

$$\frac{\partial V_{BE}}{\partial T} = \frac{V_{BE}}{T} + \frac{V_T(4+m)}{T} + \frac{kT}{q} \left[ \frac{-E_g}{K \cdot T^2} \right] = \boxed{\frac{V_{BE}}{T} + \frac{V_T(4+m)}{T} + \frac{1}{q} \left[ \frac{-E_g}{T} \right]}$$

### Evaluation of $dV_{BE}/dT$

$$V_T = \frac{kT}{q} = \frac{1.3807 \times 10^{-23} \cdot 300}{1.602 \times 10^{-19}} = 25.8 \text{ mV}$$

Where  $E_g$  = Bandgap voltage (for silicon = 1.12eV) &  $m = -\frac{3}{2}$

and

$K$  = Boltzmanns constant =  $1.3807 \times 10^{-23}$  J.K<sup>-1</sup>

$q$  = charge on electron =  $1.602 \times 10^{-19}$  C

$$V_{BE} = V_T \cdot \ln\left(\frac{I_E}{I_S}\right) \quad \text{Where } I_S = \frac{q \cdot A \cdot n_i^2 \cdot \overline{D_n}}{Q_B} \quad \text{Typical values are } 10^{-14} \text{ to } 10^{-16} \text{ A}$$

Where

$Q_B = W_B \cdot N_A$  is the number of doping atoms in the base per unit area of the emitter.  
(for 0.8um process  $N_A = 3 \times 10^{16}$  for p - type device);  $W_B$  = base width.

$\overline{D_n}$  = The average effective value for the electron diffusion constant in the base.  
(Typically =  $13 \text{ cm}^2 \text{ s}^{-1}$ ).

$n_i^2$  = Intrinsic carrier concentration in Silicon ( $1.5 \times 10^{10} \text{ cm}^{-3}$ )

$A$  = Base - Emitter area.



To find a typical value for  $V_{be}$  and  $\Delta V_{be}$  assume  $I_E = 50\mu A$ ,  $A = 1\mu m^2$   
then

$$V_{BE} = V_t \cdot \ln\left(\frac{I_E}{I_S}\right) \quad \text{Where } I_S = \frac{q \cdot A \cdot n_i^2 \cdot \bar{D}_n}{Q_B}$$

$$Q_B = W_B \cdot N_A = 1 \times 10^{-6} \cdot 3 \times 10^{16} = 3 \times 10^{10}$$

$$I_S \approx \frac{1.602 \times 10^{-19} \cdot 1 \times 10^{-6} \cdot (1.5 \times 10^{10})^2 \cdot 0.013}{3 \times 10^{10}} = 1.562 \times 10^{-17} \text{ A}$$

$$V_{BE} = 25.8 \times 10^{-3} \cdot \ln\left(\frac{50 \times 10^{-6}}{1.562 \times 10^{-17}}\right) = 0.743 \text{ V}$$

$$\frac{\partial V_{BE}}{\partial T} = \frac{V_{BE} - (4 + m)V_T - \frac{Eq}{q}}{T}$$

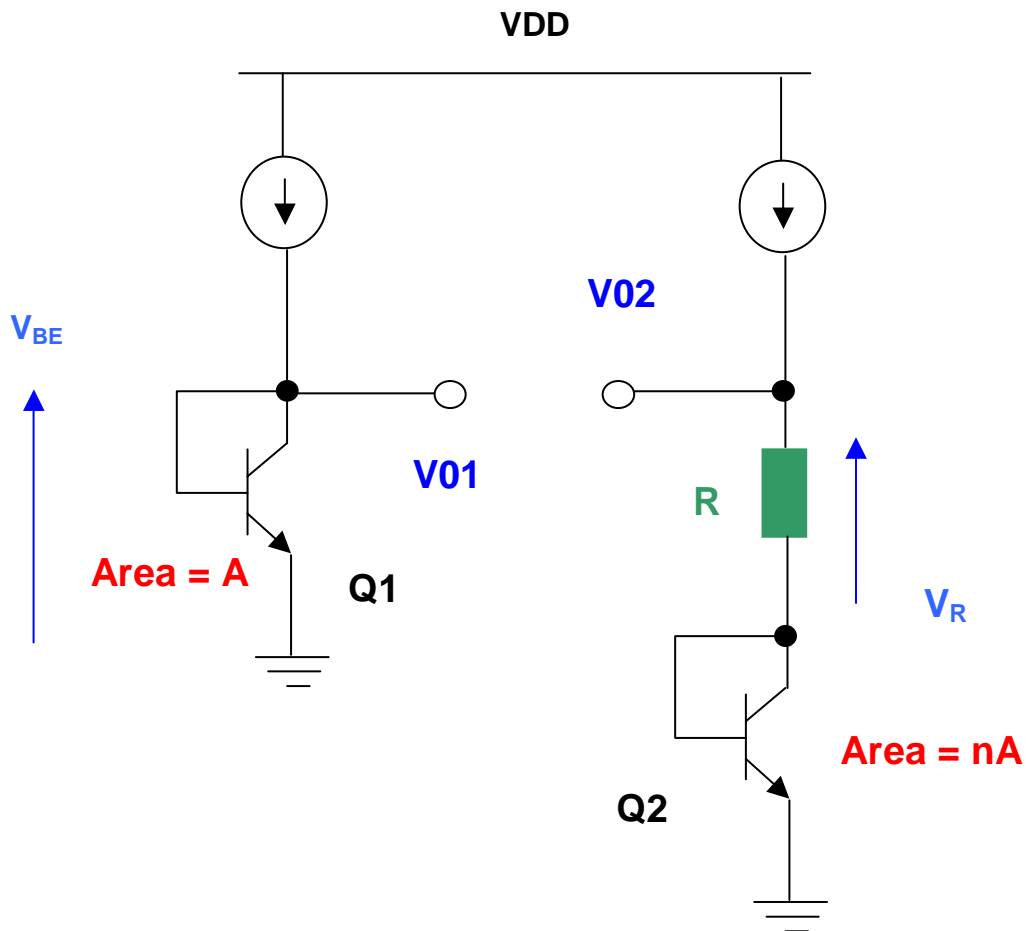
$$V_T = 25.8 \text{ mV} \quad \& \quad V_{BE} = 0.743 \text{ V}$$

Where  $Eq = \text{Bandgap voltage (for silicon} = 1.12 \text{ eV)}$  &  $m = -\frac{3}{2}$

$$\frac{\partial V_{BE}}{\partial T} = \frac{0.743 - \left(4 - \frac{3}{2}\right)25.8 \times 10^{-3} - 1.11}{300} = \boxed{-1.44 \text{ mV/}^\circ\text{K}}$$

**$V_{PTAT}$  generation**

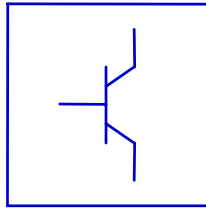
The PTAT term is realised by determining the voltage difference between two forward-biased diodes (eg  $V_{BE}$ ). MOS transistors operating in the weak inversion region can also be used to form the diodes.



**Figure 4 Generation of VPTAT voltage.**

We can simulate the variation VPTAT over temperature using the ADS simulation shown in Figure 5.

If we run the same simulation again but this time on the results graph we calculate  $V_{ref}$  given that we know  $v_{be1}$  and  $(v_{be1} - v_{be2})$ . Various values of K were tried until the temperature compensation was achieved as shown in the graph of Figure 7. This now forms the basis of the band-gap reference in a practical circuit the voltage summing and setting of K is achieved using a resistive network and an op-amp.



BJT\_Model  
BJTM1  
NPN=yes  
Vje=0.7



DC  
DC1  
SweepVar="Tc"  
Start=-55  
Stop=155  
Step=1

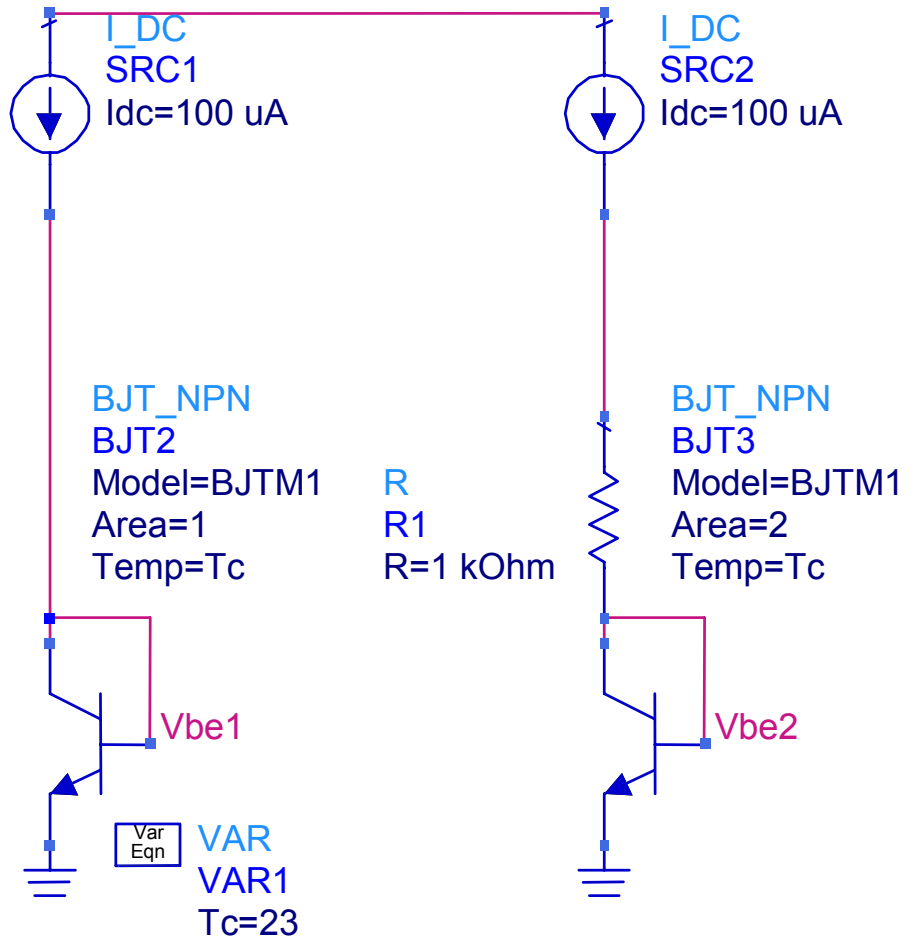
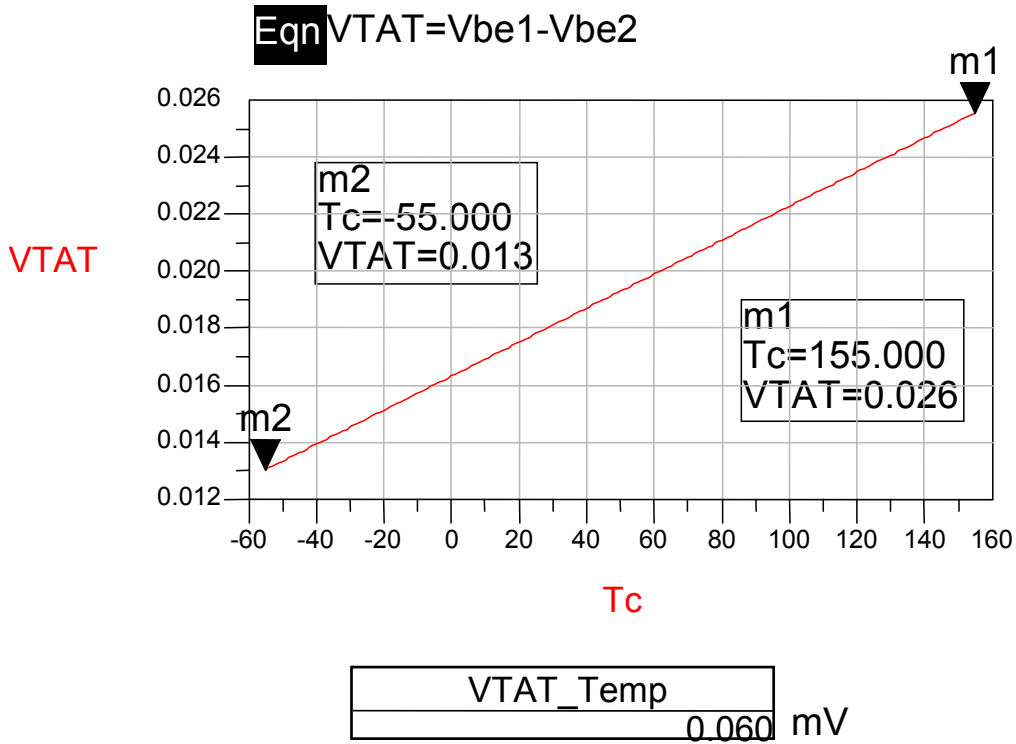


Figure 5 ADS simulation setup to analyse the variation of VPTAT over temperature. As for the previous examples the temperature is swept in the DC simulation box. The resulting plot is shown in Figure 6.



**Eqn**  $VTAT\_Temp = 1e3 * (VTAT[210] - VTAT[0]) / (Tc[210] - Tc[0])$

Figure 6 Resulting simulation of VPTAT vs temperature after running the simulation shown in Figure 5.



Figure 4 shows how the VPTAT voltage can be realised. If we force  $V_{01}$  and  $V_{02}$  to be the same then the voltage across the resistor  $R$  will be the difference of the two  $V_{BE}$ 's.

$$I_E = A \cdot J_S \left( e^{\frac{q \cdot V_{BE}}{kT}} - 1 \right) \approx A \cdot J_S \left( e^{\frac{q \cdot V_{BE}}{kT}} \right) \text{ When } I_E > 0$$

Assume circuit is configured such that  $I_{E1} = I_{E2}$  then

$$\frac{I_{E2}}{I_{E1}} = \left( \frac{A_2 \cdot J_S}{A_1 \cdot J_S} \right) e^{\frac{V_{BE1} - V_{BE2}}{v_t}} \quad \text{Where } v_t = \frac{kT}{q}$$

Assume transistors are from the same process, such that  $J_S$  and  $v_t$  are the same for each device then

$$e^{\frac{V_{BE1} - V_{BE2}}{v_t}} = \left( \frac{I_{E2}}{I_{E1}} \right) \left( \frac{A_1}{A_2} \right) = \left( \frac{A_1}{A_2} \right) \text{ If } I_{E1} = I_{E2}$$

$$e^{\frac{V_{BE1} - V_{BE2}}{v_t}} = \left( \frac{A_1}{A_2} \right) \text{ Rearrange to give } V_{BE1} - V_{BE2} = v_t \cdot \ln \left( \frac{A_1}{A_2} \right)$$

$$\text{If } A_1 > A_2 \text{ then } V_{BE2} - V_{BE1} = v_t \cdot \ln \left( \frac{A_1}{A_2} \right) = \Delta V_{be} = I_{E1} \cdot R_1 \quad (I_{E1} = I_{E2})$$

$$\text{Let } n = \left( \frac{A_1}{A_2} \right) \text{ and } V_T = \frac{kT}{q}$$

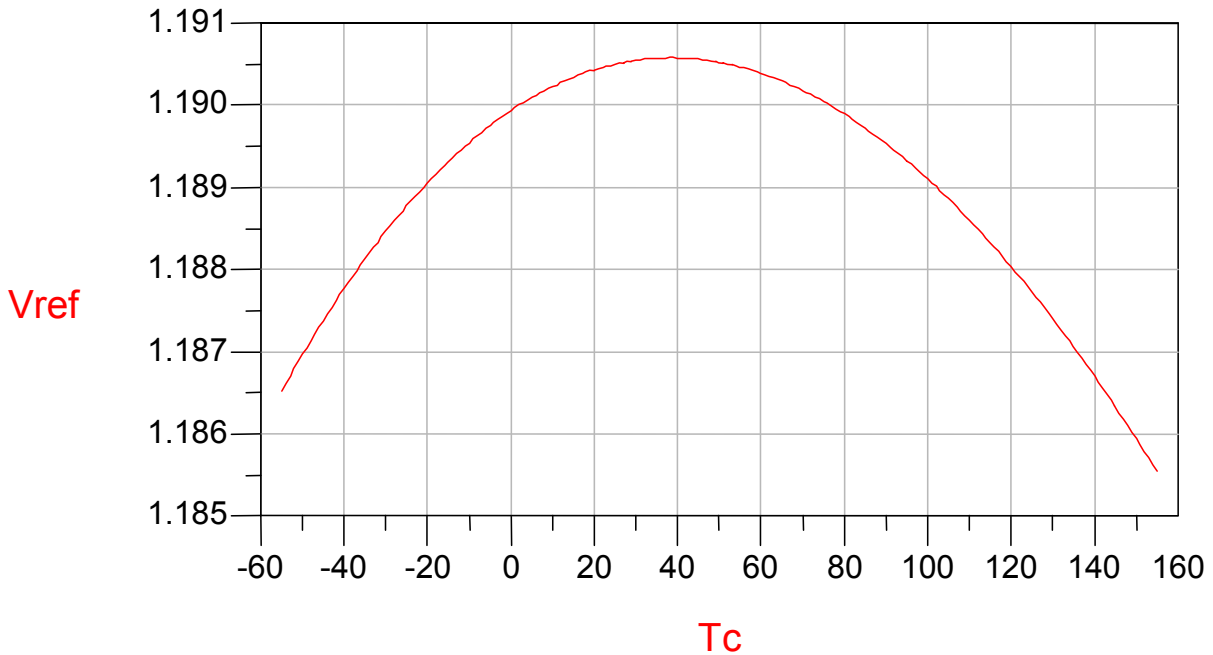
$$\therefore \Delta V_{be} = \frac{kT}{q} \cdot \ln(n) \quad \therefore \frac{\partial \Delta V_{be}}{\partial T} = \frac{K}{q} \cdot \ln(n) \text{ Using } ax^n = anx^{n-1} \cdot \frac{dy}{dx}$$

Where

$K = \text{Boltzmanns constant} = 1.3807 \times 10^{-23} \text{ J.K}^{-1}$

$q = \text{charge on electron} = 1.602 \times 10^{-19} \text{ C}$

$A = \text{Area of base-emitter junction } \mu\text{m}^2$



**Eqn**  $K=27$    **Eqn**  $V_{TAT}=V_{be1}-V_{be2}$

**Eqn**  $V_{ref}=V_{be1}+(K*V_{TAT})$

Figure 7 Graph of the simulation shown in Figure 5. In this case we have calculated  $V_{TAT}$  as  $v_{be1}-v_{be2}$  and evaluated  $V_{ref}$  from  $V_{be1}+(K*V_{TAT})$ , where  $K = 27$ .

**BandGap reference voltage**

Previously we found  $\Delta V_{be} = V_{BE1} - V_{BE2} = \frac{KT}{q} \ln\left(\frac{J_{C1}}{J_{C2}}\right) = \frac{KT}{q} \ln\left(\frac{A_1}{A_2}\right)$

and therefore  $\frac{\partial \Delta V_{be}}{\partial T} = \frac{V_T}{T} \ln\left(\frac{J_{C1}}{J_{C2}}\right)$

$\frac{\partial V_{BE}}{\partial T} = \frac{V_{BE}}{T} + \frac{V_T(4+m)}{T} + \frac{1}{q} \left[ \frac{-E_g}{T} \right] = -1.44mV/^{\circ}K$



The band-gap reference voltage is given by:-

$$V_{REF} = V_{BE} + K.V_t$$

The temperature stable value of  $V_{REF}$  at 300°K is 1.262V. Therefore the value of K required is:

$$V_{REF} = V_{BE} + K.V_T \quad \text{Rearrange to get K}$$

$$K = \frac{V_{REF} - V_{BE}}{V_T} \quad \text{With } V_{BE} = 0.743 \text{ (Calculated earlier)}$$

$$V_T = \frac{KT}{q} = \frac{1.3807 \times 10^{-23} \cdot 300}{1.602 \times 10^{-19}} = 25.8\text{mV}$$

$$K = \frac{1.262 - 0.743}{25.8 \times 10^{-3}} = 20.11$$

With reference to Figure 8.

The cascode current mirror makes  $I_1 = I_2 = I_3$

$$\text{The voltage across R} = \Delta V_{be} = V_{BE2} - V_{BE1} = V_t \cdot \ln\left(\frac{A_1}{A_2}\right) \quad \text{Let } N = \frac{A_1}{A_2}$$

$$\text{and so } I_2 = \frac{V_t}{R} \cdot \ln(N) = I_1 = I_3$$

$$V_{OUT} = I_3 \cdot K \cdot R + V_{BE3} \quad \text{As } I_3 = I_2 \text{ sub in } I_3 = \frac{V_t}{R} \cdot \ln(N)$$

$$V_{OUT} = \frac{V_t}{R} \cdot \ln(N) \cdot K \cdot R + V_{BE3}$$

$$\therefore V_{OUT} = V_t \cdot \ln(N) \cdot K + V_{BE3}$$



Assume a temperature of 23° C and that  $R = 1\text{K}\Omega$ ;  $N = 8$

$$v_t = \frac{kT}{q} = \frac{1.38 \times 10^{-23} \cdot (273 + 23)}{1.602 \times 10^{-19}} = 0.025\text{V}$$

$$I_2 = \frac{\Delta V_{be}}{R_1} = \frac{V_t \cdot \ln\left(\frac{A_1}{A_2}\right)}{R_1} = \frac{(0.025) \cdot \ln\left(\frac{8}{1}\right)}{1 \times 10^3} = 52\mu\text{A at } 23^\circ\text{C}$$

$$\text{With } \Delta V = V_t \cdot \ln\left(\frac{A_1}{A_2}\right) = (0.025) \cdot \ln\left(\frac{8}{1}\right) = 0.0536\text{V}$$

The zero temperature coefficient reference voltage at 23° C = 1.262V

$$\therefore K = \frac{V_{REF} - V_{be}}{V_t \cdot \ln(N)} = \frac{1.262 - 0.63}{0.025 \cdot \ln(8)} = 10.45$$

$$\therefore K \cdot R = 10.45\text{K}\Omega$$

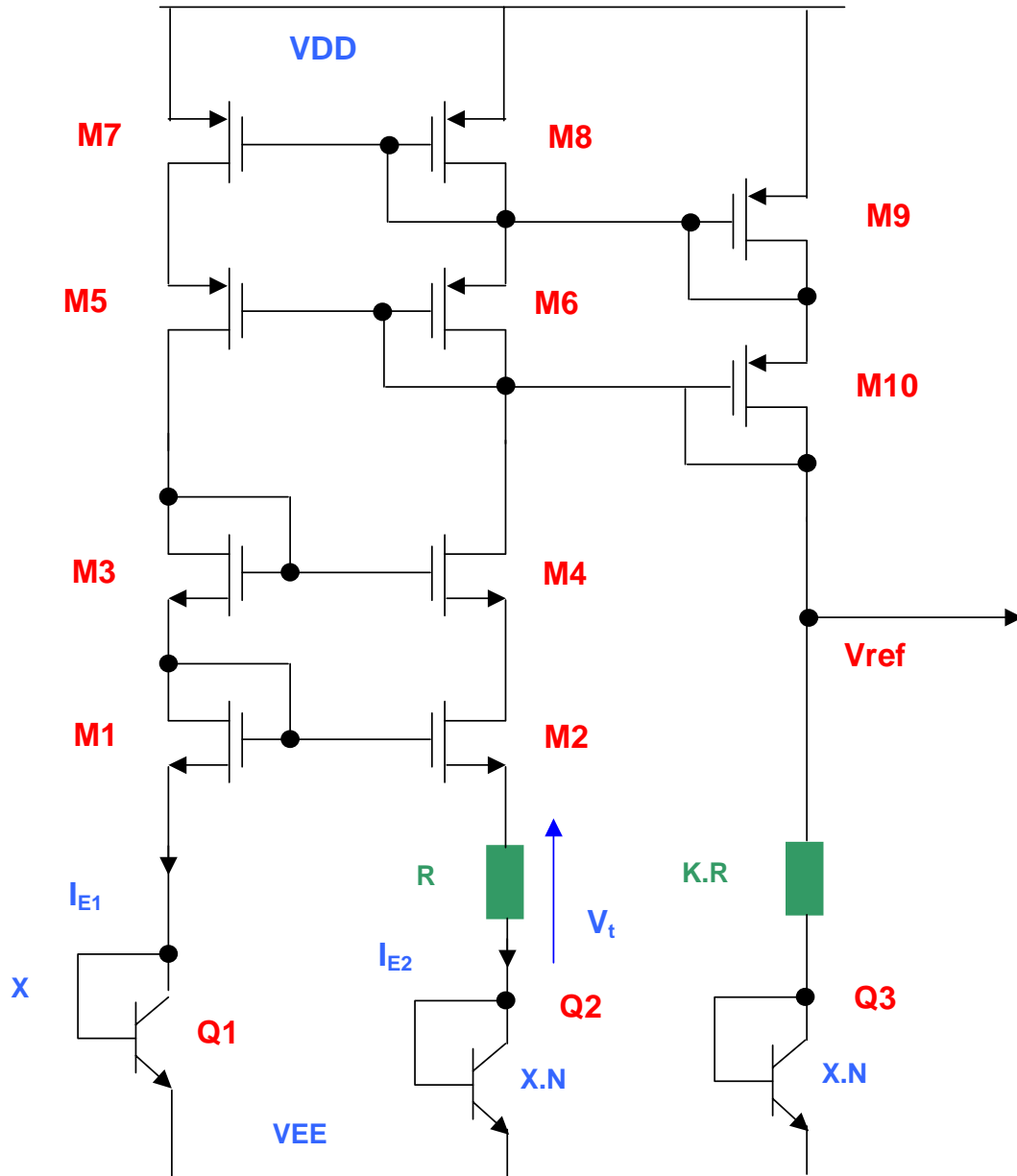
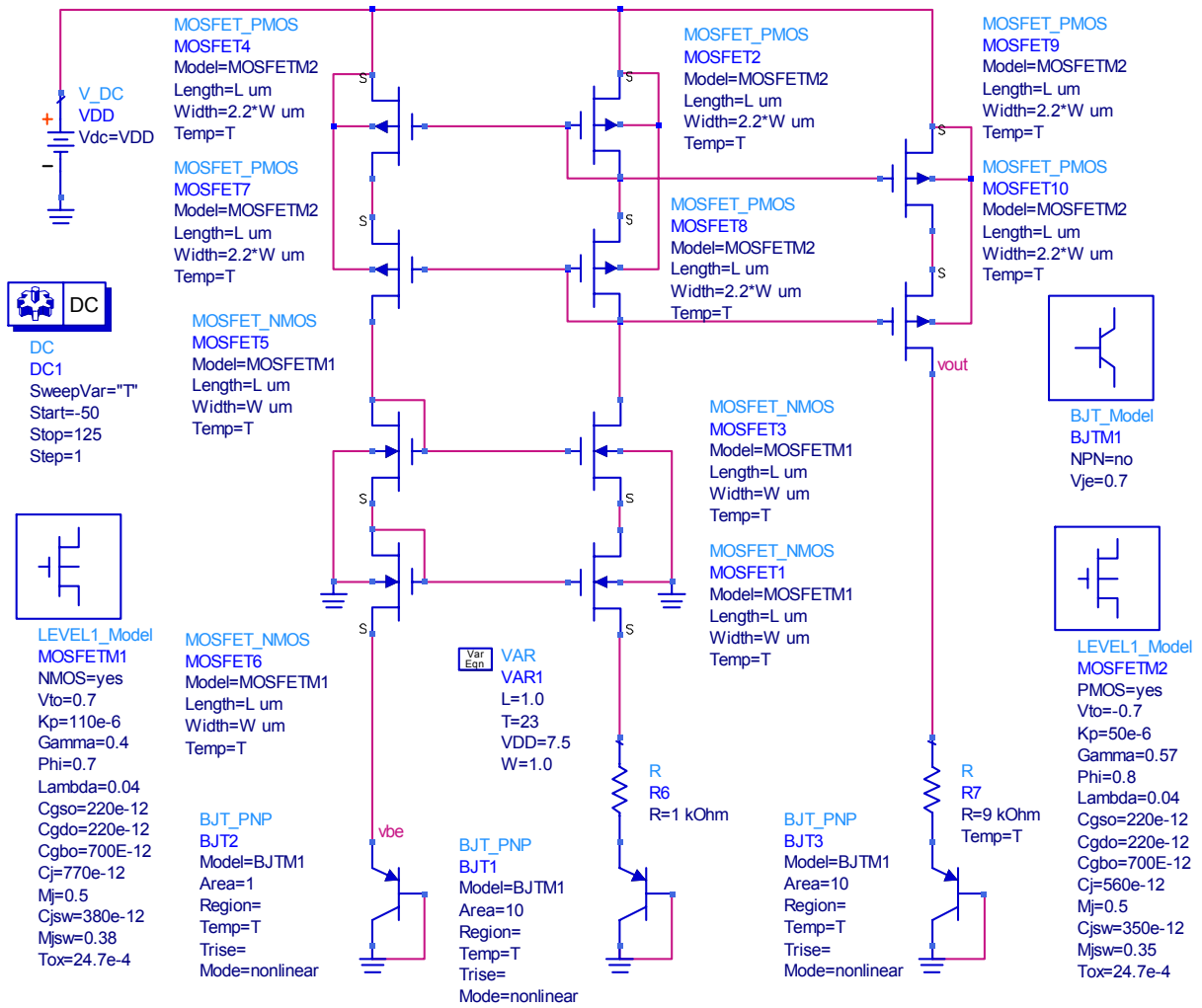
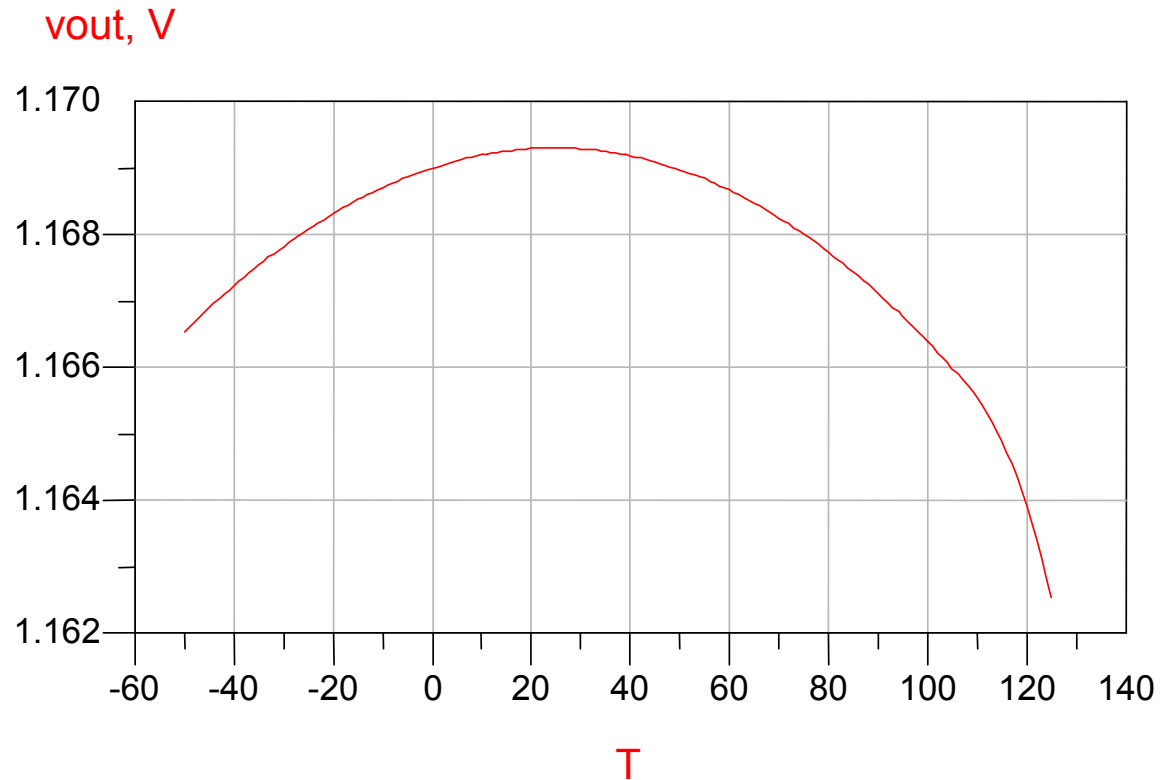


Figure 8 Circuit of the bandgap reference used in the example.

The Bandgap circuit of Figure 8 was entered as a schematic into ADS as shown in figure and analysed using a DC simulation block. For the simulation, the Temperature variable was added to the active devices and resistor and the resistor initially set to 10K was varied until the correct compensated curve resulted.



**Figure 9 ADS schematic setup for analysing the bandgap example circuit. R7 was initially set to 10K (as per the hand calculations) and then varied to optimise the bandgap voltage vs temperature curve shown in Figure 10**



**Figure 10** Resulting plot from the simulation shown in Figure 8. For this simulation the temperature parameter for the active devices and resistor was varied over the temperature range  $-50$  to  $125$  deg C using the parameter sweep within the DC simulation block.

One disadvantage of the example circuit is the headroom required on the supply rails. This is because there are  $4 V_{SAT} + V_T$  and a  $V_{be}$ , resulting in the need to raise the supply from the nominal  $+5V$  to  $+7.5V$ . Lower rail circuits tend to use low supply differential op-amp circuits.